

Scilab Textbook Companion for  
Solid State Physics: Structure And Properties  
Of Materials  
by M. A. Wahab<sup>1</sup>

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# Book Description

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Scilab numbering policy used in this document and the relation to the above book.

**Exa** Example (Solved example)

**Eqn** Equation (Particular equation of the above book)

**AP** Appendix to Example(Scilab Code that is an Appednix to a particular Example of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means a scilab code whose theory is explained in Section 2.3 of the book.

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# Chapter 1

## Atoms in Crystals

Scilab code Exa 1.1 Relationship among crystal elements

```
1 // Scilab Code Ex1.1 Relationship among crystal
  elements: Page-2 (2010)
2 f = 18; // Number of faces of the quartz crystal
3 c = 14; // Number of angles in the quartz crystal
4 // The relationship amongst the crystal elements can
  be
5 // expressed by the following formula:
6 //  $f + c = e + 2$ ;
7 // Solving for e
8 e = f + c - 2;
9 disp (e, "The number of edges of the quartz crystal
  is : ");
10
11 // Result
12 // The number of edges of the quartz crystal is :
13 // 30
```

---

Scilab code Exa 1.2 Primitive unit cell

```

1 // Scilab Code Ex1.2 Primitive unit cell: Page-4
  (2010)
2 a = 3, b = 3; // Lattice translation vectors
  along X and Y direction , angstrom
3 c_bar = 3; // Assumed translation vector along Z
  direction , angstrom
4 c = 1.5*(a+b+c_bar); // Real translation vector
  along Z direction , angstrom
5 printf("\n%3.1f is the body centered position of a
  cubic unit cell defined by the primitive
  translation vectors a, b and c_bar.", c);
6 V_con = a^3; // Volume of conventional unit cell ,
  metre cube
7 V_primitive = 1/2*V_con; // Volume of primitive
  unit cell , metre cube
8 printf("\nThe volume of conventional unit cell: %2d
  angstrom cube", V_con);
9 printf("\nThe volume of primitive unit cell: %4.1f
  angstrom cube", V_primitive);
10
11 // Result
12 // 13.5 is the body centered position of a cubic
  unit cell defined by the primitive translation
  vectors a, b and c_bar.
13 // The volume of conventional unit cell: 27 angstrom
  cube
14 // The volume of primitive unit cell: 13.5 angstrom
  cube

```

---

### Scilab code Exa 1.3 Number of Lattice points per unit cell

```

1 // Scilab Code Ex1.3 Number of Lattice points per
  unit cell Page-9 (2010)
2 a = 3.60D-10; // Lattice parameter , m:
3 M = 63.6; // Atomic weight , gram per mole

```

```

4 d = 8960D+03;    // Density of copper , g per metre
    cube
5 N = 6.023D+23;    // Avogadro 's No.
6 // Volume of the unit cell is given by
7 //  $a^3 = M*n/(N*d)$ 
8 // Solving for n
9 n = a^3*d*N/M; // Number of lattice points per unit
    cell
10 disp (n, "The number of atoms per unit cell for an
    fcc lattice of copper crystal is :");
11
12 // Result
13 // The number of atoms per unit cell for an fcc
    lattice of copper crystal
14 // 3.9588702

```

---

#### Scilab code Exa 1.4 Lattice constant of a unit cell

```

1 // Scilab Code Ex 1.4 Lattice constant of a unit
    cell: Page-9 (2010)
2 M = 58.5;        // Atomic weight of NaCl, gram per
    mole
3 d = 2180D+03;    // Density of rock salt , per metre
    cube
4 n = 4;          // No. of atoms per unit cell for an fcc
    lattice of NaCl crystal
5 N = 6.023D+23;    // Avogadro 's No.
6 // Volume of the unit cell is given by
7 //  $a^3 = M*n/(N*d)$ 
8 // Solving for a
9 a = (n*M/(d*N))^(1/3); // Lattice constant of
    unit cell of NaCl
10 disp (a/1D-10, "Lattice constant for the rock salt (
    NaCl) crystal , in angstrom , is : ");
11

```

```
12 // Result
13 // Lattice constant for the rock salt (NaCl) crystal
    , in angstrom, is :
14 // 5.6275
```

---

### Scilab code Exa 1.5 Density of diamond

```
1 // Scilab Code Ex 1.5 Density of diamond: Page-9
    (2010)
2 a = 3.57D-10; // Lattice parameter of a diamond
    crystal
3 M = 12D-03; // Atomic weight of diamond, kg per
    mole
4 n1 = 8; // No. of corner atoms in the diamond
    cubic unit cell
5 n2 = 6; // No. of face centered atoms in the
    diamond cubic unit cell
6 n3 = 4; // No. of atoms completely within the
    unit cell
7 n = 1/8*n1+1/2*n2+1*n3; // No. of atoms per unit
    cell for an fcc lattice of NaCl crystal
8 N = 6.023D+23; // Avogadro's No.
9 // Volume of the unit cell is given by
10 //  $a^3 = M*n/(N*d)$ 
11 // Solving for d
12 d = M*n/(N*a^3); // Density of diamond cubic unit
    cell
13 disp (round(d), "Density of diamond cubic unit cell,
    in kg per metre cube, is : ");
14
15 // Result
16 // Density of diamond cubic unit cell, in kg per
    metre cube, is :
17 // 3503
```

---

### Scilab code Exa 1.6 Calculating Unit cell dimensions

```
1 // Scilab Code Ex 1.6 Calculating Unit cell
  dimensions: Page-9 (2010)
2 d = 2.7D+03; // Density of fcc structure of
  aluminium, kg per metre cube
3 M = 26.98D-03; // Atomic weight of aluminium, kg
  per mole
4 n = 4; // No. of atoms per unit cell of fcc
  lattice structure of aluminium
5 N = 6.023D+23; // Avogadro's No.
6 // Volume of the unit cell is given by
7 //  $a^3 = M*n/(N*d)$ 
8 // Solving for a
9 a = ((M*n)/(N*d))^(1/3); // Lattice parameter of
  aluminium unit cell
10 // For an fcc crystal lattice,
11 //  $2^{(1/2)} = 4R = 2D$ 
12 // Solving for D
13 D = (a/2^(1/2)); // Diameter of aluminium atom
14 disp(a/1D-10, "The Lattice parameter of aluminium,
  in angstrom, is : ");
15 disp(D/1D-10, "The diameter of aluminium atom, in
  angstrom, is : ");
16
17 // Result
18 // The Lattice parameter of aluminium, in angstrom,
  is :
19 // 4.0486332
20 // The diameter of aluminium atom, in angstrom, is :
21 // 2.862816
```

---



**Scilab code Exa 1.17** Angle between two crystal directions

```
1 // Scilab Code Ex 1.17 Angle between two crystal
  directions: Page-23 (2010)
2 h1 = 1;k1 = 1;l1 = 1; // Miller indices of first set
  of planes
3 h2 = 0;k2 = 0;l2 = 1; // Miller indices of second
  set of planes
4 // We know that
5 //  $\cos(\theta) = (h_1h_2+k_1k_2+l_1l_2)/(\sqrt{h_1^2+k_1^2+l_1^2}*\sqrt{h_2^2+k_2^2+l_2^2})$ 
6 // Solving for theta
7 theta = acos((h1*h2+k1*k2+l1*l2)/(sqrt(h1^2+k1^2+l1
  ^2)*sqrt(h2^2+k2^2+l2^2)));
8 printf("\nThe angle between [%d%d%d] and [%d%d%d]
  directions in the cubic crystal, in degrees, is :
  %4.2f", h1,k1,l1,h2,k2,l2, theta*180/pi);
9
10 // Result
11 // The angle between [111] and [001] directions in
  the cubic crystal, in degrees, is :
12 //      54.74
```

---

**Scilab code Exa 1.18** Angle between two directions of cubic crystal

```
1 // Scilab Code Ex 1.18 Angle between two directions
  of cubic crystal: Page-23(2010)
2 h1 = 1; k1 = 1; l1 = 1 // Miller indices for first
  set of planes
3 h2 = -1; k2 = -1; l2 = 1; // Miller indices for
  second set of planes
4 // We know that
5 //  $\cos(\theta) = (h_1h_2+k_1k_2+l_1l_2)/(\sqrt{h_1^2+k_1^2+l_1^2}*\sqrt{h_2^2+k_2^2+l_2^2})$ 
6 // Solving for theta
```

```

7 theta = acos((h1*h2+k1*k2+l1*l2)/(sqrt(h1^2+k1^2+l1
      ^2)*sqrt(h2^2+k2^2+l2^2)));
8 printf("\nThe angle between [%d%d%d] and [%d %d %d]
      directions in the cubic crystal, in degrees, is :
      %4.1f", h1,k1,l1,h2,k2,l2, theta*180/%pi);
9
10 // Result
11 // The angle between [111] and [-1-1 1] directions
      in the cubic crystal, in degrees, is :
12 //      109.5

```

---

**Scilab code Exa 1.19** Miller indices of the crystal plane

```

1 // Scilab Code Ex 1.19 Miller indices of the crystal
      plane: Page-25 (2010)
2 m = 2; n = 3; p = 6; // Coefficients of intercepts
      along three axes
3 m_inv = 1/m; // Reciprocate the first
      coefficient
4 n_inv = 1/n; // Reciprocate the second
      coefficient
5 p_inv = 1/p; // Reciprocate the third
      coefficient
6 mul_fact = double(lcm(int32([m,n,p]))); // Find l.c.
      m. of m,n and p
7 m1 = m_inv*mul_fact; // Clear the first fraction
8 m2 = n_inv*mul_fact; // Clear the second fraction
9 m3 = p_inv*mul_fact; // Clear the third fraction
10 printf("\nThe required miller indices are : (%d %d
      %d) ", m1,m2,m3);
11
12 // Result
13 // The required miller indices are : (3 2 1)

```

---

### Scilab code Exa 1.20 Indices of lattice plane

```
1 // Scilab Code Ex 1.20 Indices of lattice plane:
   Page-25 (2010)
2 m = 10000; // Coefficient of intercept along x-axis,
   can be taken as some large value
3 n = 2;    // Coefficient of intercept along y-axis
4 p = 1/2;  // Coefficient of intercept along z-axis
5 m_inv = 1/m; // Reciprocate m
6 n_inv = 1/n; // Reciprocate n
7 p_inv = 1/p; // Reciprocate p
8 mul_fact = n; // multiplicative factor
9 m1 = m_inv*mul_fact; // Clear the first fraction
10 m2 = n_inv*mul_fact; // Clear the second fraction
11 m3 = p_inv*mul_fact; // Clear the third fraction
12 printf("\nThe required miller indices are : %d, %d,
   %d ", m1,m2,m3);
13
14 // Result
15 // The required miller indices are :
16 //      0, 1, 4
```

---

### Scilab code Exa 1.21 Length of the intercepts

```
1 // Scilab Code Ex 1.21 Length of the intercepts:
   Page-26 (2010)
2 a = 1.21D-10; // Lattice parameter of the unit
   cell , m
3 b = 1.84D-10; // Lattice parameter of the unit
   cell , m
4 c = 1.97D-10; // Lattice parameter of the unit
   cell , m
```

```

5 p = 1/2;    // Reciprocal of miller index on x-axis
6 q = 1/3;    // Reciprocal of miller index on y-axis
7 r = 1/(-1); // Reciprocal of miller index on z-
    axis
8 l1 = 1.21D-10; // Actual length of the intercept
    along x-axis , m
9 mul_fact = l1/(p*a); // Calculate multiplication
    factor
10 l2 = mul_fact*q*b; // Actual length of the
    intercept along y-axis , m
11 l3 = mul_fact*r*c; // Actual length of the
    intercept along z-axis , m
12 disp(l2/1D-10, "The length of the intercept along y-
    axis , in angstrom , is : ");
13 disp(l3/1D-10, "The length of the intercept along z-
    axis , in angstrom , is : ");
14
15 // Result
16 // The length of the intercept along y-axis , in
    angstrom , is :
17 //      1.2266667
18 // The length of the intercept along z-axis , in
    angstrom , is :
19 //      - 3.94

```

---

### Scilab code Exa 1.22 Miller indices of lattice planes

```

1 // Scilab Code Ex 1.22 Miller indices of lattice
    plane: Page-26 (2010)
2 a = 4;    // Lattice parameter of the unit cell
3 b = 3;    // Lattice parameter of the unit cell
4 c = 2;    // Lattice parameter of the unit cell
5 l1 = 2;   // Length of the intercept along x-axis ,
    m
6 l2 = 3;   // Length of the intercept along y-axis ,

```

```

7   m
   l3 = 4;    // Length of the intercept along z-axis,
   m
8   l = l1/a; // Intercept per unit translation along
   x-axis
9   m = l2/b; // Intercept per unit translation along
   y-axis
10  n = l3/c; // Intercept per unit translation along
   z-axis
11  r1 = 1/l; // Reciprocal of l
12  r2 = 1/m; // Reciprocal of m
13  r3 = 1/n; // Reciprocal of n
14  m1 = 2*r1; // miller index along x-axis
15  m2 = 2*r2; // miller index along y-axis
16  m3 = 2*r3; // miller index along z-axis
17  printf("The required miller indices of the plane are
   : %d %d %d", m1, m2, m3);
18
19  // Result
20  // The required miller indices of the plane are :
21  //      4, 2, 1

```

---

### Scilab code Exa 1.23 Indices of tetragonal lattice

```

1 // Scilab Code Ex 1.23 Indices of tetragonal lattice
   : Page-26 (2010)
2 // For a tetragonal system we have a = b
3 a = 1; // Lattice parameter of the unit cell
   along x-axis
4 b = 1; // Lattice parameter of the unit cell
   along y-axis
5 c = 1.5; // Lattice parameter of the unit cell
   along z-axis
6 l1 = 3; // Length of the intercept along x-axis,
   angstrom

```

```

7 l2 = 4;    // Length of the intercept along y-axis ,
    angstrom
8 l3 = 3;    // Length of the intercept along z-axis ,
    angstrom
9 l  = l1/a;  // Intercept per unit translation along
    x-axis
10 m = l2/b;  // Intercept per unit translation along
    y-axis
11 n = l3/c;  // Intercept per unit translation along
    z-axis
12 r1 = 1/l;  // Reciprocal of l
13 r2 = 1/m;  // Reciprocal of m
14 r3 = 1/n;  // Reciprocal of n
15 mul_fact = double(lcm(int32([l,m,n])));
16 m1 = mul_fact*r1;    // miller index along x-axis
17 m2 = mul_fact*r2;    // miller index along y-axis
18 m3 = mul_fact*r3;    // miller index along z-axis
19 printf("The required miller indices of the plane are
    : %d %d %d", m1, m2, m3);
20
21 // Result
22 // The required miller indices of the plane are : 4
    3 6

```

---

**Scilab code Exa 1.24 Miller Bravias indices for Miller indices**

```

1 // Scilab Code Ex 1.24 Miller–Bravias indices for
    Miller indices: Page–29 (2010)
2 function [i] = f(h,k)
3     i = -(h + k);
4 endfunction
5 h1 = 1; k1 = 1; l1 = 0 ; // First set of Miller
    indices
6 h2 = 1; k2 = -1; l2 = 0; // Second set of miller
    indices

```

```

7 h3 = 3; k3 = 4; l3 = 5;    // Third set of miller
  indices
8 h4 = 3; k4 = -4; l4 = 5;  // Fourth set of miller
  indices
9 printf("\nThe Miller-Bravias indices corresponding
  to the miller indices (%d %d %d), = (%d %d %d %d)
  ", h1, k1, l1, h1, k1, f(h1,k1), l1);
10 printf("\nThe Miller-Bravias indices corresponding
  to the miller indices (%d %d %d), = (%d %d %d %d)
  ", h2, k2, l2, h2, k2, f(h2,k2), l2);
11 printf("\nThe Miller-Bravias indices corresponding
  to the miller indices (%d %d %d), = (%d %d %d %d)
  ", h3, k3, l3, h3, k3, f(h3,k3), l3);
12 printf("\nThe Miller-Bravias indices corresponding
  to the miller indices (%d %d %d), = (%d %d %d %d)
  ", h4, k4, l4, h4, k4, f(h4,k4), l4);
13
14 // Result
15 // The Miller-Bravias indices corresponding to the
  miller indices (1 1 0), = (1 1 -2 0)
16 // The Miller-Bravias indices corresponding to the
  miller indices (1 -1 0), = (1 -1 0 0)
17 // The Miller-Bravias indices corresponding to the
  miller indices (3 4 5), = (3 4 -7 5)
18 // The Miller-Bravias indices corresponding to the
  miller indices (3 -4 5), = (3 -4 1 5)

```

---

#### Scilab code Exa 1.25 Miller Bravias indices of lattice plane

```

1 // Scilab Code Ex 1.25 Miller Bravias indices of
  lattice planes: Page-30 (2010)
2 function [h] = fh(H,K)    // Function for
  calculating (2H-K)/3
3   h = (2*H - K)/3;
4 endfunction

```

```

5
6 function [k] = fk(H,K) // Function for
   calculating (2K-H)/3
7     k = (2*K - H)/3;
8 endfunction
9
10 function [i] = f(h,k) // Function for calculating
    i
11     i = -(h + k);
12 endfunction
13
14 function [l] = fl(L) // Function for calculating
    l
15     l = L;
16 endfunction
17
18 H1 = 1; K1 = 0; L1 = 0 ; // First set of Miller
    indices
19 H2 = 0; K2 = 1; L2 = 0; // Second set of miller
    indices
20 H3 = 1; K3 = 1; L3 = 0; // Third set of miller
    indices
21
22 h1 = fh(H1,K1)*3; // Call function fh
23 k1 = fk(H1,K1)*3; // Call function fk
24 l1 = fl(L1)*3; // Call function fl
25 i1 = f(h1,k1); // Call function
26
27 h2 = fh(H2,K2)*3; // Call function fh
28 k2 = fk(H2,K2)*3; // Call function fk
29 l2 = fl(L2)*3; // Call function l2
30 i2 = f(h2,k2); // Call function f
31
32 h3 = fh(H3,K3)*3; // Call function fh
33 k3 = fk(H3,K3)*3; // Call function fk
34 l3 = fl(L3)*3; // Call function l3
35 i3 = f(h3,k3); // Call function f
36

```



```

37 printf("\n The Miller Bravias indices of [%d%d%d]
    are [%d %d %d %d]", H1, K1, L1, h1, k1, i1, l1);
38 printf("\n The Miller Bravias indices of [%d%d%d]
    are [%d %d %d %d]", H2, K2, L2, h2, k2, i2, l2);
39 printf("\n The Miller Bravias indices of [%d%d%d]
    are [%d %d %d %d]", H3, K3, L3, h3, k3, i3, l3);
40
41 // Result
42 // The Miller Bravias indices of [100] are [2 -1 -1
    0]
43 // The Miller Bravias indices of [010] are [-1 2 -1
    0]
44 // The Miller Bravias indices of [110] are [1 1 -2
    0]

```

---

#### Scilab code Exa 1.26 Lattice parameter of a cubic crystal

```

1 // Scilab Code Ex 1.26 Lattice parameter of a cubic
    crystal: Page-33 (2010)
2 h = 1; k = 1; l = 1; // Miller Indices for planes in
    a cubic crystal
3 d = 2D-10; // Interplanar spacing, m
4 // For cubic crystals, the interplanar spacing is
    given by
5 //  $d = a / (h^2 + k^2 + l^2)^{1/2}$ ;
6 // Solving for a
7 a = (h^2+k^2+l^2)^(1/2)*d; // lattice parameter of
    cubic crystal, m
8 disp(a/1D-10, "The lattice parameter of the cubic
    crystal, in angstrom, is :");
9
10 // Result
11 // The lattice parameter of the cubic crystal, in
    angstrom, is :
12 // 3.4641016

```

---

**Scilab code Exa 1.27** Interplanar spacing in tetragonal crystal

```
1 // Scilab Code Ex 1.27 Interplanar spacing in
   tetragonal crystal: Page-33 (2010)
2 h = 1; k = 0; l = 1; // Miller Indices for planes in
   a cubic crystal
3 a = 2.42D-10; b = 2.42D-10; c = 1.74D-10; //
   Lattice parameters of a tetragonal crystal, each
   in m
4 d = [(h^2+k^2)/a^2 + l^2/c^2]^(-1/2); // The
   interplanar spacing for cubic crystal, m
5 disp(d/1D-10, "The interplanar spacing between
   consecutive (101) planes : in angstrom, is :");
6
7 // Result
8 // The interplanar spacing between consecutive (101)
   planes : in angstrom, is :
9 // 1.4127338
```

---

**Scilab code Exa 1.28** Interplanar spacing in cubic crystal

```
1 // Scilab Code Ex 1.28 Interplanar spacing in cubic
   crystal: Page-36 (2010)
2 h = 3; k = 2; l = 1; // Miller Indices for planes in
   a cubic crystal
3 a = 4.21D-10; // Interatomic spacing, m
4 d = a/(h^2+k^2+l^2)^(1/2); // The interplanar
   spacing for cubic crystals, m
5 disp(d/1D-10, "The interplanar spacing between
   consecutive (321) planes : in angstrom, is :");
6
```

```
7 // Result
8 // The interplanar spacing between consecutive (321)
   planes : in angstrom, is :
9 // 1.1251698
```

---

## Chapter 2

# Atomic Bonding

Scilab code Exa 2.1 Molecular stability based on bond dissociation energy

```
1 // Scilab Code Ex2.1 Stability of molecule based on
  bond dissociation energy: Page-61 (2010)
2 e = 1.6D-19; // Electronic charge, C
3 N = 6.023D+23; // Avogadro's number
4 e0 = 8.854D-12; // Absolute Electrical permittivity
  of free space, coulomb square per newton per
  metre square
5 Re = 3D-10; // Equilibrium separation, m
6 IE = 502; // First ionization energy of A, kJ/mol
7 EA = 335; // Electron affinity for atom B, kJ/mol
8 IS = 3D-10; // Interatomic separation between A+
  and B-, m
9 Ue = -(e^2*N)/(4*pi*e0*Re*1D+3); // Potential
  energy at equilibrium separation of A+B- molecule
  , kJ/mol
10 DE = Ue + IE - EA; // Bond dissociation energy of A+
  B- molecule, kJ/mol
11 printf("\nThe bond dissociation energy of A+B-
  molecule is : %d kJ/mol", DE);
12 if (DE < 0)
13     disp("The molecule A+B- is stable..");
```

```

14 else
15     disp("The molecule A+B- is unstable..");
16 end
17
18 //Result
19 //     The bond dissociation energy of A+B- molecule ,
        in kJ/mol, is : -294
20 //     The molecule A+B- is stable..

