Scilab Textbook Companion for Discrete Mathematics by S. Lipschutz, M. Lipson And V. H. Patil¹

Created by Neerja Bahuguna B.Tech. (pursuing) Computer Engineering Echelon Institute of Technology, Faridabad College Teacher Prashant Gupta, E. I. T. ,Faridabad Cross-Checked by Prashant Dave, IIT Bombay

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Book Description

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Scilab numbering policy used in this document and the relation to the above book.

Exa Example (Solved example)

Eqn Equation (Particular equation of the above book)

AP Appendix to Example(Scilab Code that is an Appednix to a particular Example of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means a scilab code whose theory is explained in Section 2.3 of the book.

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Chapter 1

Set Theory

Scilab code Exa 1.8 inclusion exclusion principle

- 1 disp('To find:number of mathematics students taking atleast one of the languages French(F),German(G) and Russian(R)')
- 2 F=65; //number of students studying French
- 3 G=45; // number of students studying German
- 4 R=42; //number of students studying Russian
- 5 FandG=20; //number of students studying French and German
- 6 FandR=25; //number of students studying French and Russian
- 7 GandR=15; //number of students studying German and Russian
- 8 FandGandR=8; //number of students studying French, German and Russian

```
9 //By inclusion-exclusion principle
```

- 10 ForGorR=F+G+R-FandG-FandR-GandR+FandGandR;

Scilab code Exa 1.9 Inclusion exclusion principle

1 disp('In a college, 120 mathematics students can opt for either French(F), German(G) or Russian(R)') 2 n=120; //total number of students 3 F=65; //number of students studying French 4 G=45; //number of students studying German 5 R=42; //number of students studying Russian //number of students studying French and $6 \quad \text{FandG}=20:$ German 7 FandR=25; //number of students studying French and Russian 8 GandR=15; //number of students studying German and Russian 9 FandGandR=8; //number of students studying French, German and Russian 10 **disp**('using inclusion - exclusion principle:') 11 ForGorR=F+G+R-FandG-FandR-GandR+FandGandR; 12 disp(ForGorR, 'number of students studying French or German or Russian') 13 FGnR=FandG-FandGandR; 14 disp(FGnR, 'number of students studying French and German but not Russian') 15 FRnG=FandR-FandGandR ; 16 disp(FRnG, 'number of students studying French and Russian but not German') 17 GRnF=GandR-FandGandR ; 18 disp(GRnF, 'number of students studying German and Russian but not French') 19 OF=F-FGnR-FandGandR-FRnG ; 20 disp(OF, 'number of students studying Only French') 21 OG=G-FGnR-FandGandR-GRnF; 22 disp(OG, 'number of students studying Only German') 23 OR=R-FRnG-FandGandR-GRnF; 24 disp(OR, 'number of students studying Only Russian') 25 k=n-ForGorR; 26 disp(k, 'number of students not studying any of the languages ')

Scilab code Exa 1.13 Power sets

```
1 x=10; //number of members of set X
2 P=2^x //number of members of the power set of X
3 q=P-1; //x itself is not the proper subset. Hence it
    isn't counted
4 disp(q, 'number of members of powerset P which are
    proper subsets of x are:')
```

Scilab code Exa 1.14 Power sets

```
1 A=[1,2,3,4,5]; //eatables for salad preparation 1=
    onion,2=tomato,3=carrot,4=cabbage,5=cucumber
2 p=length(A); //total number of eatables available
3 n=2^p-1; //no salad can be made without atleast one
    of the eatables.Hence null set isn't counted
4 disp(n,'number of different salads that can be
    prepared using the given eatables')
```

Scilab code Exa 1.18 Mathematical induction

```
1 U1=1; //given
2 U2=5; //given
3 P=[];
4 for i=1:2
5 P(i)=3^i-2^i;
6 disp(P(i))
7 end
8 disp('P(1)=U(1) and P(2)=U(2)');
```

9 disp('hence $Un=3^n-2^n$ for all n belonging to N');

Chapter 3

Functions and Algorithms

Scilab code Exa 3.8 Recursively defined functions

```
1 function[k]=fact(a)
2 k = -1;
3 if(a<0|a>200)
4 disp("Invalid");
5 break;
6 else
7 if(a==1|a==0)
8 k=1;
9 else
10 k=a*fact(a-1);
11 end
12 \text{ end}
13 endfunction
14 a=4;
15 p=fact(a);
16 disp(p,'the value of 4! is')
```