```

---

### Scilab code Exa 2.2 Conversion of eV into kcal per mol

```

1 // Scilab Code Ex2.2 Conversion of eV into kcal/mol:
        Page-64 (2010)
2 e = 1.6D-19; // Electronic charge , C
3 N = 6.023D+23; // Avogadro 's number
4 J = 4.184D+3; // Joule 's mechanical equivalent of
        heat
5 V = 1; // Potential difference , V
6 eV = e*V; // Energy equivalent of 1 electron-volt , J
7 eVpm = eV*N; // Electron-volt per mole , J/mol
8 Ecal = eVpm/J; // Energy equivalent of 1eV, kcal/
        mole
9 printf("\n1 eV is approximately equal to %6.3f kcal/
        mol" , Ecal);
10
11 //Result
12 //     1 eV is approximately equal to 23.033 kcal/mol

```

---

### Scilab code Exa 2.3 Potential energy of the ionic solids

```

1 // Scilab Code Ex2.3 Potential energy of the system
        of Na+ and Cl- ions: Page-68 (2010)
2 e = 1.6D-19; // Electronic charge , C

```

```

3 ep_0 = 8.854D-12; // Absolute electrical
    permittivity of free space, coulomb square per
    newton per metre square
4 Re = 2D-10; // Equilibrium separation between Na+
    and Cl- ions, m
5 U = -e/(4*pi*ep_0*Re); // Potential energy of NaCl
    molecule at equilibrium separation, electron-volt
6 printf("\nThe potential energy of NaCl molecule at
    equilibrium separation5 is : %3.1f eV", U);
7
8 //Result
9 // The potential energy of NaCl molecule at
    equilibrium separation5 is : -7.2 eV

```

---

#### Scilab code Exa 2.4 Compressibility and energy of ionic crystal

```

1 // Scilab Code Ex2.4 Compressibility and ionic
    energy of NaCl crystal: Page-68 (2010)
2 e = 1.6D-19; // Electronic charge, C
3 ep_0 = 8.854D-12; // Absolute electrical
    permittivity of free space, coulomb square per
    newton per metre square
4 Re = 2.81D-10; // Equilibrium separation between Na+
    and Cl- ions, m
5 A = 1.7496; // Madelung constant
6 n = 9; // Power of R in the repulsive term of
    potential energy of two particles
7 IP_Na = 5.14; // Ionization potential of sodium, eV
8 EA_Cl = 3.61; // Electron Affinity of chlorine, eV
9 K0 = (72*pi*ep_0*Re^4)/((n - 1)*A*e^2); //
    Compressibility of NaCl crystal, metre square
    newton
10 U = -(A*e)/(4*pi*ep_0*Re)*(1-1/n); // Potential
    energy of NaCl molecule at equilibrium separation
    , elct

```

```

11 U_bar = U/2; // Potential energy per ion, electron-
    volt
12 delta_E = IP_Na - EA_Cl; // Energy required to
    produce the ion-pair, eV
13 E_ion = delta_E/2; // Energy required to produce per
    ion, eV
14 C_E = U_bar + E_ion; // Cohesive energy per ion, eV
15 printf("\nThe compressibility of NaCl crystal is %4
    .2e metre square newton", K0);
16 printf("\nThe cohesive energy of NaCl crystal is %4
    .2f eV", C_E);
17
18 // Result
19 // The compressibility of NaCl crystal is 3.48e-011
    metre square newton
20 // The cohesive energy of NaCl crystal is -3.21 eV

```

---

**Scilab code Exa 2.5** Potential energy and dissociation energy of a diatomic molecule

```

1 // Scilab Code Ex2.5 Potential energy and
    dissociation energy of a diatomic molecule: Page
    -69 (2010)
2 e = 1.6D-19; // Electronic charge, C
3 A = 1.44D-39; // Constant corresponding to the
    attractive term in potential energy, joule metre
    square
4 B = 2.19D-115; // Constant corresponding to the
    repulsive term in potential energy, joule metre
    raised to power 10
5 Re = (5*B/A)^(1/8); // Equilibrium spacing of
    diatomic molecule, m
6 n = 2; // Power of R in the attractive term of
    potential energy of two particles
7 m = 10; // Power of R in the repulsive term of
    potential energy of two particles

```

```

8 D = A/(Re^2*e)*(1-n/m); // Dissociation energy of
   diatomic molecule , eV
9 printf("\nThe equilibrium spacing of diatomic
   molecule is %4.2e m", Re);
10 printf("\nThe dissociation energy of diatomic
   molecule is %4.2e eV", D);
11
12 //Result
13 // The equilibrium spacing of diatomic molecule is
   4.08e-010 m
14 // The dissociation energy of diatomic molecule is
   4.34e-002 eV

```

---

**Scilab code Exa 2.6** Binding force and critical separation of a diatomic molecule

```

1 // Scilab Code Ex2.6 Binding force and critical
   separation of a diatomic molecule: Page-69 (2010)
2 Re = 3D-10; // Equilibrium spacing of diatomic
   molecule , m
3 e = 1.6D-19; // Electronic charge , C
4 D = 4*e; // Dissociation energy of diatomic molecule
   , eV
5 n = 2; // Power of R in the attractive term of
   potential energy of two particles
6 m = 10; // Power of R in the repulsive term of
   potential energy of two particles
7 Ue = -D; // Potential energy of diatomic molecule at
   equilibrium separation , joule
8 A = -(Ue*Re^n)/(1-n/m); // Constant corresponding to
   the attractive term in potential energy , joule
   metre square
9 B = A*Re^8/5; // Constant corresponding to the
   repulsive term in potential energy , joule metre
   raised to power 10
10 Rc = (55/3*B/A)^(1/8); // Critical separation

```



```

    between the nuclei, m
11 F_min = -2*A/Rc^3*(1-(Re/Rc)^8); // The minimum
    force required to dissociate the molecule, N
12 disp(A,"The constant A corresponding to the
    attractive potential energy, in joule metre
    square, is :");
13 disp(B,"The constant B corresponding to the
    repulsive potential energy, in joule metre raised
    to power 10, is :");
14 disp(Rc/1d-10, "The critical separation between the
    nuclei, in angstrom, is : ");
15 disp(F_min, "The minimum force required to
    dissociate the molecule, in N, is : ");
16
17 //Result
18 // The constant A corresponding to the attractive
    potential energy, in joule metre square, is :
    // 7.200D-38
19 // The constant B corresponding to the repulsive
    potential energy, in joule metre raised to power
    10, is : // 9.44D-115
20 // The critical separation between the nuclei, in
    angstrom, is :
21 // 3.529D-10
22 // The minimum force required to dissociate the
    molecule, in N, is :
23 // -2.383D-09

```

---

### Scilab code Exa 2.7 Bond formation energy of ionic solid

```

1 // Scilab Code Ex2.7 Bond formation Energy for K+
    and Cl- ion pair: Page-70 (2010)
2 eps_0 = 8.854D-12; // Absolute electrical
    permittivity of free space, coulomb sqaure per
    newton per metre square

```

```

3 e = 1.6D-19; // Electronic charge, C
4 IP_K = 4.1; // Ionization potential of potassium,
    electron-volt
5 EA_Cl = 3.6; // Electron affinity of chlorine,
    electron-volt
6 delta_E = IP_K - EA_Cl; // Net energy required to
    produce the ion-pair, electron-volt
7 Ec = delta_E; // Coulomb energy equals net energy
    required to produce the ion pair, in electron-
    volt
8 // Since  $E_c = -e/(4*\%pi*\epsilon_0*R)$ , solving for R
9 R = -e/(4*\%pi*\epsilon_0*Ec); // Separation between K+
    and Cl- ion pair, m
10 disp(Ec,"The bond formation energy for K+ and Cl-
    ion pair, in eV, is : ");
11 disp(R/1D-10, "The separation between K+ and Cl- ion
    pair, in angstrom, is : ");
12
13 //Result
14 // The bond formation energy for K+ and Cl- ion pair
    , in eV, is :
15 // 0.5
16 // The separation between K+ and Cl- ion pair, in
    angstrom, is :
17 // - 28.760776

```

---

### Scilab code Exa 2.8 Energy liberation during electron transfer

```

1 // Scilab Code Ex2.8 Energy liberated during
    electron transfer between ions of a molecule:
    Page-71 (2010)
2 eps_0 = 8.854D-12; // Absolute electrical
    permittivity of free space, coulomb sqaure per
    newton per metre square
3 e = 1.6D-19; // Electronic charge, C

```

```

4 R = 5D-10;    // Separation between the ions M and X
    , m
5 IP_M = 5;    // Ionization potential of M, eV
6 EA_X = 4;    // Electron affinity of X, eV
7 U = -e/(4*pi*eps_0*R); // The potential energy of
    MX molecule, eV
8 delta_E = IP_M - EA_X; // The net energy required to
    produce the ion pair, eV
9 Er = delta_E + U; // Energy required to transfer an
    electron from M to X atom, eV
10 printf("\nThe energy required to transfer an
    electron from M to X atom = %4.2f eV", Er);
11
12 //Result
13 // The energy required to transfer an electron from
    M to X atom = -1.88 eV

```

---

# Chapter 3

## Atomic Packing

Scilab code Exa 3.1 Packing of spheres in 2D square lattice

```
1 // Scilab Code Ex3.1 Packing of equal spheres in two
  dimensional square lattice: Page-88 (2010)
2 // Here we may assume square of unit length i.e. a =
  1 such that radius of sphere, R = a/2 = 0.5
3 a = 1; // Length of the side of the square, unit
4 R = a/2; // Radius of the sphere, unit
5 r = (sqrt(2)-1)*R; // Radius of the sphere
  introduced within the void produced by the
  packing of equal spheres on square lattice, unit
6 A = %pi*R^2; // Area associated with a sphere,
  square units
7 FA = a^2-A; // Free area occupied by void in
  square lattice, square units
8 FA_per = FA*100; // Percentage free area in
  square lattice
9 printf("\nFree area in square lattice is : %4.1f
  percent", FA_per);
10 //Result
11 // Free area in square lattice is : 21.5 percent
```

---

### Scilab code Exa 3.2 Packing efficiency in diamond structure

```
1 // Scilab Code Ex3.2 Packing efficiency in diamond
   structure: Page-92 (2010)
2 // For simplicity we may take radius of the atom, R
   = 1 unit
3 R = 1; // Radius of the atom in bcc lattice , unit
4 nc = 8; // Number of corner atoms in diamond
   structure
5 nfcc = 6; // Number of face centred atoms in
   diamond structure
6 na = 4; // Number of atoms completely within the
   unit cell
7 n = 1/8*nc+1/2*nfcc+1*na; // Effective number of
   atoms in the diamond structure
8 V_atom = 8*4/3*%pi*R^3; // Volume of atoms within
   the unit cell , unit cube
9 // Since for a diamond cubic crystal , the space
   lattice is fcc , with two atos per lattice point ,
   such that 8*R = sqrt(3)*a , solving for a
10 a = 8*R/sqrt(3); // lattice parameter of diamond
   structure , unit
11 V_cell = a^3; // Volume of the unit cell , unit
   cube
12 eta = V_atom/V_cell*100; // Packing efficiency in
   diamond structure
13 printf("\nThe packing efficiency in diamond
   structure is : %2.0f percent", eta);
14 //Result
15 // The packing efficiency in diamond structure is :
   34 percent
```

---

**Scilab code Exa 3.3** Radius of largest sphere at octahedral void

```
1 // Scilab Code Ex3.3 Radius of largest sphere that
   can be placed at the octahedral void: Page-100
   (2010)
2 // For simplicity we may take radius of the atom, R
   = 1 unit
3 R = 1; // Radius of the atom in bcc lattice , unit
4 // For a bcc lattice ,  $4R = a\sqrt{3}$ , solving for a
5 a = 4*R/sqrt(3); // lattice parameter of bcc crystal
   , unit
6 // Since  $R + R_x = a/2$ , solving for  $R_x$ 
7  $R_x = a/2 - R$ ; // Radius of the largest sphere that
   will fit into the octahedral void, unit
8 printf("\nThe radius of the largest sphere that will
   fit into the octahedral void is : %5.3fR", Rx);
9 //Result
10 // The radius of the largest sphere that will fit
   into the octahedral void is : 0.155R
```

---

**Scilab code Exa 3.4** Radius of largest sphere at tetrahedral void

```
1 // Scilab Code Ex3.4 Radius of largest sphere that
   can be placed at the tetrahedral void: Page-100
   (2010)
2 // For simplicity we may take radius of the atom, RL
   = 1 unit
3 RL = 1; // Radius of the atom in bcc lattice ,
   unit
4 // For a bcc lattice ,  $4RL = a\sqrt{3}$ , solving for
   a
5 a = 4*RL/sqrt(3); // Lattice parameter of bcc
   crystal , unit
6 // Further  $RL + R_x = \sqrt{5}*a/4$ , solving for  $R_x$ 
7  $R_x = \sqrt{5}*a/4 - RL$ ; // Radius of the largest
```

```

    sphere that will fit into the octahedral void ,
    unit
8  printf("\nThe radius of the largest sphere that will
    fit into the tetrahedral void is : %5.3fRL", Rx)
    ;
9  //Result
10 // The radius of the largest sphere that will fit
    into the tetrahedral void is : 0.291RL

```

---

**Scilab code Exa 3.5** Diameter of the largest atom at tetrahedral void

```

1  // Scilab Code Ex3.5 Diameter of the largest atom
    that would fit into the tetrahedral void:5 Page
    -101 (2010)
2  a = 3.52D-10;    // Lattice parameter for Ni, m
3  // For an fcc lattice , sqrt(2)*a = 4*R, solving for
    R
4  R = sqrt(2)*a/4;    // Radius of the atom in fcc
    lattice , m
5  R_oct = 0.414*R;    // Radius of the octahedral void
    in fcc close packing , m
6  D = 2*R_oct;    // Diameter of the octahedral void
    in the fcc structure of nickel , m
7  disp(D/1D-10, "The diameter of the octahedral void
    in the fcc structure of nickel , in angstrom , is :
    ");
8  //Result
9  // The diameter of the octahedral void in the fcc
    structure of nickel , in angstrom , is :
10 // 1.0304526

```

---

**Scilab code Exa 3.6** Void space in cubic close packing

```

1 // Scilab Code Ex3.6 Void space in cubic close
   packing: Page-101 (2010)
2 R = 1; // For simplicity, radius of the sphere, m
3 // For cubic close packing, side of the unit cell
   and the radius of the sphere is related as
4 //  $\sqrt{2} \cdot a = 4 \cdot R$ , solving for a
5 a = 2*sqrt(2)*R; // Lattice parameter for cubic
   close packing, m
6 V_cell = a^3; // Volume of the unit cell
7 n = 4; // Number of lattice points in fcc unit
   cell
8 V_occupied = 4*4/3*pi*((1.000)^3+(0.414)
   ^3+2*(0.225)^3); // Volume occupied by the atoms,
   metre cube
9 void_space = V_cell - V_occupied; // Void space
   in the close packing
10 percent_void = void_space/V_cell*100; // Percentage
   void space
11 printf("\nThe void space in the close packing is :
   %2.0f percent", percent_void);
12 //Result
13 // The void space in the close packing is : 19
   percent

```

---

**Scilab code Exa 3.7** The Minimum value of radius ratio in a compound

```

1 // Scilab Code Ex3.7 The minimum value of radius
   ratio in AX-compound: Page-104 (2010)
2 // For simplicity we may assume a = 1
3 a = 1; // Lattice parameter of the crystal, unit
4 b = 2/3*a*sin(pi/3); // Lattice parameter of the
   crystal, unit
5 // Here  $a = 2 \cdot R_x$ , where a is the lattice parameter
   and  $R_x$  is the radius of X-ions representing the
   bigger spheres, solving for  $R_x$ 

```



```
6 Rx = 0.5*a;
7 // Also b = RA + Rx, solving for RA
8 RA = b - Rx; // Radius of A-ion representing the
  smaller sphere, unit
9 Rad_ratio = RA/Rx; // Radius ratio in AX compound
10 printf("\nThe minimum value of radius ratio in AX
  compound is : %5.3f", Rad_ratio);
11 // Result
12 // The minimum value of radius ratio in AX compound
  is : 0.155
```

---

# Chapter 4

## Atomic Shape and Size

Scilab code Exa 4.1 Bohr orbit for the hydrogen atom

```
1 // Scilab Code Ex4.1 Bohr's orbit for the hydrogen
  atom: Page-126 (2010)
2 n = 1; // The ground state orbit of hydrogen atom
3 Z = 1; // The atomic number of hydrogen
4 h = 6.626D-34; // Plank's constant, Js
5 eps_0 = 8.85D-12; // Absolute electrical
  permittivity of free space, coulomb square per
  newton per metre square
6 e = 1.602D-19; // Electronic charge, C
7 m = 9.1D-31; // Electronic mass, kg
8 r_B = (n^2*h^2*eps_0)/(%pi*m*Z*e^2); // Radius of
  first Bohr's orbit (Bohr radius), m
9 disp(r_B/1D-10, "The radius of first Bohr orbit, in
  angstrom, is : ");
10 // Result
11 // The radius of first Bohr orbit, in angstrom, is :
12 // 0.5295779
```

---

Scilab code Exa 4.2 Ionization potentials of hydrogen atom

```

1 // Scilab Code Ex4.2 Ionization potentials of
  hydrogen atom: Page-126 (2010)
2 Z = 1; // The atomic number of hydrogen
3 h = 6.626D-34; // Plank's constant, Js
4 eps_0 = 8.85D-12; // Absolute electrical
  permittivity of free space, coulomb square per
  newton per metre square
5 e = 1.602D-19; // Electronic charge, C
6 m = 9.1D-31; // Electronic mass, kg
7 E = zeros(1, 3); // Initialize three potentials to 0
  value in a vector
8 for n = 1:1:3
9     select n
10    case 1 then
11        state = "First";
12    case 2 then
13        state = "Second";
14    else
15        state = "Third";
16    end
17 E(1,n) = -(m*Z^2*e^4)/(8*eps_0^2*n^2*h^2*e); //
  Energy of nth bohr orbit, eV
18 printf("\nThe %s Ionization Potential is : %5.3f eV"
  ,state, E(1,n));
19 end
20 // Result
21 // The First Ionization Potential is : -13.600 eV
22 // The Second Ionization Potential is : -3.400 eV
23 // The Third Ionization Potential is : -1.511 eV

```

---

#### Scilab code Exa 4.3 Univalent radii of ions

```

1 // Scilab Code Ex4.3 Univalent radii of ions: Page
  -130 (2010)
2 S = 4.52; // Screening constant for neon like

```

```

        configurations
3  Cn = 1;      // A constant determined by the quantum
        number, m; for simplicity it can be assumed as
        unity
4  Z_Na = 11;   // Atomic number of sodium
5  Z_F = 9;    // Atomic number of fluorine
6  Z_O = 8;    // Atomic number of oxygen
7  r_Na = Cn/(Z_Na - S); // Radius of sodium ion, m
8  r_F = Cn/(Z_F - S);  // Radius of fluorine ion, m
9  r_ratio = r_Na/r_F;  // Radius ratio
10 r_Na = r_F*r_ratio;  // Calculating radius of
        sodium ion from r_ratio, m
11 // Given that r_Na + r_F = 2.31D-10,
12 // or r_Na + r_Na/0.69 = 2.31D-10,
13 // or r_Na(1 + 1/0.69) = 2.31D-10, solving for r_Na
14 r_Na = 2.31D-10/(1+1/0.69); // Calculating radius
        of sodium, m
15 r_F = 2.31D-10 - r_Na; // Calculating radius of
        fluorine from r_Na, m
16 Cn = r_Na*(Z_Na - S); // Calculating Cn, m
17 r_O = Cn/(Z_O - S);  // Radius of oxygen, m
18 disp(r_Na/1D-10, "Radius of sodium ion, in angstrom,
        is :");
19 disp(r_F/1D-10, "Radius of fluorine ion, in angstrom
        , is :");
20 disp(Cn/1D-10, "Constant determined by quantum
        number is : ");
21 disp(r_O/1D-10, "Radius of oxygen, in angstrom, is :
        ");
22 // Result
23 // Radius of sodium ion, in angstrom, is :
24 // 0.9431361
25 // Radius of fluorine ion, in angstrom, is :
26 // 1.3668639
27 // Constant determined by quantum number, in
        angstrom, is :
28 // 6.1115219
29 // Radius of oxygen, in angstrom, is :

```

30 // 1.7561845

---

#### Scilab code Exa 4.4 Ionic Radius of Si ions in silicon dioxide

```
1 // Scilab Code Ex4.4 Ionic Radius of Si ions in
  silicon dioxide: Page-131 (2010)
2 a = 7.12D-10; // Lattice parameter of the
  crystal. m
3 d = sqrt(3*a^2/16); // Si-Si distance from (0,0,0)
  to (1/4,1/4,1/4)
4 RO = 1.40D-10; // Radius of oxygen, m
5 // Distance of oxygen ions between the two Si ions
  is 2*RSi+2*RO = d, solving for RSi
6 RSi = (d - 2*RO)/2; // Radius of silicon ion, m
7 disp(RSi/1D-10, "The radius of Si4+ ion, in angstrom
  , is : ");
8 //Result
9 // The radius of Si4+ ion, in angstrom, is :
10 // 0.1415252
```

---

#### Scilab code Exa 4.5 Ionic Radius occupying an octahedral position

```
1 // Scilab Code Ex4.5 Ionic Radius occupying an
  octahedral position: Page-138 (2010)
2 R_ratio = 0.414; // Radius ratio for an
  octahedral void in an M+X- ionic lattice
3 R_x = 2.5D-10; // Critical radius of X- anion, m
4 R_m = R_x*0.414; // Radius of M+ cation, m
5 disp(R_m/1D-10, "The radius of cation occupying
  octahedral position in an M+X- ionic solid, in
  angstrom, is : ");
6 //Result
```

```

7 // The radius of cation occupying octahedral
   position in an M+X- ionic solid , in angstrom , is
   :
8 // 1.035

```

---

**Scilab code Exa 4.6 Percentage ionic character of a covalent molecule**

```

1 // Scilab Code Ex4.7 Percentage ionic character of a
   covalent molecule: Page-142 (2010)
2 x_A = 4.0;    // Electronegativity of fluorine
3 x_B = 2.1;    // Electronegativity of hydrogen
4 P = 16*(x_A - x_B) + 3.5*(x_A - x_B)^2; //Percentage
   ionic character of the covalent bond in HF
   molecule
5 printf("\nThe percentage ionic character in HF
   molecule is %5.2f percent", P);
6 //Result
7 // The percentage ionic character in HF molecule is
   43.03 percent

```

---

**Scilab code Exa 4.7 Metallic radius from unit cell dimension**

```

1 // Scilab Code Ex4.8 Calculating metallic radius
   from unit cell dimension: Page-146 (2010)
2 a = 2.81D-10; // Unit cell dimension of bcc
   structure of iron , m
3 // For bcc structure we have
4 //          sqrt(3)*a = 4*R, solving for R
5 R = sqrt(3)/4*a; // Metallic radius of iron atom,
   m
6 printf("\nThe metallic radius of iron atom is %4.2f
   angstrom", R/1D-10);
7 //Result

```

```
8 // The metallic radius of iron atom is 1.22 angstrom
```

---

**Scilab code Exa 4.8** Metallic radii from unit cell dimension

```
1 // Scilab Code Ex4.9 Calculating metallic radii from
  unit cell dimensions: Page-146 (2010)
2 a_Au = 4.08e-10; // Unit cell dimension of fcc
  structure of gold, m
3 a_Pt = 3.91e-10; // Unit cell dimension of fcc
  structure of platinum, m
4 // For fcc structure we have
5 // sqrt(2)*a = 4*R, solving for R
6 R_Au = sqrt(2)/4*a_Au; // Metallic radius of gold
  atom, m
7 R_Pt = sqrt(2)/4*a_Pt; // Metallic radius of gold
  atom, m
8 printf("\nThe metallic radius of gold atom, in
  angstrom, is : %4.2f", R_Au/1D-10);
9 printf("\nThe metallic radius of platinum atom, in
  angstrom, is : %4.2f", R_Pt/1D-10);
10 //Result
11 // The metallic radius of gold atom, in angstrom, is
  : 1.44
12 // The metallic radius of platinum atom, in angstrom
  , is : 1.38
```

---

**Scilab code Exa 4.9** Metallic diameter and unit cell dimension of aluminium

```
1 // Scilab Code Ex4.10 Calculating metallic diameter
  and unit cell dimension of aluminium: Page-146
  (2010)
2 Z_Al = 13; // Atomic number of aluminium
3 A_Al = 26.98; // Atomic mass of aluminium, g
```

```

4 d_Al = 2700D3;    // Density of aluminium , g per
    metre cube
5 n = 4;    // number of atoms in the fcc structure of
    aluminium
6 N = 6.023D+23;    // Avogadro's number
7 // We have number of atoms per fcc unit cell given
    as
8 //  $n = (V*d\_Al*N)/A\_Al$ , solving for V
9 //  $V = (n*A\_Al)/(d\_Al*N)$ , V is the volume of the
    unit cell
10 // or  $a^3 = (n*A\_Al)/(d\_Al*N)$ , solving for a
11 a = ((n*A_Al)/(d_Al*N))^(1/3);    // unit cell
    parameter of aluminium
12 // For an fcc structure we have
13 //  $\sqrt{2}*a = 4*R = 2*D$ , solving for D
14 D = a/sqrt(2);    // metallic diameter of aluminium
    having fcc structure
15 printf("\nThe unit cell dimension of aluminium, is :
    %4.2f angstrom", a/1D-10);
16 printf("\nThe metallic diameter of aluminium, is :
    %4.2f angstrom", D/1D-10);
17 //Result
18 // The unit cell dimension of aluminium, is : 4.05
    angstrom
19 // The metallic diameter of aluminium, is : 2.86
    angstrom

```

---



# Chapter 5

## Crystal Imperfections

Scilab code Exa 5.1 Variation of atomic fraction with temperature

```
1 // Scilab Code Ex5.1 Variation of fraction of atoms
  in a solid with temperature Page-158 (2010)
2 E = 1.5; // Energy of the solid, electron-volt
3 T1 = 300; // First absolute temperature, K
4 T2 = 1500; // Second absolute temperature, K
5 k = 8.614D-5; // Boltzmann constant, electron-
  volt/K
6 // Now fraction of atoms = f_atom = n/N = exp(-E/(k*
  T))
7 f_atom_300 = exp(-E/(k*T1)); // Fraction of atoms
  in the solid at 300 K
8 f_atom_1000 = exp(-E/(k*T2)); // Fraction of
  atoms in the solid at 1000 K
9 printf("\nThe fraction of atoms in the solid at 300
  K, is : %5.3e", f_atom_300);
10 printf("\nThe fraction of atoms in the solid at 1000
  K, is : %5.3e", f_atom_1000);
11 //Result
12 // The fraction of atoms in the solid at 300 K, is :
  6.185e-026
13 // The fraction of atoms in the solid at 1000 K, is
```

: 9.084e-006

---

### Scilab code Exa 5.2 Vacancy formation in copper

```
1 // Scilab Code Ex5.2 Vacancy formation in copper
  Page-159 (2010)
2 E = 1; // Energy of formation of vacancy in
  copper, electron-volt
3 T = 1356; // Melting point of copper, K
4 k = 8.614D-5; // Boltzmann constant, electron-
  volt
5 N = 6.023D23; // Avogadro's number
6 // Now fraction of vacancies = f_vacancy = n/N = exp
  (-E/(k*T))
7 f = exp(-E/(k*T)); // Fraction of vacancies in
  the solid at 300 K
8 n = N*f; // Number of vacancy per mole
9 delta_d = n + N; // Change in the density due to
  creation of vacancy
10 f_d = delta_d/N; // Relative change in the
  density of copper due to vacancy formation
11 printf("\nThe relative change in the density of
  copper due to vacancy formation (n+N)/N, is : %9
  .7f : 1", f_d);
12 //Result
13 // The relative change in the density of copper due
  to vacancy formation (n+N)/N, is : 1.0001914 : 1
```

---

### Scilab code Exa 5.3 Concentration of Schottky imperfections

```
1 // Scilab Code Ex5.3 Concentration of Schottky
  imperfections Page-159 (2010)
2 N = 6.023D23; // Avogadro's number
```

```

3 k = 8.614D-5;    // Boltzmann's constant , eV/K
4 T1 = 27+273;    // First absolute temperature , K
5 T2 = 1000;      // Second absolute temperature , K
6 C_300 = 1D-10;  // Concentration of Schottky
    defects in an fcc crystal at 300 K temperature
7 n = C_300*N;    // Number of Schottky imperfections
    per mole
8 d = 1D-10;      // Interatomic spacing assumed to be
    unit angstrom , m
9 V = d^3;        // Volume of the unit cube , metre cube
10 V_mole = V*N;  // Volume occupied by one mole of
    atoms in fcc crystal , metre cube
11 V_per_defect = V_mole/n;    // Volume per defect ,
    metre cube
12 a = (V_per_defect)^(1/3);    // Average separation
    between the defects , m
13 E_v = 23.03*k*T1;    // Energy of the solid ,
    electron-volt
14 C_1000 = exp(-E_v/(k*T2));    // Schottky defect
    concentration at 1000 K
15 printf("\nThe average separation between the defects
    , is : %3.1e m", a);
16 printf("\nThe expected concentration of Schottky
    defect at 1000 K, n/N, is : %3.1e", C_1000);
17 //Result
18 // The average separation between the defects , is :
    2.2e-007 m
19 // The expected concentration of Schottky defect at
    1000 K, n/N, is : 1.0e-003

```

---

**Scilab code Exa 5.4** Number of Schottky imperfections in NaCl crystal

```

1 // Scilab Code Ex5.4 Number of Schottky
    imperfections in NaCl crystal Page-160 (2010)
2 N = 6.023D23;    // Avogadro's number

```

```

3 k = 8.614D-5;    // Boltzmann's constant , eV/K
4 T = 27+273;    // Absolute room temperature , K
5 Ep = 2;        // Energy required to remove a pair of Na
                // + and Cl- ions , electron-volt
6 // Now Concentration of imperfections in a crystal
                // is given by
7 //  $n/N = \exp(-E_p/(2*k*T))$  , solving for n
8 n = N*exp(-Ep/(2*k*T));    // No. of Schottky
                // imperfections present in NaCl crystal
9 printf("\nNo. of Schottky imperfections present in
                NaCl crystal is : %4.2e", n);
10 V = 26.83;    // Volume of one mole of the crystal ,
                // cm cube
11 n = n/V;    // Number per mole volume of the crystal
                // , per cm cube
12 printf("\nConcentration of Schottky imperfections
                present in NaCl crystal is : %4.2e per cm cube",
                n);
13 //Result
14 // No. of Schottky imperfections present in NaCl
                // crystal is : 9.42e+006
15 // Concentration of Schottky imperfections present
                // in NaCl crystal is : 3.51e+005 per cm cube

```

---

**Scilab code Exa 5.5** Average energy required to create one Schottky defect

```

1 // Scilab Code Ex5.5 Average energy required to
                // create one Schottky defect in NaCl Page-160
                // (2010)
2 N = 6.023D23;    // Avogadro's number
3 k = 8.614D-5;    // Boltzmann's constant , eV/K
4 T = 27+273;    // Absolute room temperature , K
5 r = 2.82D-10;    // Interatomic separation of NaCl
                // crystal , m
6 n = 5D+11;    // Density of defects , per metre

```

```

    cube
7 //Ep = 2;          // Energy required to remove a pair
    of Na+ and Cl- ions , electron-volt
8 a = 2*r;          // Lattice parameter of unit cell of
    NaCl, m
9 V = a^3;          // Volume of the unit cell of sodium
    , metre cube
10 n_ip = 4;        // Number of ion-pairs of NaCl
11 N = n_ip/V;      // No. of ion-pairs in unit volume of
    an ideal NaCl crystal
12 // Now n/N = exp(-Ep/(2*k*T)), solving for Ep
13 Ep = 2*k*T*log(N/n); // Average energy required
    to create one Schottky defect , electron-volt
14 printf("\nThe Average energy required to create one
    Schottky defect in NaCl crystal is : %4.2f eV",
    Ep);
15 //Result
16 // The Average energy required to create one
    Schottky defect in NaCl crystal is : 1.98 eV

```

---

### Scilab code Exa 5.6 Ratio of Frenkel defects at two different temperatures

```

1 // Scilab Code Ex5.6 Ratio of Frenkel defects at two
    different temperatures in an ionic crystal Page
    -161 (2010)
2 k = 8.614D-5;    // Boltzmann's constant , eV/K
3 Ef = 1.4;        // Average energy required to create a
    Frenkel defect , eV
4 T1 = 300;        // First absolute temperature, K
5 T2 = 600;        // Second absolute temperature, K
6 // The concentration of Frenkel defect for given Ef
    and absolute temperature T is given by
7 // n = A*exp(-Ef/(2*k*T)), per metre cube, so that
8 // n1 = A*exp(-Ef/(2*k*T1)), per metre cube, and
9 // n2 = A*exp(-Ef/(2*k*T2)), per metre cube,

```

```

    therefore ,
10 // n1/n2 = exp((-Ef/k)*(1/T1 - 1/T2)), the ratio of
    Frenkel defects is
11 n300_r_n600 = exp((-Ef/(2*k))*(1/T1 - 1/T2)); //
    Frenkel defect ratio
12 printf("\nThe ratio of Frenkel defect , n300_r_n600 ,
    is : %5.3e", n300_r_n600);
13 //Result
14 // The ratio of Frenkel defect , n300_r_n600 , is :
    1.312e-006

```

---

**Scilab code Exa 5.7** Dislocation density of bcc structure of iron

```

1 // Scilab Code Ex5.7 Dislocation density of bcc
    structure of iron Page-163 (2010)
2 L = 0.15; // Length of the strip , m
3 t = 0.02; // Thickness of the iron strip , m
4 r = 0.12; // Radius of curvature of the bent , m
5 a = 2.81D-10; // Lattice parameter of the bcc
    structure of iron , m
6 b = sqrt(3)*a/2; // Magnitude of Burger vector , m
7 // For n positive edge dislocations
8 // n*b = L*t/r, solving for n/(L*t)
9 // n/(L*t) = 1/(r*b), Number of dislocation line
    piercing through a unit area of the plane of the
    paper , per metre square
10 d = 1/(r*b); // Dislocation density in bcc
    structure of iron , number per metre square
11 printf("\nThe dislocation density in bcc structure
    of iron : %4.2e, dislocations per Sq. m", d);
12 //Result
13 // The dislocation density in bcc structure of iron
    : 3.42e+010, dislocations per Sq. m

```

---

**Scilab code Exa 5.8** Minimum dislocation density in aluminium

```
1 // Scilab Code Ex5.8 Minimum dislocation density in
  aluminium Page-164 (2010)
2 b = 3D-10; // Magnitude of Burgers vector , m
3 r = 0.05; // Radius of curvatur of the aluminium
  crystal , m
4 // For n positive edge dislocations
5 // n*b = L*t/r, solving for n/(L*t)
6 // n/(L*t) = 1/(r*b), Number of dislocation line
  piercing through a unit area of the plane of the
  paper , per Sq.m
7 d = 1/(r*b); // Minimum dislocation density in
  aluminium , number per Sq. m
8 printf("\nThe minimum dislocation density in
  aluminium , %4.1e, dislocations per Sq. m", d);
9 //Result
10 // The minimum dislocation density in aluminium , 6.7
  e+010, dislocations per Sq. m
```

---

**Scilab code Exa 5.9** Total force from its resolved component in a given direction

```
1 // Scilab Code Ex5.9 Determining total force from
  its resolved component in a given direction: Page
  -168 (2010)
2 h1 = 1; k1 = -1; l1 = 0 // Miller indices for first
  set of planes
3 h2 = 1; k2 = 0; l2 = 0; // Miller indices for
  second set of planes
4 F_100 = 130; // Resolved component of force along
  [100] direction , N
```

```

5 cos_theta = (h1*h2+k1*k2+l1*l2)/(sqrt(h1^2+k1^2+l1
      ^2)*sqrt(h2^2+k2^2+l2^2)); // Cosine of angle
      between [1 -1 0] and [100] directions
6 // As F/F_100 = cos_theta, solving for F
7 F_110 = F_100/cos_theta; // Applied force along
      [1 -1 0] direction, N
8 printf("\nThe applied force along [1-10] direction =
      %3d N", F_110);
9 // Result
10 // The applied force along [1-10] direction = 183 N

```

---

**Scilab code Exa 5.10** Resolved componet of shearing force in a given direction

```

1 // Scilab Code Ex5.10 Determining resolved componet
      of shearing force in a given direction: Page-168
      (2010)
2 h1 = 1; k1 = 1; l1 = 1 // Miller indices for first
      set of planes
3 h2 = 1; k2 = 1; l2 = 0; // Miller indices for
      second set of planes
4 F_111 = 660; // Shearing force along [111]
      direction, N
5 cos_theta = (h1*h2+k1*k2+l1*l2)/(sqrt(h1^2+k1^2+l1
      ^2)*sqrt(h2^2+k2^2+l2^2)); // Cosine of angle
      between [1 -1 0] and [100] directions
6 // As F_110/F_111 = cos_theta, solving for F_110
7 F_110 = F_111*cos_theta; // Resolved component of
      shearing force along [110] direction, N
8 printf("\nThe resolved component of shearing force
      along [110] direction, F_110 = %3d N", F_110);
9 // Result
10 // The resolved component of shearing force along
      [110] direction, F_110 = 538 N

```

---



Scilab code Exa 5.11 Dependence of applied stress on the slip direction

```
1 // Scilab Code Ex5.11 Dependence of applied stress
   on the slip direction of a copper: Page-169
   (2010)
2 tau_critical = 1; // Critical shear stress for
   the <-110>{111} slip system, mega-pascal (MPa)
3 // For directions [001] and [-111]
4 h1 = 0; k1 = 0; l1 = 1 // Miller indices for
   first set of planes
5 h2 = -1; k2 = 1; l2 = 1; // Miller indices for
   second set of planes
6 cos_phi = (h1*h2+k1*k2+l1*l2)/(sqrt(h1^2+k1^2+l1^2)*
   sqrt(h2^2+k2^2+l2^2)); // Cosine of angle
   between [001] and [-111] directions
7 // For directions [001] and [101]
8 h1 = 0; k1 = 0; l1 = 1 // Miller indices for
   first set of planes
9 h2 = 1; k2 = 0; l2 = 1; // Miller indices for
   second set of planes
10 cos_lambda = (h1*h2+k1*k2+l1*l2)/(sqrt(h1^2+k1^2+l1
   ^2)*sqrt(h2^2+k2^2+l2^2)); // Cosine of angle
   between [001] and [101] directions
11 sigma = tau_critical/(cos_phi*cos_lambda); //
   Stress along [001] direction, newton per metre
   square
12 printf("\nThe stress required to be applied along
   [001] direction to produce slip in the [101]
   direction on the (-111) plane = %4.2f MPa", sigma
   );
13 // For directions [001] and [110]
14 h1 = 0; k1 = 0; l1 = 1 // Miller indices for
   first set of planes
15 h2 = 1; k2 = 1; l2 = 0; // Miller indices for
```

```

    second set of planes
16 cos_lambda = (h1*h2+k1*k2+l1*l2)/(sqrt(h1^2+k1^2+l1
    ^2)*sqrt(h2^2+k2^2+l2^2)); // Cosine of angle
    between [001] and [110] directions
17 if cos_lambda <> 0 then
18     sigma = tau_critical/(cos_phi*cos_lambda); //
    Stress along [001] direction , newton per
    metre square
19     printf("\nThe stress required to be applied
    along [001] direction to produce slip in the
    [110] direction on the (-111) plane = %4.2f
    MPa", sigma);
20 else
21     printf("\nSince cos_lambda = 0, this implies
    that slip cannot occur in [110] direction
    when the stress is applied along [001]
    direction");
22 end
23 // Result
24 // The stress required to be applied along [001]
    direction to produce slip in the [101] direction
    on the (-111) plane = 2.45 MPa
25 // Since cos_lambda = 0, this implies that slip
    cannot occur in [110] direction when the stress
    is applied along [001] direction

```

---

**Scilab code Exa 5.12** Resolved stress in a direction from applied stress in other d

```

1 // Scilab Code Ex5.12 Resolved stress in a direction
    from applied stress in some other direction of
    bcc iron: Page-169 (2010)
2 sigma = 123; // Axial stress applied in the
    direction [110] of bcc iron , MPa
3 // For directions [010] and [110]
4 h1 = 0; k1 = 1; l1 = 0 // Miller indices for

```

```

    first set of planes
5 h2 = 1; k2 = 1; l2 = 0;    // Miller indices for
    second set of planes
6 cos_phi = (h1*h2+k1*k2+l1*l2)/(sqrt(h1^2+k1^2+l1^2)*
    sqrt(h2^2+k2^2+l2^2));    // Cosine of angle
    between [010] and [110] directions
7 // For directions [110s] and [101]
8 h1 = 1; k1 = 0; l1 = 1    // Miller indices for
    first set of planes
9 h2 = 1; k2 = 1; l2 = 0;    // Miller indices for
    second set of planes
10 cos_lambda = (h1*h2+k1*k2+l1*l2)/(sqrt(h1^2+k1^2+l1
    ^2)*sqrt(h2^2+k2^2+l2^2));    // Cosine of angle
    between [110] and [101] directions
11 tau = sigma*cos_phi*cos_lambda;    // Resolved shear
    stress in the [101] direction on the (010) plane
    , MPa
12 printf("\nThe resolved shear stress in the [101]
    direction on the (010) plane = %4.1f MPa", tau);
13 // Result
14 // The resolved shear stress in the [101] direction
    on the (010) plane = 43.5 MPa

```

---

**Scilab code Exa 5.13** Critical resolved shear stress from applied stress in a given

```

1 // Scilab Code Ex5.13 Determining critical resolved
    shear stress from applied stress in a given
    direction of aluminium: Page-170 (2010)
2 sigma_critical = 3.5;    // Applied stress in the [1
    -1 1] direction , MPa
3 // For directions [111] and [1 -1 1]
4 h1 = 1; k1 = 1; l1 = 1;    // Miller indices for
    first set of planes
5 h2 = 1; k2 = -1; l2 = 1;    // Miller indices for
    second set of planes

```

```

6 cos_phi = (h1*h2+k1*k2+l1*l2)/(sqrt(h1^2+k1^2+l1^2)*
    sqrt(h2^2+k2^2+l2^2)); // Cosine of angle
    between [111] and [1 -1 1] directions
7 // For directions [1 -1 0] and [1 -1 1]
8 h1 = 1; k1 = -1; l1 = 0 // Miller indices for
    first set of planes
9 h2 = 1; k2 = -1; l2 = 1; // Miller indices for
    second set of planes
10 cos_lambda = (h1*h2+k1*k2+l1*l2)/(sqrt(h1^2+k1^2+l1
    ^2)*sqrt(h2^2+k2^2+l2^2)); // Cosine of angle
    between [1 -1 0] and [1 -1 1] directions
11 tau_c = sigma_critical*cos_phi*cos_lambda; // The
    critical resolved shear stress in the [1 -1 0]
    direction on the (111) plane, MPa
12 printf("\nThe critical resolved shear stress in the
    [1 -1 0] direction on the (111) plane = %4.2f MPa
    ", tau_c);
13 // Result
14 // The critical resolved shear stress in the [1 -1
    0] direction on the (111) plane = 0.95 MPa

```

---

#### Scilab code Exa 5.14 Initiation of slip by the applied stress

```

1 // Scilab Code Ex5.14 Determining the direction in
    which slip is initiated by the applied stress in
    zinc: Page-170 (2010)
2 sigma = 2.3; // Applied stress when the plastic
    deformation is first observed, MPa
3 phi = 60; // Angle which the normal to the basal
    plane makes with the tensile axis of zinc, degree
4 // Function to find the value of resolved shear
    stress
5 function[tau] = stress(lambda)
6     tau = sigma*cosd(phi)*cosd(lambda);
7 endfunction

```

```

8 lambda = [38 45 84]; // Angles which the three
    slip directions x1, x2 and x3 respectively makes
    with the tensile axis, degrees
9 t = zeros(1,3); // Initialize a one-
    dimensional vector of three elements
10 for i = 1:1:3
11     t(i) = stress(lambda(i)); // Calculate the
        value of resolved shear stress by calling
        stress function
12     printf("\ntau%d = %5.3f MPa", i, t(1,i)); //
        Display resolved shear stress for each
        direction , MPa
13 end
14 // Locate for the largest resolved stress value
15 big = t(1,1);
16 for i = 2:1:3
17     if t(1,i) > big then
18         big = t(1,i) // Set largest value of
            resolved stress if the condition meets
19     end
20 end
21 printf("\nThe slip is initiated along direction x1
    at tau_c = %5.3f MPa", big);
22 // Result
23 // tau1 = 0.906 MPa
24 // tau2 = 0.813 MPa
25 // tau3 = 0.120 MPa
26 // The slip is initiated along direction x1 at tau_c
    = 0.906 MPa

```

---

**Scilab code Exa 5.15** Applied tensile stress in a direction to initiate plastic def

```

1 // Scilab Code Ex5.15 Determining applied tensile
    stress in a direction to initiate plastic
    deformation: Page-170 (2010)

```

```

2 tau_critical = 0.7; // Critical resolved shear
   stress for fcc crystal, MPa
3 // For directions [100] and [1 1 1]
4 h1 = 1; k1 = 0; l1 = 0; // Miller indices for
   first set of planes
5 h2 = 1; k2 = 1; l2 = 1; // Miller indices for
   second set of planes
6 cos_phi = (h1*h2+k1*k2+l1*l2)/(sqrt(h1^2+k1^2+l1^2)*
   sqrt(h2^2+k2^2+l2^2)); // Cosine of angle
   between [100] and [1 1 1] directions
7 // For directions [1 0 0] and [1 -1 0]
8 h1 = 1; k1 = 0; l1 = 0 // Miller indices for
   first set of planes
9 h2 = 1; k2 = -1; l2 = 0; // Miller indices for
   second set of planes
10 cos_lambda = (h1*h2+k1*k2+l1*l2)/(sqrt(h1^2+k1^2+l1
   ^2)*sqrt(h2^2+k2^2+l2^2)); // Cosine of angle
   between [1 0 0] and [1 -1 0] directions
11 sigma_c = tau_critical/(cos_phi*cos_lambda); //
   The critical resolved shear stress in the [1 -1
   0] direction on the (1 1 1) plane, MPa
12 printf("\nThe critical resolved shear stress in the
   [1 -1 0] direction on the (1 1 1) plane = %3.1f
   MPa", sigma_c);
13 // Result
14 // The critical resolved shear stress in the [1 -1
   0] direction on the (1 1 1) plane = 1.7 MPa

```

---

#### Scilab code Exa 5.16 Dislocation width in copper

```

1 // Scilab Code Ex5.16 Dislocation width in copper:
   Page-175 (2010)
2 mu = 1; // For simplicity, assume shear modulus
   of copper to be unity, netwon per metre square
3 tau_PN = mu/1e+05; // Shear stress to initiate

```

```

        plastic deformation, newton per metre square
4  a = 3.61e-010;    // Lattice parameter of copper, m
5  b = a/sqrt(2);   // Burger vector magnitude for fcc
        crystal of copper, m
6  // As stress necessary to move a dislocation in a
        crystal is given by
7  // tau_PN = mu*exp(-2*pi*w/b), solving for w
8  w = b*log(mu/tau_PN)/(2*pi);    // Width of the
        dislocation in copper, m
9  printf("\nThe width of dislocation in copper = %4.2e
        angstrom", w/1d-10);
10 // Result
11 // The width of dislocation in copper = 4.68e-010
        angstrom

```

---

**Scilab code Exa 5.17** Change in number of vacancies due to dislocation motion

```

1 // Scilab Code Ex5.17 Change in number of vacancies
        due to dislocation motion: Page-176 (2010)
2 l = 1e-03;    // Edge dislocation length of simple
        cubic crystal, m
3 d = 1e-06;    // Distance of dislocation climb in, m
4 a = 3e-10;    // Lattice parameter of scc, m
5 A = a^2;    // Area of the unit cell, metre square
6 A_affected = l*d;    // Affected area when the
        dislocation climbs down, metre square
7 // N.B.: Area of one unit cell in scc contributes
        one atom
8 N = A_affected/A;    // Number of vacancies created
        within the affected area
9 printf("\nThe number of vacancies lost or created =
        %3.1e", N);
10 // Result
11 // The number of vacancies lost or created = 1.1e
        +010

```

---

**Scilab code Exa 5.18** Minimum number of dislocations in motion from shearing rate

```
1 // Scilab Code Ex5.18 Minimum number of dislocations
  in motion from shearing rate of copper: Page-176
  (2010)
2 a = 3.61e-010; // Lattice parameter of copper, m
3 epsilon_dot = 10/60; // Strain rate of plastic
  deformation, mm per sec
4 v_d = 1e+06; // Velocity of dislocation, mm per
  sec
5 V = 1e+03; // Volume of the crystal, mm cube
6 b = a*1e+03/sqrt(2); // Burger vector magnitude
  for fcc crystal of copper, mm
7 // Strain rate of plastic deformation is given by
8 // epsilon_dot = rho*b*v_d, solving for rho
9 rho = epsilon_dot/(b*v_d); // Density of the
  mobile dislocations, per mm cube
10 N = round(rho*V); // Number of dislocations in
  motion in the whole cube
11 printf("\nThe number of dislocations in motion in
  the whole cube = %3d", N);
12 // Result
13 // The number of dislocations in motion in the whole
  cube = 653
```

---

**Scilab code Exa 5.19** Elastic energy of line imperfection

```
1 // Scilab Code Ex5.19 Elastic energy of line
  imperfection stored in Al: Page-178 (2010)
2 rho = 1e+010; // Dislocation density of Al, per
  metre square
```



```

3 mu = 25.94e+09;    // Shear modulus of aluminium ,
    newton per metre square
4 a = 4.05e-010;    // Lattice parameter of aluminium ,
    m
5 b = a/sqrt(2);    // Burger vector magnitude for fcc
    crystal of Al, m
6 E_bar = mu*b^2/2;    // Elastic energy per unit
    length of the dislocation , joule per metre
7 E = E_bar*rho;    // Elastic energy stored in the
    crystal, joule per metre cube
8 printf("\nThe elastic energy stored in the crystal =
    %5.2f joule per metre cube", E);
9 // Result
10 // The elastic energy stored in the crystal = 10.64
    joule per metre cube

```

---

**Scilab code Exa 5.20** Spacing between dislocations in a tilt boundary

```

1 // Scilab Code Ex5.20 Spacing between dislocations
    in a tilt boundary in fcc Ni: Page-187 (2010)
2 theta = 2;    // Angle of tilt , degree
3 a = 3.52e-010;    // Lattice parameter of Al, m
4 b = a/sqrt(2);    // Burger vector magnitude for fcc
    Ni, m
5 h = b/tand(theta);    // The vertical spacing
    between two neighbouring edge dislocations , m
6 printf("\nThe spacing between dislocations in a tilt
    boundary in fcc Ni = %4.1f angstrom", h/1D-10);
7 // Result
8 // The spacing between dislocations in a tilt
    boundary in fcc Ni = 71.3 angstrom

```

---

**Scilab code Exa 5.21** Tilt angle from dislocation spacing in the boundary

```

1 // Scilab Code Ex5.21 Determining tilt angle from
  dislocation spacing in the boundary of Cu: Page
  -188 (2010)
2 a = 3.61e-010; // Lattice parameter of Cu, m
3 b = a/sqrt(2); // Burger vector magnitude for fcc
  Cu, m
4 h = 1.5e-06; // The vertical spacing between two
  neighbouring edge dislocations, m
5 theta = atand(b/h)*(%pi/180); // tangent of tilt
  angle between two tilt boundaries of Cu, radian
6 printf("\nThe tilt angle between two tilt boundaries
  of Cu = %3.1e radian", theta);
7 // Result
8 // The tilt angle between two tilt boundaries of Cu
  = 1.7e-004 radian

```

---

**Scilab code Exa 5.22 Tilt angle from dislocation spacing**

```

1 // Scilab Code Ex5.22 Determining tilt angle from
  dislocation spacing in the boundary of Cu: Page
  -188 (2010)
2 b = 0.4e-09; // Burger vector magnitude for fcc
  Cu, m
3 h = 3.0e-06; // The vertical spacing between two
  neighbouring edge dislocations, m
4 theta = atand(b/h)*(%pi/180); // tangent of tilt
  angle between two tilt boundaries of Cu, radian
5 printf("\nThe tilt angle between two tilt boundaries
  of Cu = %4.2e radian", theta);
6 // Result
7 // The tilt angle between two tilt boundaries of Cu
  = 1.33e-004 radian

```

---

# Chapter 6

## Atomic Diffusion

Scilab code Exa 6.1 Rate of diffusion of nitrogen through steel wall

```
1 // Scilab Code Ex6.1 Rate of diffusion of nitrogen
  through steel wall: Page-195 (2010)
2 D = 1e-019; // Diffusion coefficient of nitrogen
  in steel at room temperature, metre square per
  sec
3 dc = 10; // Concentration of nitrogen at the
  inner surface of the tank, kg per metre cube
4 dx = 10e-03; // Thickness of the steel wall, m
5 J = D*(dc/dx); // Fick's first law giving outward
  flux of nitrogen through steel wall of the tank,
  kg per metre square per second
6 printf("\nThe rate at which nitrogen escapes through
  the tank wall = %1.0e kg per metre square per
  sec", J);
7 // Result
8 // The rate at which nitrogen escapes through the
  tank wall = 1e-016 kg per metre square per sec
```

---

Scilab code Exa 6.2 Rate of diffusion of copper through pure Al sheet

```

1 // Scilab Code Ex6.2 Rate of diffusion of copper
  through pure Al sheet: Page-196 (2010)
2 a = 4.05e-010; // Lattice parameter of fcc Al, m
3 N = 4; // Number of Al atoms per unit cell of fcc
  Al
4 n = N/a^3; // Number of Al atoms per unit volume,
  per metre cube
5 D = 5.25e-013; // Diffusion coefficient of copper
  in Al at 550 degree celsius, metre square per sec
6 c1 = 0.19e-02; // Atomic percent of copper at the
  surface, per unit volume
7 c2 = 0.18e-02; // Atomic percent of copper at the
  the depth 1.2 mm from the surface, per unit
  volume
8 dc = (c2 - c1)*n; // Change in concentration of
  copper at 1.2 mm depth of the surface, per metre
  cube
9 dx = 1.2e-03; // Thickness of the pure Al sheet,
  m
10 J = -D*(dc/dx); // Fick's first law giving
  outward flux of copper through the Al sheet, Cu
  atoms per metre square per second
11 printf("\nThe outward flux of copper through the Al
  sheet = %4.2e Cu atoms per metre square per sec",
  J);
12 // Result
13 // The outward flux of copper through the Al sheet =
  2.63e+015 Cu atoms per metre square per sec

```

---

**Scilab code Exa 6.3 Rate of diffusion of carbon through steel bar**

```

1 // Scilab Code Ex6.3 Rate of diffusion of carbon
  through steel bar: Page-196 (2010)
2 a = 3.65e-010; // Lattice parameter of fcc
  structure of iron, m

```

```

3 D = 3e-011;    // Diffusion coefficient of carbon in
  iron at 1000 degree celsius , metre square per sec
4 n1 = 20;      // Number of unit cells per carbon atom
  at the surface of steel
5 n2 = 30;      // Number of unit cells per carbon atom
  at a depth 1 mm from the surface of steel
6 c1 = 1/(n1*a^3);    // Atomic percent of carbon at
  the surface , per metre cube
7 c2 = 1/(n2*a^3);    // Atomic percent of carbon at a
  depth 1 mm from the surface , per metre cube
8 dx = 1e-03;    // Thickness of the steel bar , m
9 J = -D*((c2-c1)/dx);    // Fick's first law giving
  outward flux of carbon through the Steel bar , C
  atoms per metre square per second
10 J_uc = J*a^2*60;    // The number of carbon atoms
  diffusing through each unit cell per minute
11 printf("\nThe number of carbon atoms diffusing
  through each unit cell per minute = %2d atoms per
  minute", J_uc);
12 // Result
13 // The number of carbon atoms diffusing through each
  unit cell per minute = 82 atoms per minute

```

---

#### Scilab code Exa 6.4 Diffusion through a cylinder

```

1 // Scilab Code Ex6.4 Diffusion through a cylinder:
  Page-199 (2010)
2 r = 12;    // Radius of cylindrical crystal , mm
3 A1 = %pi*r^2;    // Cross-sectional area for
  diffusion through the cylinder , milli-metre
  square
4 t = 4e-07;    // Assume effective thickness of the
  surface to be 4 angstrom = two atomic diameters ,
  mm
5 A2 = 2*%pi*r*t;    // Cross-sectional area for

```

```

    diffusion along the surface , milli-metre square
6 ratio = A2/A1;    // Ratio of two cross-sectional
    areas
7 printf("\nThe ratio of two cross-sectional areas =
    %4.2e", ratio);
8 // Result
9 // The ratio of two cross-sectional areas = 6.67e
    -008

```

---

#### Scilab code Exa 6.5 Diffusion length of Li in Ge

```

1 // Scilab Code Ex6.5 Diffusion length of Li in Ge:
    Page-203 (2010)
2 D = 1e-010;    // Diffusion coefficient for Li in Ge
    , metre square per sec
3 t = 1*60*60;    // Time taken by diffusing Li to
    travel diffusion depth, sec
4 T = 500+273;    // absolute temperature of the
    system, kelvin
5 x = sqrt(D*t);    // Diffusion length of Li in Ge, m
6 printf("\nThe diffusion length of Li in Ge = %1.0e m
    ", x);
7 // Result
8 // The diffusion length of Li in Ge = 6e-004 m

```

---

#### Scilab code Exa 6.6 Diffusion time of Li in Ge

```

1 // Scilab Code Ex6.6 Diffusion time of Li in Ge:
    Page-203 (2010)
2 D = 1e-010;    // Diffusion coefficient for Li in Ge
    , metre square per sec
3 T = 500+273;    // Absolute temperature of the
    system, kelvin

```

```

4 x = 0.2e-03;    // Diffusion length of Li in Ge, m
5 // Diffusion length is given by
6 // x = sqrt(D*t), solving for t
7 t = x^2/D;    // Time taken by diffusing Li to
   travel diffusion depth of 0.2 mm, sec
8 printf("\nThe time taken by diffusing Li to travel
   diffusion depth of 0.2 mm = %3d s", t);
9 // Result
10 // The time taken by diffusing Li to travel
   diffusion depth of 0.2 mm = 400 s

```

---

#### Scilab code Exa 6.7 Diffusion coefficient of Cu in Al

```

1 // Scilab Code Ex6.7 Diffusion coefficient of Cu in
   Al: Page 206 (2010)
2 D0 = 0.25e-04;    // Pre-exponential diffusion
   constant independent of temperature, metre square
   per second
3 T = 550+273;    // Absolute temperature of the
   system, kelvin
4 R = 8.314;    // Molar gas constant, J/mol/K
5 Q = 121e+03;    // The activation energy for
   diffusion, joule per mole
6 t = 1*60*60;    // Time taken by Cu to diffuse into
   Al, sec
7 D = D0*exp(-Q/(R*T));    // Diffusion coefficient of
   Cu in Al at 550 degree celsius, metre square per
   sec
8 x = sqrt(D*t);    // Diffusion length of Cu in Al, m
9 printf("\nThe diffusion coefficient of Cu in Al at
   550 degree celsius = %4.2e metre square per sec",
   D);
10 printf("\nThe diffusion length of Cu in Al = %5.3f
   mm", x*1000);
11 // Result

```

```
12 // The diffusion coefficient of Cu in Al at 550
    degree celsius = 5.22e-013 metre square per sec
13 // The diffusion length of Cu in Al = 0.043 mm
```

---

**Scilab code Exa 6.8** Activation energy for diffusion of Ag in Si

```
1 // Scilab Code Ex6.8 Activation energy for diffusion
    of silver in silicon: Page 206 (2010)
2 R = 8.314; // Molar gas constant, J/mol/K
3 T1 = 1350+273; // First temperature at which
    difusion of Ag into Si takes place, kelvin
4 T2 = 1100+273; // Second temperature at which
    difusion of Ag into Si takes place, kelvin
5 DRR = 8; // Ratio of diffusion rates of Ag in Si
    at T1 and T2
6 // As diffusion coefficient at temperature T1 is D1
    = D0*exp(-Q/(R*T1))
7 // and that at temperature T2 is D1 = D0*exp(-Q/(R*
    T2)), so that the diffusion rates ratio
8 // D1/D2 = DRR = exp(Q/R*(1/T2-1/T1)), solving for Q
    , we have
9 Q = R*log(DRR)/((1/T2-1/T1)*1000); // Activation
    energy for diffusion of Ag in Si, kJ/mol
10 printf("\nThe activation energy for diffusion of Ag
    in Si = %3d kJ/mol", Q);
11 // Result
12 // The activation energy for diffusion of Ag in Si =
    154 kJ/mol
```

---

**Scilab code Exa 6.9** Arrhenius rate law



```

1 // Scilab Code Ex6.9 Activation energy and diffusion
  constant of a diffusion system obeying Arrhenius
  rate law: Page 207 (2010)
2 R = 1.987; // Molar gas constant, cal/mol/K
3 D_1100 = 8e-013; // Diffusivity of Ga in Si at
  1100 degree celsius, cm square per sec
4 D_1300 = 1e-010; // Diffusivity of Ga in Si at
  1300 degree celsius, cm square per sec
5 T1 = 1100+273; // First temperature at which
  diffusion of Ga into Si takes place, kelvin
6 T2 = 1300+273; // Second temperature at which
  diffusion of Ga into Si takes place, kelvin
7 // Arrhenius equation in log10 form is given by
8 //  $\log_{10}(D) = \log_{10}(D_0) - Q/(2.303 \cdot R \cdot T)$  — (a)
9 // Thus  $\log_{10}(D_{1100}) = \log_{10}(D_0) - Q/(2.303 \cdot R \cdot T_1)$ 
  — (i)
10 //  $\log_{10}(D_{1300}) = \log_{10}(D_0) - Q/(2.303 \cdot R \cdot T_2)$  — (
  ii),
11 // On subtracting (ii) from (i), we get
12 //  $\log_{10}(D_{1100}/D_{1300}) = -Q/(2.303 \cdot R) \cdot (1/T_2 - 1/T_1)$ ,
  solving for Q
13 Q = (2.303*log10(D_1100/D_1300)*R)/(1/T2-1/T1);
  // Activation energy for diffusion of Ga in Si,
  cal/mol
14 // Putting Q in (ii) and solving for D0
15 D0 = exp(2.303*log10(D_1100)+Q/(R*T1))
16 //  $D_0 = \exp(2.303 \cdot \log_{10}(D_{1300}) + Q/(R \cdot T_2))$ ; // Pre
  -exponential diffusion constant independent of
  temperature, cm square per sec
17 T = 1200+273; // Temperature at which diffusion
  of Ga into Si is to be calculated, kelvin
18 // Substituting D0, Q, R and T in (a) and solving
  for D, we have
19 D = exp(2.303*log10(D0)-Q/(R*T)); // Diffusivity
  of the system, cm square per sec
20 printf("\nThe activation energy for diffusion of Ga
  in Si = %3d kcal/mol", Q/1000);
21 printf("\nThe pre-exponential diffusion constant, D0

```

```

    = %5d cm square per sec", D0);
22 printf("\nThe diffusivity of the system = %4.2e cm
    square per sec", D);
23 // Result
24 // The activation energy for diffusion of Ga in Si =
    103 kcal/mol
25 // The pre-exponential diffusion constant, D0 =
    24893 cm square per sec
26 // The diffusivity of the system = 1.05e-011 cm
    square per sec

```

---

**Scilab code Exa 6.10** Activation energy for diffusion rates at different temperatures

```

1 // Scilab Code Ex6.10 Activation energy for
    diffusion rates at different temperatures: Page
    208 (2010)
2 R = 8.314; // Molar gas constant, J/mol/K
3 T1 = 500+273; // First temperature at which
    diffusion of A into B takes place, kelvin
4 T2 = 850+273; // Second temperature at which
    diffusion of A into B takes place, kelvi
5 PDR = 1/4; // Penetration depth ratio at 500
    degree celsius and 850 degree celsius
6 //  $x_1/x_2 = \sqrt{D_1/D_2}$  i.e.  $PDR = \sqrt{DRR}$ , DRR is
    the diffusion rate ratio
7 // solving for DRR
8 DRR = PDR^2; // Diffusion rate ratio  $D_1/D_2$  of A
    in B
9 // As diffusion coefficient at temperature T1 is  $D_1 = D_0 \cdot \exp(-Q/(R \cdot T_1))$ 
10 // and that at temperature T2 is  $D_1 = D_0 \cdot \exp(-Q/(R \cdot T_2))$ , so that the diffusion rates ratio
11 //  $D_1/D_2 = DRR = \exp(Q/R \cdot (1/T_2 - 1/T_1))$ , solving for Q
    , we have
12 Q = R*log(DRR)/((1/T2-1/T1)*1000); // Activation

```

```

    energy for diffusion of A in B, kJ/mol
13 printf("\nThe activation energy for diffusion of A
    in B = %5.2f kJ/mol", Q);
14 // Result
15 // The activation energy for diffusion of A in B =
    57.17 kJ/mol

```

---

#### Scilab code Exa 6.11 Time required for carburizing of steel

```

1 // Scilab Code Ex6.11 Time required for carburizing
  of steel: Page 209 (2010)
2 C0 = 0.0018; // Intial carbon concentration of
  steel
3 Cx = 0.0030; // Carbon concentration of steel at
  0.60 mm below the surface of the gear
4 Cs = 0.01; // Carbon concentration of steel at
  the surface
5 x = 0.6e-03; // Diffusion depth below the surface
  of the gear, m
6 D_927 = 1.28e-011; // Diffusion coefficient for
  carbon in iron, metre square per sec
7 erf_Z = (Cs-Cx)/(Cs-C0); // Error function of Z
  as a solution to Fick's second law
8 Z1 = 1.0, Z2 = 1.1; // Preceding and succeeding
  values about Z from error function table
9 erf_Z1 = 0.8427, erf_Z2 = 0.8802; // Preceding
  and succeeding values about erf_Z from error
  function table
10 Z = poly(0, 'Z');
11 Z = roots((Z-Z1)/(Z2-Z1)-(erf_Z-erf_Z1)/(erf_Z2-
  erf_Z1));
12 // As  $Z = x/(2*\sqrt{D_{927}*t})$ , where Z is a constant
  argument of error function as erf(Z)
13 // Solving for t, we have
14 t = (x/(2*Z))^2/D_927; // Time necessary to

```

```

    increase the carbon content of steel , sec
15 printf("\nThe time necessary to increase the carbon
    content of steel = %3d minutes", t/60);
16 // Result
17 // The time necessary to increase the carbon content
    of steel = 110 minutes

```

---

**Scilab code Exa 6.12** Carbon concentration of carburized steel at certain depth

```

1 // Scilab Code Ex6.12 Carbon concentration of
    carburized steel at certain depth: Page 210
    (2010)
2 C0 = 0.0020; // Initial carbon concentration of
    steel
3 Cs = 0.012; // Carbon concentration of steel at
    the surface
4 t = 10*60*60; // Carburizing time of steel , sec
5 x = 0.06*25.4*1e-03; // Diffusion depth below the
    surface of the gear , mm
6 D_927 = 1.28e-011; // Diffusion coefficient for
    carbon in iron , metre square per sec
7 Z = x/(2*sqrt(D_927*t)), // A constant argument of
    error function as erf(Z)
8 Z1 = 1.1, Z2 = 1.2; // Preceding and succeeding
    values about Z from error function table
9 erf_Z1 = 0.8802, erf_Z2 = 0.9103; // Preceding
    and succeeding values about erf_Z from error
    function table
10 efZ = poly(0, 'efZ');
11 efZ = roots((efZ-erf_Z1)/(erf_Z2-erf_Z1)-(Z-Z1)/(Z2-
    Z1)); // Error function of Z as a solution to
    Fick's second law
12 Cx = poly(0, 'Cx');
13 Cx = roots(efZ-(Cs-Cx)/(Cs-C0)); // Carbon
    concentration of carburized steel at 0.06 inch

```

```

    depth
14 printf("\nThe carbon concentration of carburized
    steel at 0.06 inch depth = %4.2f percent", Cx
    *100);
15 // Result
16 // The carbon concentration of carburized steel at
    0.06 inch depth = 0.31 percent

```

---

**Scilab code Exa 6.13** Depth of decarburization below the surface of steel

```

1 // Scilab Code Ex6.13 Depth of decarburization below
    the surface of steel: Page 211 (2010)
2 C2 = 0.012; // Initial carbon concentration of
    steel
3 Cx = 0.008; // Carbon concentration of carburized
    steel at x metre depth
4 Cs = 0; // Carbon concentration of steel at the
    surface
5 t = 5*60*60; // Carburizing time of steel, sec
6 D_927 = 1.28e-011; // Diffusion coefficient for
    carbon in iron, metre square per sec
7 erf_Z = abs((Cs-Cx)/(C2-Cs)); // Error function
    of Z as a solution to Fick's second law
8 Z1 = 0.65, Z2 = 0.70; // Preceding and succeeding
    values about Z from error function table
9 erf_Z1 = 0.6420, erf_Z2 = 0.6778; // Preceding
    and succeeding values about erf_Z from error
    function table
10 Z = poly(0, 'Z');
11 Z = roots((Z-Z1)/(Z2-Z1)-(erf_Z-erf_Z1)/(erf_Z2-
    erf_Z1));
12 // As  $Z = x/(2*\sqrt{D_927*t})$ , where Z is a constant
    argument of error function as erf(Z)
13 // Solving for x, we have
14 x = Z*2*sqrt(D_927*t); // Depth of decarburization

```

```

    below the surface of steel , m
15 printf("\nThe minimum depth upto which post
    machining is to be done = %4.2f mm", x*1000);
16 // Result
17 // The minimum depth upto which post machining is to
    be done = 0.66 mm

```

---

#### Scilab code Exa 6.14 Diffusion depth of P type semiconductor

```

1 // Scilab Code Ex6.14 Diffusion depth of P-type
    semiconductor (B into Si): Page 212 (2010)
2 C0 = 0; // Initial boron concentration of silicon
3 Cx = 1e+17; // Boron concentration at depth x
    below the silicon surface
4 Cs = 1e+18; // Boron concentration of silicon at
    the surface
5 T = 1100+273; // Absolute temperature of the
    system, kelvin
6 t = 2*60*60; // Time taken to diffuse boron into
    silicon, sec
7 D_1100 = 4e-013; // Diffusion coefficient for
    boron in silicon, cm square per sec
8 erf_Z = abs((Cs-Cx)/(Cs-C0)); // Error function
    of Z as a solution to Fick's second law
9 Z1 = 1.1, Z2 = 1.2; // Preceding and succeeding
    values about Z from error function table
10 erf_Z1 = 0.8802, erf_Z2 = 0.9103; // Preceding
    and succeeding values about erf_Z from error
    function table
11 Z = poly(0, 'Z');
12 Z = roots((Z-Z1)/(Z2-Z1)-(erf_Z-erf_Z1)/(erf_Z2-
    erf_Z1));
13 // As  $Z = x/(2*\sqrt{D_{927}*t})$ , where Z is a constant
    argument of error function as erf(Z)
14 // Solving for x, we have

```

```
15 x = Z*2*sqrt(D_1100*t); // Diffusion depth of boron
    into silicon
16 printf("\nThe diffusion depth of boron into silicon
    = %4.2e cm", x);
17 // Result
18 // The diffusion depth of boron into silicon = 1.25e
    -004 cm
```

---

# Chapter 7

## Lattice or Atomic Vibrations

Scilab code Exa 7.1 Cut off frequency of the linear lattice of a solid

```
1 // Scilab Code Ex7.1 Cut-off frequency of the linear
   lattice of a solid: Page-238 (2010)
2 v = 3e+03; // Velocity of sound in the solid, m/s
3 a = 3e-010; // Interatomic distance, m
4 // As cut-off frequency occurs at  $k = \pi/a$  and  $k = 2\pi/\lambda$ , this gives
5 lambda = 2*a; // Cut-off wavelength for the solid
   , m
6 f = v/lambda; // Cut-off frequency ( $v = f*\lambda$ )
   for the linear lattice, hertz
7 printf("\nThe cut-off frequency for the linear
   lattice of a solid = %1.0e Hz", f);
8 // Result
9 // The cut-off frequency for the linear lattice of a
   solid = 5e+012 Hz
```

---

Scilab code Exa 7.2 Comparison of frequency of waves in a monoatomic and diatomic



```

1 // Scilab Code Ex7.2 Comparison of frequency of
   waves in a monoatomic and diatomic linear systems
   : Page-238 (2010)
2 a = 2.5e-010; // Interatomic spacing between two
   identical atoms, m
3 v0 = 1e+03; // Velocity of sound in the solid, m/
   s
4 lambda = 10e-010; // Wavelength of the sound wave
   , m
5 omega = v0*2*%pi/lambda; // Angular frequency of
   sound wave in a monoatomic lattice, rad per sec
6 printf("\nThe frequency of sound waves in a
   monoatomic lattice = %4.2e rad/sec", omega);
7 // For acoustic waves in a diatomic lattice (M = m),
   the angular frequency, omega = 0 at k = 0 and
8 // omega = (2*K/m)^(1/2) --- (i) at k = %pi
   /(2*a)
9 // As v0 = a*(2*K/m)^(1/2) --- (ii)
10 // From (i) and (ii), we have
11 omega_min = 0; // Angular frequency of acoustic
   waves at k = 0, rad per sec
12 omega_max = v0/a; // Angular frequency of
   acoustic waves at k = %pi/(2*a), rad per sec
13 printf("\n\nThe frequency of acoustic waves wave in
   a diatomic lattice :\n %d rad/sec for k = 0 \n %1
   .0e rad/sec for k = pi/(2*a)", omega_min,
   omega_max);
14 // For optical waves in a diatomic lattice (M = m),
   the angular frequency
15 // omega = sqrt(2)*(2*K/m)^(1/2) --- (iii) at
   k = 0
16 // As v0 = a*(2*K/m)^(1/2) --- (iv)
17 // From (iii) and (iv), we have
18 omega_max = sqrt(2)*v0/a; // Angular frequency of
   optical waves at k = 0, rad per sec
19 // For optical waves in a diatomic lattice (M = m),
   the angular frequency
20 // omega = (2*K/m)^(1/2) --- (iii) at k = %pi

```

```

    /(2*a)
21 // As  $v_0 = a \cdot (2K/m)^{1/2}$  ---- (iv)
22 // From (iii) and (iv), we have
23 omega_min = v0/a; // Angular frequency of optical
    waves at  $k = \pi/(2a)$ , rad per sec
24 printf("\n\nThe frequency of optical swaves wave in
    a diatomic lattice :\n %4.2e rad/sec for  $k = 0$  \n
    %1.0e rad/sec for  $k = \pi/(2a)$ ", omega_max,
    omega_min);
25 // Result
26 // The frequency of sound waves in a monoatomic
    lattice = 6.28e+012 rad/sec
27
28 // The frequency of acoustic waves wave in a
    diatomic lattice :
29 // 0 rad/sec for  $k = 0$ 
30 // 4e+012 rad/sec for  $k = \pi/(2a)$ 
31
32 // The frequency of optical swaves wave in a
    diatomic lattice :
33 // 5.66e+012 rad/sec for  $k = 0$ 
34 // 4e+012 rad/sec for  $k = \pi/(2a)$ 

```

---

### Scilab code Exa 7.3 Reflection of electromagnetic radiation from a crystal

```

1 // Scilab Code Ex7.3 Reflection of electromagnetic
    radiation from a crystal: Page-239(2010)
2 c = 3.0e+08; // Speed of electromagnetic wave in
    vacuum, m/s
3 a = 5.6e-010; // Lattice parameter of NaCl
    crystal, m
4 Y = 5e+010; // Modulus of elasticity along [100]
    direction of NaCl, newton per metre square
5 m = 23; // Atomic weight of sodium, amu
6 M = 37; // Atomic weight of chlorine, amu

```

```

7 amu = 1.67e-027;    // Kg equivalent of 1 amu
8 K = a*Y;    // Force constant of springs when the
    extension along [100] direction is neglected, N/m
9 omega_plus_max = (2*K*(1/(M*amu)+1/(m*amu)))^(1/2);
    // The maximum angular frequency of the
    reflected electromagnetic radiation, rad per sec
10 lambda = 2*pi*c/omega_plus_max;    // The
    wavelength at which the electromagnetic radiation
    is strongly reflected, m
11 printf("\nThe wavelength at which the
    electromagnetic radiation is strongly reflected
    by the crystal = %4.2e m", lambda);
12 // Result
13 // The wavelength at which the electromagnetic
    radiation is strongly reflected by the crystal =
    3.88e-005 m

```

---

## Chapter 8

# Diffraction of Waves and Particles by Crystals

Scilab code Exa 8.1 Shortest wavelength and frequency of X rays from accelerating

```
1 // Scilab Code Ex08.1 Determination of shortest
   wavelength and frequency of X-rays from
   accelerating potential Page-250 (2010)
2 V = 50e+03; // Accelerating potential, volt
3 c = 3e+08; // Speed of light in free space
4 Lambda_min = 1.24e-06/V; // Minimum wavelength,
   metre
5 F_max = c/Lambda_min; // Maximum frequency, Hz
6 printf("\nThe shortest wavelength present in X-rays
   = %4.2f angstrom", Lambda_min/1D-10);
7 printf("\nThe maximum frequency present in X-rays =
   %3.1e Hz", F_max);
8 // Result
9 // The shortest wavelength present in X-rays = 0.25
   angstrom
10 // The maximum frequency present in X-rays = 1.2e+19
   Hz
```

---

Scilab code Exa 8.2 Impinging electrons on the target and characteristics of X ray

```
1 // Scilab Code Ex8.2 Calculation of impinging
   electrons on the target and characteristics of X-
   rays Page-253 (2010)
2 I = 2.5e-03; // Current through X-ray tube,
   ampere
3 V = 6e+03; // Potential across the X-ray tube,
   volt
4 e = 1.6e-19; // Charge on an electron, coulomb
5 m = 9.1e-31; // mass of an electron, kg
6 t = 1; // Transit time, second
7 Q = I*t; // Total charge flowing per second
   through the x-ray tube, coulomb
8 n = Q/e; // Number of electrons striking the
   target per second
9 // We have  $eV = 1/2*m*v^2$  (stopping potential =
   maximum Kinetic energy)
10 // Solving for v
11 v = sqrt(2*e*V/m); // speed of electrons striking
   the target, m/s
12 Lambda_min = 1.24e-06/V; // Minimum wavelength of
   X-rays produced, metre
13 printf("\nThe number of electrons striking the
   target = %4.2e",n);
14 printf("\nThe velocity of electrons striking the
   target = %4.2e m/s",v);
15 printf("\nThe shortest wavelength present in X-rays
   = %4.2e m", Lambda_min);
16 // Result
17 // The number of electrons striking the target =
   1.56e+016
18 // The velocity of electrons striking the target =
   4.59e+007 m/s
```

```
19 // The shortest wavelength present in X-rays = 2.07e
    -010 m
```

---

### Scilab code Exa 8.3 Wavelength of characteristic X rays

```
1 // Scilab Code Ex8.3 Calculation of wavelength of
    characteristic X-rays Page-253 (2010)
2 h = 6.626e-034; // Planck's constant, Js
3 c = 3e+08; // Speed of light in free space, m/s
4 e = 1.602e-019; // Charge on an electron, coulomb
5 E_K = -78; // Energy of K shell for platinum, keV
6 E_L = -12; // Energy of L shell for platinum, keV
7 E_M = -3; // Energy of M shell for platinum, keV
8 E_K_alpha = E_L - E_K; // Energy of K_alpha line,
    keV
9 E_K_beta = E_M - E_K; // Energy of K_beta line,
    keV
10 // We have  $E = h*f$ , where  $f = c/\text{Lambda}$  this implies
     $E = h*c/\text{lambda}$ 
11 // Solving for Lambda
12 //  $\text{Lambda} = h*c/E$ 
13 lambda_K_alpha = h*c/(E_K_alpha*e*1e+03); //
    Wavelength of K_alpha line, metre
14 lambda_K_beta = h*c/(E_K_beta*e*1e+03); //
    Wavelength of K_beta line, metre
15 printf("\nThe wavelength of K_alpha line = %4.2 f
    angstrom", lambda_K_alpha/1D-10);
16 printf("\nThe wavelength of K_beta line = %4.2 f
    angstrom", lambda_K_beta/1D-10);
17 // Result
18 // The wavelength of K_alpha line = 0.19 angstrom
19 // The wavelength of K_beta line = 0.17 angstrom
```

---

#### Scilab code Exa 8.4 Atomic number of an unknown element

```
1 // Scilab Code Ex8.4 Calculation of atomic number of
  an unknown element Page-255 (2010)
2 lambda_Pt = 1.321e-010; // Wavelength of L_alpha
  line of Pt, m
3 Z_Pt = 78; // Atomic number of platinum
4 b = 7.4; // Constant
5 lambda_x = 4.174e-010; // Wavelength of unknown
  element, m
6 // We have  $f = [a*(Z-b)]^2$  (Moseley's law)
7 // As  $f_{Pt} = c/\lambda_{Pt} = [a*(Z_{Pt}-b)]^2$ 
8 // Similarly  $f_x = c/\lambda_x = [a*(Z_x-b)]^2$ 
9 // Dividing  $f_{Pt}$  by  $f_x$  and solving for x
10 Z_x = b + sqrt(lambda_Pt/lambda_x)*(Z_Pt-b); //
  Atomic number of unknown element
11 printf("\nThe atomic number of unknown element = %4
  .1f", Z_x);
12 // Result
13 // The atomic number of unknown element = 47.1
```

---

#### Scilab code Exa 8.5 Wavelength of copper using Moseley law

```
1 // Scilab Code Ex8.5 Calculation of wavelength of
  copper using Moseley's law Page-256 (2010)
2 c = 3.0e+08; // Speed of light, m/s
3 lambda_W = 210e-010; // Wavelength of K_alpha
  line of W, m
4 Z_W = 74; // Atomic number of tungsten
5 Z_Cu = 29; // Atomic number of copper
6 b = 1; // Constant for K-series
7 //  $f_W = c/\lambda_W = (a*73)^2$ , The frequency
  K_alpha line for tungsten, Hz
8 //  $f_{Cu} = c/\lambda_{Cu} = (a*28)^2$ , The frequency
  K_alpha line for copper, Hz
```

```

9 // Dividing f_W by f_Cu and solving for lambda_Cu
10 lambda_Cu = ((Z_W-b)/(Z_Cu-b))^2*lambda_W; //
    Wavelength of K_alpha line of Cu, m
11 printf("\nThe wavelength of K_alpha line of copper =
    %4.0f angstrom", lambda_Cu/1D-10);
12 // Result
13 // The wavelength of K_alpha line of copper = 1427
    angstrom

```

---

### Scilab code Exa 8.6 Atomic number from wavelength using Moseley law

```

1 // Scilab Code Ex8.6 Calculation of atomic number
    from wavelength using Moseley's law Page-256
    (2010)
2 c = 3.0e+08; // Speed of light , m/s
3 h = 6.626e-034; // Planck's constant , Js
4 epsilon_0 = 8.85e-012; // Absolute electrical
    permittivity of free space , coulomb square per
    newton per metre square
5 m = 9.1e-031; // Mass of an electron , kg
6 e = 1.6e-019; // Charge on an electron , C
7 lambda = 0.7185e-010; // Wavelength of K_alpha
    line of unknown element
8 b = 1; // Mosley's constant for K-series
9 n_1 = 1; n_2 = 2; // Lower and upper energy
    levels
10 // We know that  $f = c/\lambda = m \cdot e^4 \cdot (Z-b)^2 / (8 \cdot$ 
     $\epsilon_0^2 \cdot h^3) \cdot (1/n_2^2 - 1/n_1^2)$ 
11 // This implies that  $\lambda = (8 \cdot \epsilon_0^2 \cdot c \cdot h^3 / ($ 
     $m \cdot e^4 \cdot (Z-b)^2 \cdot (1/n_2^2 - 1/n_1^2))$ 
12 // Solving for Z
13 Z = sqrt(8*epsilon_0^2*c*h^3/(m*e^4*lambda*(1/n_1
    ^2-1/n_2^2)))+b; // Atomic number unknown element
14 printf("\nThe atomic number unknown element = %2d",
    Z);

```



```

15 // Result
16 // The atomic number unknown element = 42

```

---

**Scilab code Exa 8.7** Wavelengths of tin and barium using Moseley law

```

1 // Scilab Code Ex8.7 Calculation of wavelengths of
  tin and barium using Moseley's law Page-257
  (2010)
2 Z_Fe = 26; // Atomic number of iron
3 Z_Pt = 78; // Atomic number of platinum
4 Z_Sn = 50; // Atomic number of tin
5 Z_Ba = 56; // Atomic number of barium
6 b = 1; // Mosley's constant for K-series
7 lambda_Fe = 1.93e-010; // Wavelength of K-alpha
  line of Fe
8 lambda_Pt = 0.19e-010; // Wavelength of K-alpha
  line of Pt
9 // From Moseley's Law,
10 //  $f = a*(Z-1)^2$ . This implies  $\lambda = C*1/(Z-1)^2$ 
11 // so that  $\lambda_{Fe} = C*1/(Z_{Fe}-1)^2$  and  $\lambda_{Sn}$ 
  =  $C*1/(Z_{Sn}-1)^2$ 
12 // Dividing  $\lambda_{Sn}$  by  $\lambda_{Fe}$  and solving for
  lambda_Sn
13 lambda_Sn = (Z_Fe-1)^2/(Z_Sn-1)^2*lambda_Fe; //
  Wavelength of K-alpha line for tin, m
14 lambda_Ba = (Z_Pt-1)^2/(Z_Ba-1)^2*lambda_Pt; //
  Wavelength of K-alpha line for barium, m
15 printf("\nThe wavelengths of tin and barium = %3.1f
  angstrom and %4.2f angstrom respectively",
  lambda_Sn/1D-10, lambda_Ba/1D-10);
16 // Result
17 // The wavelengths of tin and barium = 0.5 angstrom
  and 0.37 angstrom respectively

```

---

**Scilab code Exa 8.8** Percentage transmitted energy of X rays

```
1 // Scilab Code Ex8.8 Percentage transmitted energy
  of X-rays: Page 259 (2010)
2 mu = 139; // Attenuation co-efficient of
  aluminium, per metre
3 x = 0.005; // Thickness of aluminium sheet, m
4 // If X% is the intensity of the X-ray transmitted
  through the aluminium sheet then
5 //  $X\% = I/I_0$ 
6 // or  $X/100 = \exp(-\text{absorb\_coeff} * x)$ 
7 // Solving for X
8 X = 100*exp(-mu*x); // Transmitted percentage of
  X-rays
9 printf("\nThe intensity of the X-ray transmitted
  through the aluminium sheet = %g percent", round(
  X));
10 // Result
11 // The intensity of the X-ray transmitted through
  the aluminium sheet = 50 percent
```

---

**Scilab code Exa 8.9** Thickness of lead piece by using two equal intensity X ray wav

```
1 // Scilab code Ex8.9 : Determination of thickness of
  lead piece by using two equal intensity X-ray
  wavelengths : Page 259 (2010)
2 lambda_1 = 0.064e-010; // First wavelength of X-
  ray, metre
3 lambda_2 = 0.098e-010; // Second wavelength of X-
  ray, metre
4 I1_ratio_I2 = 3; // Ratio of attenuated beam
  intensity
```

```

5 mu_m1 = 0.164;    // Mass absorption coefficient for
   first wavelength, metre square per kg
6 mu_m2 = 0.35;    // Mass absorption coefficient for
   second wavelength, metre square per kg
7 d = 0.164;      // Density of the lead, kg per metre
   cube
8 mu1 = mu_m1*d;   // absorption co-efficient of the
   lead for first wavelength, per metre
9 mu2 = mu_m2*d;   // absorption co-efficient of the
   lead for second wavelength, per metre
10 x = poly(0,"x"); // Declare 'x' as the thickness
   variable
11 // Now I = exp(-ac*x) thus
12 // I1_ratio_I2 = exp(-ac_1*x)/exp(-ac_2*x)
13 // or 3 = exp(2109.24)*x this implies
14 // 2104.24*x = log(3) and assume
15 p = 2104.24*x - log(3);
16 printf("\nThe thickness of lead piece = %4.2e m",
   roots(p));
17 // Result
18 // The thickness of lead piece = 5.22e-004 m

```

---

**Scilab code Exa 8.10** Angle of reflection by using wavelength of X rays

```

1 // Scilab code Ex8.10: Determining angle of
   reflection by using wavelength of X-ray Page 261
   (2010)
2 lambda = 0.440e-010; // Wavelength of X-rays, m
3 d = 2.814e-010;     // Interplanar spacing of
   rocksalt crystal, m
4 // 2*d*sin(theta) = n*lambda    **Bragg's law, n is
   the order of diffraction
5 // Solving for theta, we have
6 // theta = asin(n*lambda/(2*d))
7 // Declare a function for converting angle into

```

```

degrees and minutes
8 function [d,m] = degree_minute(n)
9     d = int(n);
10    m = (n-int(n))*60;
11 endfunction
12 for n = 1:1:5    // For diffraction order from 1 to
13                5
14    theta = asind(n*lambda/(2*d));    // Bragg's
15    angle
16    [deg, mint] = degree_minute(theta);    // Call
17    conversion function
18    printf("\nTheta%d = %2d degree(s), %2d minute(s)
19           ", n, deg, mint);
20 end
21 // Result
22 // Theta1 = 4 degree(s), 29 minute(s)
23 // Theta2 = 8 degree(s), 59 minute(s)
24 // Theta3 = 13 degree(s), 33 minute(s)
25 // Theta4 = 18 degree(s), 13 minute(s)
26 // Theta5 = 23 degree(s), 0 minute(s)

```

---

#### Scilab code Exa 8.11 Wavelength of diffracted X rays

```

1 // Scilab code Ex8.11: Determining the wavelength of
2 // diffracted X-rays Page 262 (2010)
3 d = 2.814e-010;    // Interplanar spacing of
4 // rocksalt crystal, m
5 theta = 9;    // Bragg's angle, degree
6 // 2*d*sin(theta) = n*lambda    **Bragg's law, n is
7 // the order of diffraction
8 // Solving for lambda, we have
9 // lambda = 2*d*sin(theta)/n;
10 printf("\nThe first four wavelengths of diffracted
11 beam are:");
12 for n = 1:1:5    // For diffraction order from 1 to

```

```

5
9     lambda = 2*d*sind(theta)/n;      // Wavelength of
      X-rays , m
10    if lambda >= 0.2e-010 & lambda <= 1.0e-010 then
11        printf("\nLambda%d = %6.4e angstrom", n,
      lambda/1D-10);
12    end
13 end
14 // Result
15 // The first four wavelengths of diffracted beam are
      :
16 // Lambda1 = 8.8041e-001 angstrom
17 // Lambda2 = 4.4021e-001 angstrom
18 // Lambda3 = 2.9347e-001 angstrom
19 // Lambda4 = 2.2010e-001 angstrom

```

---

**Scilab code Exa 8.12** Reciprocal lattice parameters from 2D direct lattice parameters

```

1 // Scilab code Ex8.12: Reciprocal lattice parameters
      from 2-D direct lattice parameters Page 277
      (2010)
2 a = 3e-010;      // First lattice parameter of direct
      lattice
3 b = 5e-010;      // Second lattice parameter of direct
      lattice
4 theta = 60;      // Angle between two lattice vectors
      of the direct lattice
5 // if a_prime and b_prime are the lattice vectors
      for the reciprocal lattice , then
6 // a_prime*a = 2*%pi and a_prime*b = 0
7 // Similarly , b_prime*b = 2*%pi and b_prime*a = 0
8 // Solving for a_prime and b_prime , we have
9 a_prime = 2*%pi/(a*cosd(90-theta)); // Lattice
      vector for reciprocal lattice , per metre
10 b_prime = 2*%pi/(b*cosd(90-theta)); // Lattice

```

```

    vector for reciprocal lattice , per metre
11 printf("\nThe reciprocal lattice vectors are:\n
    a_prime = %5.2f per angstrom and b_prime = %5.2f
    per angstrom", a_prime*1e-010, b_prime*1e-010);
12 // Result
13 // The reciprocal lattice vectors are:
14 // a_prime = 2.42 per angstrom and b_prime = 1.45
    per angstrom

```

---

### Scilab code Exa 8.13 Bragg angle and the indices of diffraction of Powder Lines

```

1 // Scilab code Ex8.13: Bragg angle and the indices
    of diffraction of Powder Lines Page 285 (2010)
2 n = 1; // Consider first order diffraction
3 a = 6e-010; // First lattice parameter of direct
    lattice , m
4 lambda = 1.54e-010; // Wavelength used in
    diffraction of X-rays by Powder Method, m
5 // Declare a function for converting angle into
    degrees and minutes
6 function [d,m] = degree_minute(n)
7     d = int(n);
8     m = (n-int(n))*60;
9 endfunction
10 // Calculate the hkl and hence interplanar spacing '
    d' for three lowest powder lines
11 printf("\nThe Bragg angles and the indices of
    diffraction for the three lowest powder lines are
    :");
12 for h = 0:1:2
13     for k = 0:1:2
14         for l = 0:1:1
15             if (modulo(h,2) == 1 & modulo(k,2) == 1
                & modulo(l,2) == 1) | (modulo(h,2)
                == 0 & modulo(k,2) == 0 & modulo(l

```

```

,2) == 0) then
16     if (h <> 0) then
17         N = h^2+k^2+l^2;
18         d = a/sqrt(N);    // Interplanar
                             spacing, metre
19         theta = asind(n*lambda/(2*d));
20         [deg, mint] = degree_minute(
                             theta);    // Call conversion
                             function
21         printf("\nd[%d%d%d] = %4.2e and
                             theta [%d%d%d] = %d deg %d min
                             ", h, k, l, d, h, k, l, deg,
                             mint);
22     end
23     end
24     end
25     end
26 end
27 // Result
28 // The Bragg angles and the indices of diffraction
    for the three lowest powder lines are:
29 // d[111] = 3.46e-010 and theta[111] = 12 deg 50 min
30 // d[200] = 3.00e-010 and theta[200] = 14 deg 52 min
31 // d[220] = 2.12e-010 and theta[220] = 21 deg 17 min

```

---

**Scilab code Exa 8.14** Minimum distance from the centre of the Laue pattern

```

1 // Scilab code Ex8.14: Minimum distance from the
    centre of the Laue pattern of an fcc crystal
    Page 289 (2010)
2 n = 1;    // Consider the first order diffraction
3 a = 4.5e-010;    // Lattice parameter for fcc
    lattice, m
4 V = 50e+03;    // Potential difference across the X-
    ray tube, volt

```

```

5 D = 5;      // Crystal to film distance , cm
6 h = 1, k = 1, l = 1;    // Incides for the planes of
    maximum spacing
7 lambda_min = 1.24e-06/V;    // The cut-off
    wavelength of X-rays , m
8 d_111 = a/sqrt(h^1+k^2+l^2);
9 theta_111 = asind(n*lambda_min/(2*d_111));
10 // As tan(2*theta_111) = x/D, solving for x
11 x = D*tand(2*theta_111);    // // Minimum distance
    from the centre of Laue pattern
12 printf("\n\nThe minimum distance from the centre of
    the Laue pattern at which reflections can occur
    from the planes of maximum spacing = %4.2f cm", x
    );
13 // Result
14 // The minimum distance from the centre of the Laue
    pattern at which reflections can occur from the
    planes of maximum spacing = 0.48 cm

```

---

**Scilab code Exa 8.15** Unit cell height along the axis of a rotation photograph

```

1 // Scilab code Ex8.15: Calculating unit cell height
    along the axis of a rotation photograph Page 291
    (2010)
2 n = 1;    // Consider the first order diffraction of
    X-rays
3 S = [0.29,0.59,0.91,1.25,1.65,2.12];    // An array
    of heights of first six layers above(below) the
    zero layer , cm
4 R = 3;    // Radius of the camera , cm
5 lambda = 1.54e-08;    // Wavelength of the X-rays ,
    cm
6 // For an a-axis rotation photograph , the unit cell
    parameter is given by
7 //  $a = n*\lambda/S(n)*(R^2 + S(n)^2)^{(1/2)}$ 

```



```

8 // Calculate 'a' for six different values of n from
  1 to 6
9 for n = 1:1:6
10     a = (n*lambda/S(n))*(R^2 + S(n)^2)^(1/2);
11 end
12 printf("\nThe unit cell height of the crystal = %2.0
    f angstrom", a/1D-8);
13
14 // Result
15 // The unit cell height of the crystal = 16 angstrom

```

---

**Scilab code Exa 8.16** Diffraction of thermal neutrons from planes of Ni crystal

```

1 // Scilab code Ex8.16: Diffraction of thermal
  neutrons from planes of Ni crystal Page 294
  (2010)
2 k = 1.38e-023; // Boltzmann constant, J/mol/K
3 h = 6.626e-034; // Planck's constant, Js
4 theta = 28.5; // Bragg's angle, degree
5 a = 3.52e-010; // Lattice parameter of fcc
  structure of nickel, m
6 m_n = 1.67e-027; // Rest mass of neutron, kg
7 // For fcc lattice, the interplanar spacing is given
  by
8 d = a/sqrt(3); // Interplanar spacing of Ni, m
9 // Bragg's equation for first order diffraction (n =
  1) is
10 lambda = 2*d*sind(theta); // Bragg's law, m
11 // From kinetic interpretaion of temperature, we
  have
12 // (1/2)*m*v^2 = (3/2)*k*T -- (a)
13 // Further from de-Broglie relation
14 // lambda = h/(m*v) -- (b)
15 // From (a) and (b), solving for T, we have
16 T = h^2/(3*m_n*k*lambda^2); // Effective

```

```

    temperature of the neutrons , K
17 printf("\nThe effective temperature of neutrons = %d
    K", T);
18 // Result
19 // The effective temperature of neutrons = 168 K

```

---

**Scilab code Exa 8.17** Diffraction of electrons from fcc crystal planes

```

1 // Scilab code Ex8.17: Diffraction of electrons from
    fcc crystal planes Page 295 (2010)
2 // Declare a function for converting angle into
    degrees and minutes
3 function [d,m] = degree_minute(n)
4     d = int(n);
5     m = (n-int(n))*60;
6 endfunction
7 h = 6.626e-034; // Planck's constant , Js
8 m = 9.1e-031; // Rest mass of electron , kg
9 e = 1.602e-019; // charge on an electron , coulomb
10 a = 3.5e-010; // Lattice parameter of fcc crystal
    , m
11 V = 80; // Accelerating potential for electrons ,
    volt
12 lambda = h/sqrt(2*m*e*V); // de-Broglie
    wavelength of electrons , m
13 d_111 = a/sqrt(3); // Interplanar spacing for
    (111) planes of fcc crystal , m
14 // Bragg's equation for first order diffraction (n =
    1) is
15 // lambda = 2*d_111*sind(theta_111); // Bragg's
    law , m
16 theta_111 = asind(lambda/(2*d_111)); // Bragg's
    angle , degree
17 [deg, mint] = degree_minute(theta_111); // Call
    conversion function

```

```
18 printf("\nThe Bragg angle for electron diffraction =
    %d deg %d min", deg, mint);
19 // Result
20 // The Bragg angle for electron diffraction = 19 deg
    50 min
```

---

# Chapter 9

## Thermal Properties of Materials

Scilab code Exa 9.1 Exception of Dulong Petit law at room temperature

```
1 // Scilab Code Ex9.1 Exception of Dulong-Petit law
   at room temperature: Page-303(2010)
2 h = 6.626e-034; // Planck's constant, joule
   second
3 k = 1.38e-023; // Boltzmann constant, joule/mol/
   kelvin
4 T = 300; // Room temperature, kelvin
5 f_Ag = 4.0e+012; // Vibrational frequency for
   silver, cycles/second
6 f_Dia = 2.4e+013; // Vibrational frequency for
   diamond, cycles/second
7 E_Ag = h*f_Ag; // Vibrational Energy for silver,
   joule
8 E_Dia = h*f_Dia; // Vibrational Energy for
   diamond, joule
9 E_th = k*T; // Thermal energy at room temperature
   , joule
10 if E_th > E_Ag & E_th < E_Dia then
11     printf("\nSince E_Ag < kT and E_Dia > kT,
```

```

        therefore ,");
12     printf("\nSilver metal obeys the Dulong Petit
        law at room temperature while diamond does
        not.");
13 end
14 // Result
15 // Since E_Ag < kT and E_Dia > kT, therefore ,
16 // Silver metal obeys the Dulong Petit law at room
        temperature while diamond does not.

```

---

### Scilab code Exa 9.2 Specific heat of copper from Debye temperature

```

1 // Scilab Code Ex9.2 Specific heat of copper from
    Debye temperature: Page-311(2010)
2 h = 6.626e-034; // Planck's constant, joule
    second
3 k = 1.38e-023; // Boltzmann constant, joule/mol/
    kelvin
4 T = 30; // Given temperature, kelvin
5 N = 6.023e+023; // Avogadro's number
6 R = N*k; // Universal gas constant, joule/kelvin
7 v_l = 4.76e+03; // Longitudinal velocity of
    lattice waves, m/s
8 v_t = 2.32e+03; // Tranverse velocity of lattice
    waves,
9 rho = 8.9e+03; // Density of copper, kg per metre
    cube
10 A_Cu = 63.5; // Gram atomic mass of Cu, g
11 M = A_Cu*1e-03; // Mass of 1 mole of Cu-atoms, kg
12 V = M/rho; // Volume of copper, metre cube
13 theta_D = (h/k)*((9*N)/((4*pi*V)*((1/v_l^3)+(2/v_t
    ^3))))^(1/3); // Debye temperature of copper,
    K
14 C_v = 12/5*pi^4*R*(T/theta_D)^3; // Specific
    heat of copper, kJ/kmol/kelvin

```

```

15 printf("\nThe specific heat of copper = %4.2f kJ/
    kmol/kelvin", C_v);
16 // Result
17 // The specific heat of copper = 1.33 kJ/kmol/kelvin

```

---

**Scilab code Exa 9.3** Vibrational frequency and molar heat capacity of diamond

```

1 // Scilab Code Ex9.3 Vibrational frequency and molar
    heat capacity of diamond: Page-312(2010)
2 h = 6.626e-034; // Planck's constant, joule
    second
3 k = 1.38e-023; // Boltzmann constant, joule/mol/
    kelvin
4 T = 10; // Given temperature, kelvin
5 N = 6.023e+023; // Avogadro's number
6 R = N*k; // Universal gas constant, joule/kelvin
7 theta_D = 2230; // Debye temperature for diamond,
    kelvin
8 f_D = k*theta_D/h; // Debye frequency of diamond,
    hertz
9 C_v = 12/5*pi^4*R*1e+03*(T/theta_D)^3; //
    Specific heat of diamond, J/kmol/kelvin
10 printf("\nThe highest possible vibrational frequency
    of diamond = %4.2e per second", f_D);
11 printf("\nThe molar specific heat of diamond = %5.3f
    J/kmol/kelvin", C_v);
12 // Result
13 // The highest possible vibrational frequency of
    diamond = 4.64e+013 per second
14 // The molar specific heat of diamond = 0.175 J/kmol
    /kelvin

```

---

**Scilab code Exa 9.4** Debye temperature of copper at low temperature

```

1 // Scilab Code Ex9.4 Debye temperature of copper at
  low temperature: Page-312(2010)
2 k = 1.38e-023; // Boltzmann constant, joule/mol/
  kelvin
3 N = 6.023e+023; // Avogadro's number
4 R = N*k; // Universal gas constant, joule/kelvin
5 C_vl = 4.6e-02; // Lattice specific heat, J/kmol/
  K
6 // Lattice specific heat C_vl = Molar lattice
  specific heat, C_v
7 // or  $12/5 * \pi^4 * R / (5 * \theta_D^3) = C_{vl}$ 
8 // solving for theta_D, we have
9 theta_D = (12 * pi^4 * R * 1e+03 / (5 * C_vl))^(1/3); //
  Debye temperature of copper at low temperature, K
10 printf("\nDebye temperature of copper at low
  temperature = %3d K", theta_D);
11 // Result
12 // Debye temperature of copper at low temperature =
  348 K

```

---

#### Scilab code Exa 9.5 Debye temperature for gold

```

1 // Scilab Code Ex9.5 Debye temperature for gold :
  Page-313(2010)
2 h = 6.626e-034; // Planck's constant, Js
3 k = 1.38e-023; // Boltzmann constant, joule/mol/
  kelvin
4 N = 6.023e+023; // Avogadro's number
5 R = N*k; // Universal gas constant, joule/kelvin
6 M = 197e-03; // Gram atomic weight of gold, g
7 rho = 1.9e+04; // Density of gold, kg per metre
  cube
8 V = M/rho; // Volume of gold, metre cube
9 v = 2100; // Velocity of sound in gold medium, m/
  s

```

```

10 theta_D = h*v/k*(9*N/(12*pi*V))^(1/3);    // Debye
    temperature for gold, K
11 printf("\nDebye temperature of gold = %3d K",
    theta_D);
12 // Result
13 // Debye temperature of gold = 242 K

```

---

**Scilab code Exa 9.6** Heat transference into rock salt at low temperature

```

1 // Scilab Code Ex9.6 Heat transference into rock
    salt at low temperature: Page-313(2010)
2 A = 464;    // Atomic specific heat of rock salt,
    cal g/mol/kelvin
3 theta_D = 281;    // Debye temperature of rock salt,
    K
4 delta_T = 10;    // Rise in temperature in each
    class interval, K
5 // Define a function which returns lattice specific
    heat at constant volume
6 function [C_vl] = lattice_SH(T)
7     C_vl = A*(T/theta_D)^3;
8 endfunction
9 Q = 0;    // Initialize heat accumulator to zero,
    cal
10 for t = 10:10:40
11     mean_temp = (t + (t + 10))/2;    // Calculate
        mean temperature of each class interval, K
12     Q = Q + 2*delta_T*lattice_SH(mean_temp);    //
        Accumulate heat for each step
13 end
14 printf("\nThe amount of heat required to raise the
    temperature of 2 gmol of Rock salt from 10K to 50
    K = %5.2f cal", Q);
15 // Result
16 // The amount of heat required to raise the

```



temperature of 2 gmol of Rock salt from 10K to 50  
K = 63.99 cal

---

# Chapter 10

## Free Electrons in Crystals

Scilab code Exa 10.1 Particle moving in one dimensional potential well

```
1 // Scilab Code Ex10.1 Particle Moving in One-
   Dimensional Potential Well: Page-328 (2010)
2 a = 10^-3; //Separation between the walls of the
   well, m
3 m = 10^-9; // Mass of the dust particle, kg
4 t = 100; // Average time for successive collisions
   with the wall, s
5 h = 6.626*10^-34; // Plank's constant, Js
6 v = a/t; // Velocity of the particle inside the
   potential well, m/s
7 E = 1/2*m*v^2; // Kinetic energy of the particle, J
8 // For one-dimensional potential well, the energy
   eigen value is given by
9 //           E = h^2*n^2/(8*m*a^2)
10 // Solving for n
11 n = sqrt((8*m*a^2*E)/h^2) // Quantum number
   corresponding to the energy eigen value E
12 disp (n, "The quantum number described by this
   motion is:")
13 // Result
14 // The quantum number described by this motion is:
```

15 // 3.018D+16

---

**Scilab code Exa 10.2** Motion of a ground state electron in a 3D potential well

```
1 // Scilab Code Ex 10.2 Motion of a ground state
  Electron in a 3-D Potential Well: Page-329 (2010)
2 a = 0.5*10^-10; // length of the potential box, m
3 h = 6.626*10^-34; // Plank's Constant, Js
4 m = 9.1*10^-31; // Mass of an Electron, kg
5 // In 3-D, the three quantum numbers nx, ny and nz
  each will have value equal to 1 for lowest energy
  state
6 nx = 1; // Quantum number corresponding to x-
  direction
7 ny = 1; // Quantum number corresponding to y-
  direction
8 nz = 1; // Quantum number corresponding to z-
  direction
9 EG = h^2*(nx^2+ny^2+nz^2)/(8*m*a^2); // Energy eigen
  value for 3-D potential, J
10 EeV = EG/1.6D-19; // Convert energy from joule to eV
11 disp (EeV, "The lowest energy of an electron
  confined to move in a 3D-potential box, in eV, is
  : ")
12 //Result
13 // The lowest energy of an electron confined to move
  in a 3D-potential box, in eV, is :
14 // 452.30641
```

---

**Scilab code Exa 10.3** Motion of an electron excited next to the ground state in a 3

```

1 // Scilab Code Ex 10.3 Motion of an Electron excited
   next to the ground state in a 3-D Potential Well
   : Page-329 (2010)
2 a = 1D-10; // length of the cubic potential box,
   m
3 h = 6.626*10^-34; // Plank's Constant, Js
4 m = 9.1*10^-31; // Mass of an Electron, kg
5 k = 1.38D-23; // Boltzmann Constant, J/mol-K
6 // In 3-D, the three quantum numbers nx, ny and nz
   will have values 1, 1 and 2 respectively for
   first excited energy state
7 nx = 1; // Quantum number corresponding to x-
   direction
8 ny = 1; // Quantum number corresponding to y-
   direction
9 nz = 2; // Quantum number corresponding to z-
   direction
10 EE = h^2*(nx^2+ny^2+nz^2)/(8*m*a^2); // Energy eigen
   value for 3-D potential for first excited state,
   J
11 // As EE(next to the lowest) = 3/2 (k/T), where T is
   the absolute temperature
12 // Solving for T
13 T = 2/3*1/k*EE; // Absolute temperature at which
   energy next to the lowest energy state = 3/2 (k/T
   ), K
14 EeV = EE/1.6D-19; // Convert energy from joule to eV
15 disp (EeV, "The first excited state energy of the
   electron confined to move in a 3D-potential box,
   in eV, is : ")
16 disp (T, "The temperature at which the average
   energy becomes equal to first excited state
   energy, in K, is : ")
17 //
18 //Result
19 // The first excited state energy of the electron
   confined to move in a 3D-potential box, in eV, is
   :

```

```

20 //      226.15321
21 // The temperature at which the average energy
    becomes equal to first excited state energy, in K
    , is :
22 //      1748044.1

```

---

#### Scilab code Exa 10.4 Degeneracy of energy level

```

1 // Scilab Code Ex 10.4 Degeneracy of Energy Level:
    Page-332 (2010)
2 // Function to find the factorial of a number
3 function [f] = fact(num)
4     f = 1;
5     for i = 1:1:num
6         f = f*i;
7     end
8 endfunction
9
10 // Fucntion to determine degenerate energy states
11 function [degstates] = degno(a, b, c) // degno takes
    three arguments
12     if a == b & b == c then // check if all the
        values are same
13         degeneracy = 3;
14         degstates = fact(3)/fact(degeneracy); //
            calculate degenerate states
15     end
16     if a == b | b == c | c == a then // check if
        any two values are equal
17         degeneracy = 2;
18         degstates = fact(3)/fact(degeneracy); //
            calculate degenerate states
19     end
20     if a ~= b & b ~= c then // check if all the
        values are different

```

```

21         degeneracy = 1;
22         degstates = fact(3)/fact(degeneracy); //
           calculate degenerate states
23     end
24 endfunction
25 //
26 clc
27 coef = 38; // Coefficient of H^2/(8*m*a^2)
28 nx = zeros(1,5); // Quantum number corresponding
           to x-direction
29 ny = zeros(1, 5); // Quantum number corresponding
           to y-direction
30 nz = zeros(1,5); // Quantum number corresponding
           to z-direction
31 deg = zeros(1,5); // Variable to store the
           degeneracy of states
32 count = 1; // set the counter
33 sum = 0; // initialize the sum
34 // Look for all the possible set of values for nx,
           ny and ny
35 for i = 1:1:10
36     for j = 1:1:10
37         for k = 1:1:10
38             // Check for the condition and avoid
               repetition of set of values
39                 if ((i^2+j^2+k^2==coef) & (i+j+k)> sum)
40                     then
41                         nx(1,count)=i; // Save current i
                           value
42                         ny(1,count)=j; // Save current j
                           value
43                         nz(1,count)=k; // Save current k
                           value
44                         deg(1,count) = degno(i, j, k); //
                           Save degeneracy for given set of
                           values
45                     count = count + 1; // Increment the
                           counter

```

```

45             sum = i + j + k; // Add the three
                values of quantum numbers
46             end
47         end
48     end
49 end
50 printf("\nThe %d set(s) of values of quantum number
        are : \n", count-1);
51 deg_states = 0; // Intialize the variable
52 for i = 1:1:count-1
53     printf("\nnx = %d, ny = %d, nz = %d\n", nx(1,i),
            ny(1,i), nz(1,i));
54     deg_states = deg_states + deg(1,i); //
        Accumulate the degeneracy
55 end
56     printf("\nThe given energy level is %d-fold
        degenerate.", deg_states);
57 //Result
58 // The 2 set(s) of values of quantum number are :
59 //         nx = 1, ny = 1, nz = 6
60 //         nx = 2, ny = 3, nz = 5
61 // The energy level is 9-fold degenerate

```

---

### Scilab code Exa 10.5 Fermi energy of zinc at absolute zero

```

1 //Scilab Code Ex 10.5 Fermi energy of zinc at
  absolute zero: Page-335 (2010)
2 d = 7.13D+3; // Density of Zn, in kg per m cube
3 M = 65.4D-3; // Atomic weight of Zn, kg/mol
4 me = 9.1D-31; // Mass of an electron , kg
5 meff = 0.85*me; // Effective mass of the electron
  in zinc , kg
6 v = 2; // valency of divalent (Zn) metal
7 N = 6.023D+23; // Avogadro's Number
8 h = 6.626D-34; //Plank's constant , in Js

```

```

9  n = v*d*N/M;    // Number of electrons per unit
    volume
10 Ef = h^2/(2*meff)*(3*n/(8*pi))^(2/3); //Fermi
    energy in zinc at absolute zero , J
11 EfeV = Ef/1.6D-19;    // Fermi energy in eV
12 Ebar = (3/5)*EfeV;    // Average energy of an
    electron at 0K, eV
13 disp(EfeV,"The fermi energy in zinc at absolute zero
    ,in eV, is : ");
14 disp(Ebar,"The average energy of an electron at 0K,
    in eV, is : ");
15 //Result
16 // The fermi energy in zinc at absolute zero ,in eV,
    is :
17 // 11.110065
18 // The average energy of an electron at 0K,in eV, is
    :
19 // 6.6660389

```

---

### Scilab code Exa 10.6 Electron probability above Fermi energy

```

1 // Scilab Code Ex 10.6 Electron probability above
    Fermi energy: Page-336 (2010)
2 k = 1.38D-23; // Boltzmann constant , in J/mol-K
3 FD = 0.10;    // Fermi-Dirac distribution
    probability for electrons
4 Efermi = 5.5;    // Fermi Energy of silver , in eV
5 E = Efermi + 0.01*Efermi;    // Allowed energy for
    electrons
6 dE = E - Efermi;    //Deviation of allowed energy
    from Fermi energy , in eV
7 DEeV = dE*1.6D-19; //Convert into joule
8 // The Fermi-Dirac distribution function as at any
    temperature T is given by
9 //          F(E) = FD = 1/(exp((E-Efermi)/kT)+1

```



```

10 // Solving for T
11 T = DEeV/(k*log(1/FD-1)); // Absolute temperature at
    which result follows , in K
12 disp(DEeV, dE, E);
13 disp(T, "The temperature at which the given
    probability is expected , in K, is :");
14 //Result
15 // The temperature at which the given probability
    is expected , in K, is :
16 // 290.2212

```

---

#### Scilab code Exa 10.7 The electroic specific heat of Cu

```

1 // Scilab Code Ex 10.7 The Electroic Specific Heat
    of Cu: Page-341 (2010)
2 k = 1.38D-23; //Boltzmann constant , in J/mol-K
3 N = 6.023D+23; // Avogadro's Number
4 Efermi = 7.05; // Fermi energy of copper , in
    eV
5 EFeV = Efermi*1.6D-19; // Fermi energy conversion ,
    in J
6 T1 = 4; //Lower value of temperature , in K
7 T2 = 300; //Upper value of temperature , in K
8 Ce4 = (%pi^2*k^2*T1)/(2*EFeV)*N; // Electronic
    specific heat at 4K, J/mol/K
9 Ce100 = (%pi^2*k^2*T2)/(2*EFeV)*N; // Electronic
    specific heat at 100K, J/mol/K
10 disp(Ce4, "The Electronic specific heat at 4K, in J/
    mol/K is :");
11 disp(Ce100, "The Electronic specific heat at 100K,
    in J/mol/K is :");
12 //Result
13 // The Electronic specific heat at 4K, in J/mol/K is
    :
14 // 0.0020072

```

```

15 // The Electronic specific heat at 100K, in J/mol/K
    is :
16 // 0.1505404

```

---

**Scilab code Exa 10.8 Electrical resistivity of sodium metal**

```

1 // Scilab Code Ex 10.10 Electron mobility inside
    conductors : Page-346 (2010)
2 e = 1.6D-19; // Electronic charge, in C
3 m = 9.1D-31; // Electronic mass, in kg
4 res = 1.54D-8; // Electrical resistivity of
    silver, in ohm metre
5 E = 100; // Electric field applied along
    the length of the wire, V/m
6 n = 5.8D+28; // Number of conduction electrons
    per unit volume, per metre cube
7 mu = 1/(res*n*e); // Mobility of electron through
    silver, metre square per volt-sec
8 vd = mu*E; // Average drift velocity of
    electrons, m/s
9 t = mu*m/e; // Relaxation time of the electron
    , s
10 disp(mu, "The mobility of electron through silver,
    in metre square per V-s, is : ");
11 disp(vd, "The average drift velocity of electrons,
    in m/s, is : ");
12 disp(t, "c ");
13 // Result
14 // The mobility of electron through silver, in metre
    square per V-s, is :
15 // 0.0069973
16 // The average drift velocity of electrons, in m/s,
    is :
17 // 0.6997313
18 // The average drift velocity of electrons, in m/s,

```

```

19 // is :
// 3.980D-14

```

---

### Scilab code Exa 10.9 Electrical conductivity of Cu

```

1 // Scilab Code Ex 10.9 Electrical Conductivity of Cu
  : Page-345 (2010)
2 e = 1.6D-19; // Electronic charge, C
3 N = 6.023D+23; // Avogadro's number
4 d = 8920; // Density of Copper, kg per metre
  cube
5 A = 63.5; // Atomic weight of copper, g/mole
6 I = 10; // Current through uniform copper wire
  , A
7 D = 16D-4; //Diameter of circular cross-
  section of copper wire, m
8 R = D/2; // Radius of circular cross-
  section of copper wire, m
9 n = d*N/63.5*1D+3; // The number of electrons per
  unit volume in copper, per metre cube
10 J = I/(%pi*R^2); // Current density of electrons
  in copper, ampere per metre square
11 vd = J/(n*e); // Drift velocity of electrons
  in copper, metre per second
12 disp(J,"The current density of electrons in copper,
  in ampere per metre square, is : ");
13 disp(vd,"The drift velocity of electrons in copper,
  in metre per second, is : ");
14 //Result
15 //The current density of electrons in copper, in
  ampere per metre square, is :
16 // 4973592
17 // The drift velocity of electrons in copper, in
  metre per second, is :
18 // 0.0003674

```

---

Scilab code Exa 10.10 Electron mobility inside conductors

```
1 // Scilab Code Ex 10.10 Electron mobility inside
   conductors : Page-346 (2010)
2 e = 1.6D-19; // Electronic charge, in C
3 m = 9.1D-31; // Electronic mass, in kg
4 res = 1.54D-8; // Electrical resistivity of
   silver, in ohm metre
5 E = 100; // Electric field applied along
   the length of the wire, V/m
6 n = 5.8D+28; // Number of conduction electrons
   per unit volume, per metre cube
7 mu = 1/(res*n*e); // Mobility of electron through
   silver, metre square per volt-sec
8 vd = mu*E; // Average drift velocity of
   electrons, m/s
9 t = mu*m/e; // Relaxation time of the electron
   , s
10 disp(mu, "The mobility of electron through silver,
   in metre square per V-s, is : ");
11 disp(vd, "The average drift velocity of electrons,
   in m/s, is : ");
12 disp(t, "c ");
13 // Result
14 // The mobility of electron through silver, in metre
   square per V-s, is :
15 // 0.0069973
16 // The average drift velocity of electrons, in m/s,
   is :
17 // 0.6997313
18 // The average drift velocity of electrons, in m/s,
   is :
19 // 3.980D-14
```

---

Scilab code Exa 10.11 Lorentz number calculation of a solid

```
1 // Scilab Code Ex 10.11 Lorentz number calculation
   of a solid: Page-347 (2010)
2 e = 1.6D-19; // Electronic charge, in C
3 k = 1.38D-23; // boltzmann constant, J/mol-K
4 T = 293; // Absolute temperature of the
   solid
5 K = 390; // Thermal conductivity of copper at 293
   K, W/m-K
6 l = 0.5; // Lenght of the copper wire, m
7 d = 0.3D-3; // Diameter of cross-section of Cu, m
8 r = d/2; // Radius of copper wire, m
9 R = 0.12; // Resistance of copper wire, ohm
10 // As  $R = 1/\text{con} * l / (\%pi * r^2)$ 
11 // Solving for R
12 con =  $1/(\%pi * r^2 * R)$ ; // Conductance of copper,
   per ohm per metre
13 // The Lorentz number is defined as the ratio of the
   Thermal conductivity to the
14 // Electrical conductivity of a solid per degree
   rise in temperature
15 Lexp =  $K/(\text{con} * T)$ ; // Experimental value of
   Lorentz number, watt ohm per kelvin square
16 Lth =  $\%pi^2/3 * (k/e)^2$ ; // Thoeretical value of
   Lorentz number value, watt ohm per kelvin square
17 disp(Lexp, "The experimetal value of Lorentz number,
   in watt ohm per kelvin square, is :");
18 disp(Lth, "The theoretical value of Lorentz number,
   in watt ohm per kelvin square, is :");
19 printf("\nThe theoretical value of Lorentz number is
   %f times higher than the experimental one.\n",
   Lth/Lexp);
20 // Result
```

```

21 // The experimetal value of Lorentz number, in watt
    ohm per kelvin square, is :
22 //      2.258D-08
23 // The theoretical value of Lorentz number, in watt
    ohm per kelvin square, is :
24 //      2.447D-08
25 // The theoretical value of Lorentz number is      times
    higher than the experimental one.
26 //      1.083817

```

---

**Scilab code Exa 10.12** Increase in electrical resistivity of a metal with temperature

```

1 // Scilab Code Ex 10.12 Increase in electrical
    resistivity of a metal with temperature: Page-349
    (2010)
2 function [res] = final_res(T)
3     alpha = 0.0001;    // Temperature co-efficient
        of resistance
4     resi = 0;         // Initial resistivity of the
        nichrome which is an arbitray
5     //constant and can be taken to be zero
6 res = resi + alpha*T; // Final resistivity of the
        nichrome as function of T
7 endfunction
8 T1 = 300;    // Initial temperature of nichrome, K
9 T2 = 1000;   // Final temperature of nichrome, K
10 res300 = final_res(T1); // Final resistivity of the
        nichrome at 300 K
11 res1000 = final_res(T2); // Final resistivity of the
        nichrome at 1000 K
12 percent_res = (res1000 - res300)*100;    //
        Percentage increase in resistivity
13 printf("\\nThe percentage increase in the resistivity
        of nichrome is %d percent", percent_res);
14 // Result

```

```
15 // The percentage increase in the resistivity of
    nichrome is 7 percent
```

---

**Scilab code Exa 10.13** Thermionic emission of a filament

```
1 // Scilab Code Ex 10.13 Thermionic emission of a
    filament: Page-352 (2010)
2 e = 1.6D-19; // Electronic charge, C
3 m = 9.1D-31; // Mass of the electron, kg
4 k = 1.38D-23; // Boltzmann constant, J/mol-K
5 h = 6.626D-34; // Plank's constant, Js
6 W = 4.5; // Work function of tungsten filament,
    eV
7 D = 1D-4; // Diameter of the filament, m
8 r = D/2; // Radius of the filament, m
9 T = 2400; // Temperature of the filament, K
10 l = 0.05; // Length of the filament, m
11 A = 4*%pi*e*m*k^2/h^3; // A constant expressed
    in ampere per metre square
12 // per kelvin square
13 a = 2*%pi*r*l; // Surface area of the
    filament, meter square
14 J = A*T^2*exp(-e*W/(k*T)); // Electronic current
    density of the filament,
15 // ampere per metre
    square
16 I = a*J; // Electric current due to thermionic
    emission, ampere
17 disp(I,"The electric current due to thermionic
    emission, in A, is : ");
18 // Result
19 // The electric current due to thermionic emission,
    in A, is :
20 // 0.0392404
```

---

**Scilab code Exa 10.14** Hall coefficient of sodium based on free electron model

```
1 // Scilab Code Ex 10.14 Hall coefficient calculation
   of sodium based on free electron model: Page-353
   (2010)
2 e = 1.6D-19; // Electronic charge, C
3 a = 4.28D-10; // lattice parameter (side) of the
   unit cell of sodium crystal, m
4 N = 2; // Number of atoms per unit cell in
   bcc structure of sodium
5 n = N/a^3; // Number of electrons per unit volume
   for the sodium crystal, per metre cube
6 RH = -1/(n*e); // Hall coefficient of sodium,
   metre cube per coulomb
7 disp(RH,"The Hall coefficient of sodium , in metre
   cube per coulomb, is : ");
8 // Result
9 // The Hall coefficient of sodium , in metre cube
   per coulomb, is :
10 // -2.450D-10
```

---



# Chapter 11

## Band Theory

Scilab code Exa 11.2 Ratio between kinetic energy of an electron in 2D square lattice

```
1 // Scilab Code Ex11.2 Determining ratio between K.E.
  of an electron in 2D square lattice: Page-370
  (2010)
2 h = 6.626e-034; // Planck's constant, Js
3 m = 9.1e-031; // Mass of an electron, kg
4 a = 1; // For simplicity assuming lattice
  parameter to be unity, m
5 // Case-I when k_x = k_y = %pi/a
6 k_x = %pi/a, k_y = %pi/a; // Wave numbers in X-
  and Y- directions, rad per metre
7 E1 = h^2/(8*%pi^2*m)*(k_x^2 + k_y^2); // Energy
  of the electron inside a Brillouin Zone, J
8 // Case-II when k_x = %pi/a and k_y = 0
9 k_x = %pi/a, k_y = 0; // Wave numbers in X- and Y
  - directions, rad per metre
10 E2 = h^2/(8*%pi^2*m)*(k_x^2 + k_y^2); // Energy
  of the electron inside a Brillouin Zone, J
11 E_ratio = E1/E2; // Ratio between K.E. of an
  electron in 2D square lattice
12 printf("\nThe ratio between K.E. of an electron in 2
  D square lattice = %ld", E_ratio);
```

```
13 // Result
14 // The ratio between K.E. of an electron in 2D
    square lattice = 2
```

---

# Chapter 13

## Semiconducting Properties of Materials

Scilab code Exa 13.3 Intrinsic concentration of charge carriers in semiconductors

```
1 // Scilab Code Ex13.3 Intrinsic concentration of
  charge carriers in semiconductors: Page-432
  (2010)
2 k = 1.38e-023; // Boltzmann constant, J/mol/K
3 h = 6.626e-034; // Planck's constant, Js
4 eV = 1.6e-019; // Joule equivalent of 1 eV
5 T = 300; // Room temperature, kelvin
6 m_0 = 9.1e-031; // Rest mass of an electron, kg
7 m_e = 0.12*m_0; // Effective mass of electron, kg
8 m_h = 0.28*m_0; // Effective mass of electron, kg
9 E_g = 0.67; // Energy gap of Ge, eV
10 n_i = 2*(2*pi*k*T/h^2)^(3/2)*(m_e*m_h)^(3/4)*exp(-
  E_g*eV/(2*k*T)); // Intrinsic carrier
  concentration of Ge, per metre cube
11 printf("\nThe intrinsic carrier concentration of Ge
  = %3.1e per metre cube", n_i);
12 // Result
13 // The intrinsic carrier concentration of Ge = 4.7e
  +018 per metre cube
```

---

Scilab code Exa 13.4 Comparison of intrinsic carrier densities of two semiconductors

```
1 // Scilab Code Ex13.4 Comparison of intrinsic
  carrier densities of two semiconductors at room
  temperature Page-433 (2010)
2 eV = 1.6e-019; // Joule equivalent of 1 eV
3 m = 9.1e-031; // Rest mass of an electron , kg
4 m_e = m; // Effective mass of electron , kg
5 m_h = m; // Effective mass of electron , kg
6 Eg_A = 0.36; // Energy gap of A, eV
7 Eg_B = 0.72; // Energy gap of B, eV
8 k = 1.38e-023; // Boltzmann constant , J/mol/K
9 h = 6.626e-034; // Planck's constant , Js
10 k_T = 0.052/2; // Thermal energy , eV
11 // As  $n_i \text{ ratio} = n_{iA}/n_{iB} = \exp(-E_{gA}/(2*k_T))/\exp$ 
  ( $-E_{gA}/(2*k_T)$ )
12 n_i_ratio = exp(-Eg_A/(2*k_T))/exp(-Eg_B/(2*k_T));
  // Intrinsic carrier density ratio of A and B
13 printf("\nThe ratio of intrinsic carrier density =
  %4d ", n_i_ratio);
14 // Result
15 // The ratio of intrinsic carrier density = 1015
```

---

Scilab code Exa 13.5 Shift in fermi level with change in concentration of impurities

```
1 // Scilab Code Ex13.5 Shift in position of fermi
  level with change in concentration of impurities:
  Page-436 (2010)
2 k_T = 0.03; // Thermal energy , eV
3 dE_Fv = 0.4; // Energy difference between fermi
  level and topmost valence level , eV
```

```

4 // The hole concentration in P-type material is
5 //  $p = N_A = N_v \exp(-E_F - E_v) / (k_T) = N_v \exp(-dE_{Fv}) / (k_T)$ 
6 // The new value of hole concentration in P-type
   material is
7 //  $p_{\text{prime}} = 3 * N_A = N_v \exp(-E_{F_{\text{prime}}} - E_v) / (k_T) =$ 
    $N_v \exp(-dE_{F_{\text{prime}}v}) / (k_T)$ 
8 // Solving for  $dE_{F_{\text{prime}}v}$  by removing exponential
   term
9  $dE_{F_{\text{prime}}v} = dE_{Fv} - k_T * \log(3);$  // Energy
   difference between new fermi level and topmost
   valence level, eV
10 printf("\nThe energy difference between new fermi
   level and topmost valence level = %5.3f eV",
   dE_{F_{\text{prime}}v});
11 // Result
12 // The energy difference between new fermi level and
   topmost valence level = 0.367 eV

```

---

### Scilab code Exa 13.6 Electrical resistivity of Ge

```

1 // Scilab Code Ex13.6 Electrical resistivity of Ge:
   Page-439 (2010)
2 e = 1.602e-019; // Charge on an electron, C
3 n_i = 2.37e+019; // Intrinsic carrier density of
   Ge at room temperature, per metre cube
4 mu_e = 0.38; // Mobility of electrons, metre
   square per volt per second
5 mu_h = 0.18; // Mobility of holes, metre square
   per volt per second
6 T = 300; // Room temperature, kelvin
7 sigma_i = n_i * e * (mu_e + mu_h); // Intrinsic
   electrical conductivity, per ohm per metre
8 rho_i = 1/sigma_i; // Intrinsic electrical
   resistivity, ohm-metre

```

```

9 printf("\nThe intrinsic electrical resistivity = %4
    .2f ohm-metre", rho_i);
10 // Result
11 // The intrinsic electrical resistivity = 0.47 ohm-
    metre

```

---

**Scilab code Exa 13.7** Electrical conductivity of intrinsic and extrinsic Si

```

1 // Scilab Code Ex13.7 Electrical conductivity of
    intrinsic and extrinsic Si: Page-439 (2010)
2 NA = 6.023e+23; // Avogadro's number
3 A_Si = 28.09e-03; // Kilogram atomic mass of Si,
    kg
4 e = 1.602e-019; // Charge on an electron, C
5 n_impurity = 1/1e+08; // Donor impurity atoms per
    Si atom
6 n_i = 1.5e+016; // Intrinsic carrier density of
    Si at room temperature, per metre cube
7 mu_e = 0.13; // Mobility of electrons, metre
    square per volt per second
8 mu_h = 0.05; // Mobility of holes, metre square
    per volt per second
9 T = 300; // Room temperature, kelvin
10 sigma_i = n_i*e*(mu_e + mu_h); // Intrinsic
    electrical conductivity, per ohm per metre
11 Si_density = 2.23e+03; // Density of silicon, kg
    per metre cube
12 N_Si = NA * Si_density/A_Si; // Number of Si
    atoms, per metre cube
13 N_D = N_Si*n_impurity; // Density of donor
    impurity, per metre cube;
14 sigma_ext = ceil(N_D)*e*mu_e; // Extrinsic
    electrical conductivity of Si, per ohm per metre
15 printf("\nThe intrinsic electrical conductivity of
    Si = %5.3e per ohm per metre", sigma_i);

```

```

16 printf("\nThe extrinsic electrical conductivity of
    Si = %4.1f per ohm per metre", sigma_ext);
17 // Result
18 // The intrinsic electrical conductivity of Si =
    4.325e-004 per ohm per metre
19 // The extrinsic electrical conductivity of Si =
    10.0 per ohm per metre

```

---

### Scilab code Exa 13.8 Resistance of intrinsic Ge Rod

```

1 // Scilab Code Ex13.8 Resistance of intrinsic Ge Rod
  : Page-440 (2010)
2 e = 1.602e-019; // Charge on an electron, C
3 T = 300; // Room temperature, kelvin
4 l = 1e-02; // Length of the Ge rod, m
5 b = 1e-03; // Width of the Ge rod, m
6 t = 1e-03; // Thickness of the Ge rod, m
7 n_i = 2.5e+019; // Intrinsic carrier density of
  Ge, per metre cube
8 mu_e = 0.39; // Mobility of electrons, metre
  square per volt per second
9 mu_h = 0.19; // Mobility of holes, metre square
  per volt per second
10 sigma_i = n_i*e*(mu_e + mu_h); // Intrinsic
  electrical conductivity, per ohm per metre
11 A = b*t; // Surface area of the Ge rod, metre
  square
12 rho = 1/sigma_i; // Electrical resistivity of Ge
  Rod, ohm-metre
13 R = rho*l/A; // Resistance of Ge Rod, ohm
14 printf("\nThe resistance of Ge Rod = %3.1e ohm", R);
15 // Result
16 // The resistance of Ge Rod = 4.3e+003 ohm

```

---

### Scilab code Exa 13.9 Hall effect in Si semiconductor

```
1 // Scilab Code Ex13.9 Hall effect in Si
   semiconductor: Page-442 (2010)
2 e = 1.602e-019; // Charge on an electron, C
3 T = 300; // Room temperature, kelvin
4 R_H = -7.35e-05; // Hall coefficient of Si
   specimen, metre cube per coulomb
5 sigma = 200; // Electrical conductivity of Si,
   per ohm per metre
6 n = -1/(e*R_H); // Electron density in the Si
   specimen
7 mu_e = sigma/(n*e); // Electron mobility in the
   Si specimen, metre cube per volt per second
8 printf("\nThe density of electron = %3.1e metre cube
   ", n);
9 printf("\nThe mobility of electron = %4.2e metre
   cube per volt per second", mu_e);
10 // Result
11 // The density of electron = 8.5e+022 metre cube
12 // The mobility of electron = 1.47e-002 metre cube
   per volt per second
```

---

### Scilab code Exa 13.10 Forward current of a pn diode using diode equation

```
1 // Scilab Code Ex13.10 Forward current of a p-n
   diode in terms of reverse saturation current
   using diode equation: Page-450 (2010)
2 e = 1.6e-019; // Charge on an electron, coulomb
3 k = 1.38e-023; // Boltzmann constant, J/mol/K
4 V = 0.35; // Potential difference applied across
   a Ge diode, volt
```



```

5 T = 300;      // Room temperature , kelvin
6 Io = 1;      // Reverse saturation current , micro-
               // ampere, for simplicity assume I0 = 1
7 Iv = Io*(exp(e*V/(k*T))-1);    // "Diode Equation"
               // for net forward current , milliamperes
8 printf("\nThe net forward current = %4.2e Io", Iv);
9 // Result
10 // The net forward current = 7.49e+005 Io

```

---

**Scilab code Exa 13.11 Voltage from net forward current using Diode Equation**

```

1 // Scilab Code Ex13.11 Finding voltage from net
  // forward current using Diode Equation: Page-450
  // (2010)
2 e = 1.6e-019; // Charge on an electron , coulomb
3 k = 1.38e-023; // Boltzmann constant , J/mol/K
4 T = 300;      // Room temperature , kelvin
5 Io = 1;      // Reverse saturation current , micro-
               // ampere, for simplicity assume I0 = 1
6 Iv = 0.9*Io; // "Diode Equation" for net forward
               // current , milliamperes
7 // As Iv = Io*(exp(e*V/(k*T))-1), solving for V
8 V = log(Iv/Io+1)*k*T/e; // Potential difference
               // applied across p-n junction , volt
9 printf("\nThe potential difference applied across p-
  // n junction = %6.4f volt", V);
10 // Result
11 // The potential difference applied across p-n
  // junction = 0.0166 volt

```

---

# Chapter 14

## Dielectric Properties of Materials

Scilab code Exa 14.1 Polarization of water molecule

```
1 // Scilab Code Ex14.1 Polarization of water molecule
   : Page-456 (2010)
2 NA = 6.023e+23; // Avogadro's number
3 p = 6e-030; // Dipole moment of water molecule, C
   -m
4 r = 1e-03; // Radius of water molecule, m
5 M = 18e-03; // Molecular weight of water, kg
6 d = 1e+03; // Density of water, kg per metre cube
7 V = M/d; // Volume of water, metre cube
8 // Now M/d metre cube volume will contain NA = 6.023
   e+023 water molecules, so that 4*pi/3*(r^3)
   metre cube volume will contain
9 N = NA*d*4*pi*r^3/(M*3); // Number of water
   molecules per metre cube
10 P = N*p; // Polarization of water molecules,
   coulomb per metre square
11 printf("\nThe polarization of water molecules = %3.1
   e coulomb per metre square", P);
12 // Result
```

```
13 // The polarization of water molecules = 8.4e-010
    coulomb per metre square
```

---

**Scilab code Exa 14.2** Dielectric constant from electric polarizability of the atom

```
1 // Scilab Code Ex14.2 Calculating dielectric
    constant from electric polarizability of the atom
    : Page-464 (2010)
2 alpha_Kr = 2.18e-040; // Electric polarizability
    of the Kr-atom, farad-metre square
3 NA = 6.023e+023; // Avogadro's number
4 epsilon_0 = 8.85e-012; // Electrical permittivity
    of free space, coulomb square per newton per
    metre square
5 N = NA/(22.4e-03); // Number of Kr atoms per
    metre cube
6 epsilon_r = N*alpha_Kr/epsilon_0 + 1; // Relative
    electrical permittivity of Kr specimen
7 printf("\nThe dielectric constant of Kr specimen = %7
    .5f", epsilon_r);
8 // Result
9 // The dielectric constant of Kr specimen = 1.00066
```

---

**Scilab code Exa 14.3** Electric polarizability of a molecule from its susceptibility

```
1 // Scilab Code Ex14.3 Calculating electric
    polarizability of a molecule from its
    susceptibility: Page-464 (2010)
2 NA = 6.023e+023; // Avogadro's number
3 epsilon_0 = 8.85e-012; // Electrical permittivity
    of free space, coulomb square per newton per
    metre
```

```

4 chi = 0.985e-03;    // Electrical susceptibility of
   carbon-dioxide molecule
5 rho = 1.977;      // Density of carbon-dioxide , kg per
   metre cube
6 M = 44e-03;      // Molecular weight of CO2, kg
7 N = NA*rho/M;    // Number of molecules per unit
   volume, per metre cube
8 alpha = epsilon_0*chi/N;    // Total electric
   polarizability of carbon-dioxide , farad-metre
   square
9 printf("\n\nThe total electric polarizability of
   carbon-dioxide = %4.2e farad-metre square", alpha
   );
10 // Result
11 // The total electric polarizability of carbon-
   dioxide = 3.22e-040 farad-metre square

```

---

#### Scilab code Exa 14.4 Electric polarizability of oxygen atom

```

1 // Scilab Code Ex14.4 Calculating electric
   polarizability of Oxygen atom: Page-465 (2010)
2 e = 1.602e-019;    // Charge on an electron , coulomb
3 p = 0.5e-022;     // Dipole moment of oxygen atom, C-
   m
4 d = 4e-017;      // Distnace of the centre of negative
   charge cloud from the nucleus , m
5 epsilon_0 = 8.85e-012;    // Electrical permittivity
   of free space , coulomb square per newton per
   metre
6 // In equilibrium , Coulomb interaction = Lorentz
   force
7 // i.e.      8*e*E = (8*e)*(8*e)/(4*%pi*epsilon_0*d^2)
8 // Solving for E
9 E = 8*e/(4*%pi*epsilon_0*d^2);    // The strength of
   local electric field , volt per metre

```

```

10 // As  $p = \alpha \cdot E$ , solving for  $\alpha$ 
11 disp(E);
12 alpha = p/E; // Atomic polarizability of oxygen,
    farad-metre square
13 printf("\nThe atomic polarizability of oxygen = %3.1
    e farad-metre square", alpha);
14 // Result
15 // The atomic polarizability of oxygen =  $6.9 \times 10^{-48}$ 
    farad-metre square

```

---

#### Scilab code Exa 14.5 Dipolar polarization of HCl molecule

```

1 // Scilab Code Ex14.5 Dipolar polarization of HCl
    molecule: Page-470 (2010)
2 k = 1.38e-023; // Boltzmann constant, J/mol/K
3 T = 300; // Temperature of the HCl vapour, kelvin
4 N = 1e+027; // Number of HCL molecuels per unit
    volume, per metre cube
5 E = 1e+06; // Electric field strength to which
    the HCL vapour is subjected, volt/m
6 p = 3.46e-030; // The dipole moment of HCl
    molecule, C-m
7 alpha_d = p^2/(3*k*T); // Dipolar polarizability
    of HCl molecule, farad-metre square
8 // As  $P = N \cdot p = N \cdot \alpha_d \cdot E$ 
9 P = N*alpha_d*E; // Orientational or Dipolar
    polarization of HCl molecule, coulomb per metre
    square
10 E_M = p*E; // Magnetic energy stored in the
    dipole-field system, joule
11 E_Th = k*T; // Thermal energy of the HCl molecule
    , joule
12 a = E_M/E_Th; // Ratio of magnetic energy to the
    thermal energy
13 printf("\nThe orientational polarization of

```

```

        molecules in HCl vapour = %4.2e coulomb per metre
        square", P);
14 printf("\nThe ratio of magnetic energy to the
        thermal energy = %f << 1", a);
15 // Result
16 // The orientational polarization of molecules in
        HCl vapour = 9.64e-007 coulomb per metre square
17 // The ratio of magnetic energy to the thermal
        energy = 0.000836 << 1

```

---

#### Scilab code Exa 14.6 Effect of molecular deformation on polarizability

```

1 // Scilab Code Ex14.6 Effect of molecular
        deformation on polarizability: Page-471 (2010)
2 alpha_309 = 2.42e-039; // Polarizability of
        ammonia molecule at 309 K, farad-metre square
3 alpha_448 = 1.74e-039; // Polarizability of
        ammonia molecule at 448 K, farad-metre square
4 k = 1.38e-023; // Boltzmann constant, J/mol/K
5 T1 = 309; // First temperature of the experiment,
        kelvin
6 T2 = 448; // Second temperature of the experiment
        , kelvin
7 // As  $\alpha = \alpha_i + \alpha_d = \alpha_i + p^2/(3*k$ 
         $*T) = \alpha_i + bta/T$ 
8 // where  $bta = p^2/(3*k)$ 
9 // Thus  $\alpha_{309} = \alpha_i + bta/309$  and  $\alpha_{448}$ 
        =  $\alpha_i + bta/448$ 
10 // Solving for bta
11 //  $bta(1/309 - 1/448) = \alpha_{309} - \alpha_{448}$ 
12 bta = poly(0, "bta");
13 bta = roots(bta*(1/309 - 1/448) - alpha_309 +
        alpha_448); // bta =  $p^2/(3*k)$ , farad-kelvin
        metre square
14 // Solving for alpha_i

```

```

15 alpha_i = alpha_309 - bta/309;    // Polarizability
    due to permanent dipole moment, farad-metre
    square
16 // Polarizability due to deformation of molecules =
    bta/T, bta = p^2/(3*k)
17 alpha_d_309 = bta/T1;    // Orientational
    polarizability at 309 K, farad-metre square
18 alpha_d_448 = bta/T2;    // Orientational
    polarizability at 448 K, farad-metre square
19 printf("\nThe polarizability due to permanent dipole
    moment = %4.1e farad-metre square", alpha_i);
20 printf("\nThe orientational polarization of ammonia
    at 309 K = %4.2e farad-metre square", alpha_d_309
    );
21 printf("\nThe orientational polarization of ammonia
    at 448 K = %4.2e farad-metre square", alpha_d_448
    );
22 // Result
23 // The polarizability due to permanent dipole moment
    = 2.3e-040 farad-metre square
24 // The orientational polarization of ammonia at 309
    K = 2.19e-039 farad-metre square
25 // The orientational polarization of ammonia at 448
    K = 1.51e-039 farad-metre square

```

---

# Chapter 15

## Optical Properties of Materials

Scilab code Exa 15.1 Photon count from Planck quantum law

```
1 // Scilab Code Ex15.1 Determining Photon number by
  using Planck quantum law: Page-486 (2010)
2 h = 6.626e-034; // Planck's constant, Js
3 f = 1760e+03; // Frequency of the radio
  transmitter, Hz
4 P = 10e+03; // Power of radio transmitter, W
5 E = h*f; // Energy carried by one photon from
  Planck's law, J
6 N = P/E; // Number of photons emitted per second,
  number per second
7 printf("\nThe number of photons emitted per second =
  %4.2e", N);
8 // Result
9 // The number of photons emitted per second = 8.58e
  +030
```

---

Scilab code Exa 15.2 Incident energy of photon in photoelectric effect



```

1 // Scilab Code Ex15.2 Finding suitable energy for
  Photoelectric Effect from Na metal: Page-486
  (2010)
2 e = 1.602e-019; // Charge on an electron , C
3 h = 6.626e-034; // Planck's constant , Js
4 c = 3.0e+08; // Speed of light in vacuum, m/s
5 W = 2.3*e; // Work function of Na metal, J
6 lambda = 2800e-010; // Wavelength of incident
  light , m
7 f = c/lambda; // Frequency of the incident light ,
  Hz
8 E = h*f; // Energy carried by one photon from
  Planck's law , J
9 printf("\nThe energy carried by each photon of
  radiation = %4.2f eV", E/e);
10 if E > W then
11     printf("\nThe photoelectric effect is possible..
  ");
12 else
13     printf("\nThe photoelectric effect is impossible
  ..");
14 end
15 // Result
16 // The energy carried by each photon of radiation =
  4.43 eV
17 // The photoelectric effect is possible..

```

---

### Scilab code Exa 15.3 photon count for green wavelength of Hg

```

1 // Scilab Code Ex15.3 Finding number of photons for
  green wavelength of Hg: Page-487 (2010)
2 h = 6.626e-034; // Planck's constant , Js
3 c = 3.0e+08; // Speed of light in vacuum, m/s
4 lambda = 496.1e-09; // Wavelength of green light
  of mercury , m

```

```

5 E_total = 1;    // Work done by photons from green
   light , J
6 f = c/lambda;  // Frequency of the green light , Hz
7 E = h*f;      // Energy carried by one photon from
   Planck's law , J
8 N = E_total/E; // Number of photons of green
   light of Hg
9 printf("\nThe number of photons of green light of Hg
   = %3.1e", N);
10 // Result
11 // The number of photons of green light of Hg = 2.5e
   +018

```

---

#### Scilab code Exa 15.4 Photoelectric effect in a photocell

```

1 // Scilab Code Ex15.4 Photoelectric effect in a
   photocell: Page-487 (2010)
2 e = 1.602e-019; // Charge on an electron , C
3 h = 6.626e-034; // Planck's constant , Js
4 c = 3.0e+08;    // Speed of light in vacuum, m/s
5 lambda = 1849e-010; // Wavelength of incident
   light , m
6 V_0 = 2.72;    // Stopping potential for emitted
   electrons , V
7 f = c/lambda; // Frequency of incident radiation
   , Hz
8 E = h*f;      // Energy carried by one photon from
   Planck's law , J
9 T_max = e*V_0; // Maximum kinetic energy of
   electrons , J
10 // We have,  $T_{max} = E - h*f_0 = h*f - W$ 
11 f_0 = poly(0, "f_0"); // Declare f_0 as variable
12 f_0 = roots(T_max - E + h*f_0); // Threshold
   frequency for Cu metal, Hz
13 W = h*f_0/e;  // Work function of Cu metal, eV

```

```

14 printf("\nThe threshold frequency for Cu metal = %4.2
    e Hz", f_0);
15 printf("\nThe work function of Cu metal = %g eV",
    round(W));
16 printf("\nThe maximum kinetic energy of
    photoelectrons = %4.2f eV", T_max/e);
17 // Result
18 // The threshold frequency for Cu metal = 9.65e+014
    Hz
19 // The work function of Cu metal = 4 eV
20 // The maximum kinetic energy of photoelectrons =
    2.72 eV

```

---

**Scilab code Exa 15.5** Energy required to stimulate the emission of Na doublets

```

1 // Scilab Code Ex15.5 Energy required to stimulate
    the emission of Na d-lines: Page-497 (2010)
2 e = 1.6e-019; // Charge on an electron , C
3 h = 6.626e-034; // Planck's constant, Js
4 c = 3.0e+08; // Speed of light in vacuum, m/s
5 lambda_mean = 5893e-010; // Wavelength of
    incident light , m
6 delta_E = h*c/(lambda_mean*e); // The energy of
    the electron which must be transferred to the
    atoms of Na
7 printf("\nThe energy which must be transferred to
    stimulate the emission of Na d-lines = %5.3f eV",
    delta_E);
8 // Result
9 // The energy which must be transferred to stimulate
    the emission of Na d-lines = 2.108 eV

```

---

## Chapter 16

# Magnetic Properties of Materials

Scilab code Exa 16.1 Response of copper to magnetic field

```
1 // Scilab Code Ex16.1 Response of Cu to magnetic
   field: Page-503 (2010)
2 H = 1e+06; // Applied magnetic field in
   copper, A/m
3 chi = -0.8e-05; // Magnetic susceptibility of
   copper
4 mu_0 = 4*pi*1e-07; // Magnetic permeability of
   free space, henry/metre
5 M = chi*H; // Intesity of magnetization in copper
   , A/m
6 B = mu_0*(H + M); // Magnetic flux density in
   copper, tesla
7 printf("\nThe magnetization of copper = %d A/m", M);
8 printf("\nThe magnetic flux density of copper = %5.3
   f T", B);
9 // Result
10 // The magnetization of copper = -8 A/m
11 // The magnetic flux density of copper = 1.257 T
```

---

**Scilab code Exa 16.2** Diamagnetic susceptibility of copper

```
1 // Scilab Code Ex16.2 Diamagnetic susceptibility of
  copper: Page-512 (2010)
2 e = 1.6e-019; // Charge on an electron , C
3 m = 9.1e-031; // Mass of an electron , kg
4 mu_0 = 4*pi*1e-07; // Magnetic permeability of
  free space , henry/metre
5 Z = 1; // Number of electrons contributing to the
  magnetic moment
6 r = 1e-010; // Radius of copper atom, m
7 a = 3.608e-010; // Lattice parameter of copper , m
8 // For FCC lattice of Cu, there are 4 atoms per unit
  cell
9 n = 4; // Number of atoms per unit cell
10 N = n/a^3; // Number of electrons per unit volume
  , per metre cube
11 chi_dia = -mu_0*Z*e^2*N*r^2/(6*m); // Diamagnetic
  susceptibility of copper
12 printf("\nThe diamagnetic susceptibility of copper =
  %3.1e", chi_dia);
13 // Result
14 // The diamagnetic susceptibility of copper = -5.0e
  -006
```

---

**Scilab code Exa 16.3** Magnetic induction from orientational energy equivalent of thermal energy

```
1 // Scilab Code Ex16.3 Calculating magnetic induction
  from orientational energy equivalent of thermal
  energy: Page-514 (2010)
2 k = 1.38e-023; // Boltzmann constant , joule per
  mole per kelvin
```

```

3 mu_B = 9.27e-024;    // Bohr's magneton, joule per
    tesla
4 mu_m = 5*mu_B;      // Magnetic moment of
    paramagnetic sample, joule per tesla
5 T = 300;           // Thermal energy of specimen, joule
6 // At equilibrium, mu_m*B = k*T, solving for B
7 B = k*T/mu_m;     // Magentic induction of
    paramagnetic sample, weber per metre square
8 printf("\nThe magentic induction of paramagnetic
    sample = %5.2f weber per metre square", B);
9 // Result
10 // The magentic induction of paramagnetic sample =
    89.32 weber per metre square

```

---

Scilab code Exa 16.4 Behaviour of paramagnetic salt when placed in uniform magnetic field

```

1 // Scilab Code Ex16.4 Behaviour of paramagnetic salt
    when placed in uniform magnetic field: Page-514
    (2010)
2 k = 1.38e-023;     // Boltzmann constant, joule per
    mole per kelvin
3 T = 300;          // Thermal energy of specimen, joule
4 mu_B = 9.27e-024; // Bohr's magneton, ampere per
    metre square
5 mu_0 = 4*pi*1e-07; // Magnetic permeability of
    free space, henry per metre
6 N = 1e+28;        // Concentration of paramagnetic ions
    in paramagnetic salt, per metre cube
7 mu_m = mu_B;
8 H = 1e+06;        // Applied magnetic field, A/m
9 chi = mu_0*N*mu_m^2/(3*k*T); // Paramagnetic
    susceptibility of salt at room temperature
10 M = chi*H;       // Intensity of magnetization at room
    temperature, A/m
11 printf("\nThe paramagnetic susceptibility of salt at

```

```
    room temperature = %3.1e", chi);
12 printf("\nThe intensity of magnetization of salt =
    %d A/m", round(M));
13 // Result
14 // The paramagnetic susceptibility of salt at room
    temperature = 8.7e-005
15 // The intensity of magnetization of salt = 87 A/m
```

---

# Chapter 17

## Superconductivity

Scilab code Exa 17.1 Variation of critical magnetic field with temperature

```
1 // Scilab Code Ex17.1 Variation of critical magnetic
   field with temperature Page-537 (2010)
2 T_c = 3.7; // Critical temperature of
   superconducting transition , kelvin
3 H_c0 = 0.0306; // Critical magnetic field to
   destroy superconductivity , tesla
4 T = 2; // Temperature at which critical magnetic
   field is to be found out, kelvin
5 H_cT = H_c0*(1-(T/T_c)^2);
6 printf("\nThe critical magnetic field at %d K = %f T
   ", T, H_cT);
7 // Result
8 // The critical magnetic field at 2 K = 0.021659 T
```

---

Scilab code Exa 17.2 Temperature variation of critical magnetic field for tin

```
1 // Scilab Code Ex17.2 Variation of critical magnetic
   field with temperature for tin Page-537 (2010)
```



```

2 T_c = 3.69; // Critical temperature of
  superconducting transition , kelvin
3 B_c0 = 3e+5/(4*pi); // Critical magnetic field
  intensity to destroy superconductivity at zero
  kelvin , tesla
4 B_cT = 2e+5/(4*pi); // Critical magnetic field
  at temperature T kelvin
5 // T = 2; // Temperature at which critical
  magnetic field is to be found out, kelvin
6 // since B_cT = B_c0*(1-(T/T_c)^2); // Critical
  magnetic field intensity as a function of
  temperature
7 // Solving for T
8 T = sqrt(1-B_cT/B_c0)*T_c; // Temperature at
  which critical magnetic field becomes B_cT,
  kelvin
9 printf("\nThe temperature at which critical magnetic
  field becomes %4.2e T = %4.2f K",B_cT,T); //
  Display result
10 // Result
11 // The temperature at which critical magnetic field
  becomes 1.59e+04 T = 2.13 K

```

---

**Scilab code Exa 17.3** Critical current for a lead wire from its critical temperature

```

1 // Scilab Code Ex17.3 Calculating critical current
  for a lead wire from critical temperature of lead
  Page-537 (2010)
2 T_c = 7.18; // Critical temperature of
  superconducting transition for Pb, kelvin
3 H_c0 = 6.5e+4; // Critical magnetic field
  intensity to destroy superconductivity at zero
  kelvin , A/m
4 T = 4.2; // Temperature at which critical
  magnetic field becomes H_cT, kelvin

```

```

5 d = 1e-03; // Diameter of lead wire, m
6 H_cT = H_c0*(1-(T/T_c)^2); // Critical magnetic
  field intensity at temperature T kelvin, A/m
7 I_c = %pi*d*H_cT; // Critical current through the
  lead wire, A
8 printf("\nThe critical current through the lead wire
  = %6.2f A", I_c);
9
10 // Result
11 // The critical current through the lead wire =
  134.33 A

```

---

**Scilab code Exa 17.4** Dependence of London penetration depth on temperature

```

1 // Scilab Code Ex17.4 Dependence of London
  penetration depth on temperature Page-548 (2010)
2 N = 6.02e+023; // Avogadro's number
3 rho = 13.55e+03; // Density of mercury, kg per
  metre cube
4 M = 200.6e-03; // Molecular mass of mercury, kg
5 lambda_T = 750e-010; // Penetration depth of
  mercury at T kelvin, m
6 T_c = 4.12; // Critical temperature of
  superconducting transition for Hg, kelvin
7 T = 3.5; // Temperature at which penetration
  depth for Hg becomes lambda_T, kelvin
8 lambda_0 = lambda_T*(1-(T/T_c)^4)^(1/2); //
  Penetration depth of mercury at 0 kelvin, m
9 n_0 = N*rho/M; // Normal electron density in
  mercury, per metre cube
10 n_s = n_0*(1-(T/T_c)^4); // Superelectron density
  in mercury, per metre cube
11 printf("\nThe penetration depth at 0 K = %4.2e m",
  lambda_0);
12 printf("\nThe superconducting electron density = %4

```

```
    .2e per metre cube", n_s);  
13  
14 // Result  
15 // The penetration depth at 0 K = 5.19e-008 m  
16 // The superconducting electron density = 1.95e+028  
    per metre cube
```

---