Scilab code Exa 3.9 Cardinality

```
1 x=1;
2 y = 2;
3 z=3;
4 A = [x, y, z];
5 disp('cardinality of set A is:')
6 \text{ length}(A)
7 B=[1,3,5,7,9]
8 disp('cardinality of set B is:')
9 length(B)
10
11 // 3.9 (b)
12 disp('the set E has the following elements)
13 E = [2, 4, 6 \% inf] //set E is the set of all positive
      even numbers and N is the set of all natural
      numbers
14 \operatorname{disp}(\operatorname{inction} f: \mathbb{N} \text{ to } E \text{ is defined}. So, E \text{ has the same}
        cardinality as N')
15 disp('set E is countably infinite:')
16 for x=2:2:%inf
17 y = 2 * x;
18 disp(y)
19 end
```

Scilab code Exa 3.10 Polynomial evaluation

```
1 x = poly(0, 'x');
2 p = 2*x^3-7*x^2+4*x-15;
3 disp(p, 'the polynomial is')
4 k=horner(p,5);
5 disp(k, 'value of the polynomial at x=5 is')
```

Scilab code Exa 3.11 Greatest Common Divisor

Chapter 5

Vectors and Matrices

Scilab code Exa 5.2 Vector operations

```
1 u=[2,3,-4];
2 v=[1,-5,8];
3 u+v
4 5*u
5 -v
6 2*u-3*v
7 u.*v;
8 k=sum(u.*v);
9 disp(k,'dot product of the two vectors')
10 l=norm(u);
11 disp(l,'norm or length of the vector u')
```

Scilab code Exa 5.3 Column vectors

```
1 u=[5,3,-4]'
2 v=[3,-1,-2]'
3 2*u-3*v
4 k=sum(u.*v);
```

Scilab code Exa 5.5 Matrix addition and Scalar multiplication

Scilab code Exa 5.6 Matrix multiplication

```
1 a=[7,-4,5];
2 b=[3,2,-1]';
3 k=a*b;
4 disp(k,'product of a and b is;')
5 p=[6,-1,8,3];
6 q=[4,-9,-2,5]';
7 l=p*q;
8 disp(l,'product of p and q is:')
```

Scilab code Exa 5.7 Matrix multiplication

Scilab code Exa 5.8 Algebra of square matrices

```
1 A=[1 2;3 -4];
2 A2=A*A //multiplying A by itself
3 A3=A2*A
4 f=2*A2-3*A+5;
5 disp(f, 'for the function f(x)=2x^2-3x+5,f(A) is:')
6 g=A2+3*A-10;
7 disp(g, 'for the function g(x)=x^2+3x-10,g(A) is')
```

Scilab code Exa 5.9 Invertible matrices

Scilab code Exa 5.10 Determinants

```
1 A=[5 4;2 3];
2 det(A);
3 disp(det(A), 'determinant of A')
4 B=[2 1;-4 6]
5 det(B);
6 disp(det(B), 'determinant of B')
7 C=[2 1 3;4 6 -1;5 1 0]
8 disp(det(C), 'determinant of C')
```

Scilab code Exa 5.13 Matrix solution of a system of linear equations

```
1 A=[1 2 1;2 5 -1;3 -2 -1]; //left hand side of
the system of equations
2 B=[3 -4 5]'; //right hand side or
the constants in the equations
3 X=[];
4 X=A\B; //unique solution for the system of
equations
5 x=X(1)
6 y=X(2)
7 z=X(3)
```

Scilab code Exa 5.14 Inverse of a square matrix

```
1 A=[1 0 2;2 -1 3;4 1 8];
2 P=rref([A,eye(3,3)]);
3 disp(P,'canonical form of matrix A :')
4 disp('left side of the matrix P is the identity
matrix so the right side is the inverse of A')
5 inverseA=P(:,4:6)
```

Chapter 6

Counting

Scilab code Exa 6.1 Sum rule principle

```
1 M=8;
           //number of male professors teaching
      calculus
           //number of female professors teaching
2 F=5;
      calculus
3 T=M+F;
4 disp(T, 'number of ways a student can choose a
      calculus professor')
5
                  //event of choosing a prime number
6 \quad E = [2, 3, 5, 7];
     less than 10
                  //event of choosing an even number
7 F = [2, 4, 6, 8];
     less than 10
8 G=intersect(E,F); //event of getting an even and
     prime number
9 H=length(E)+length(F)-length(G);
10 disp(H, 'event of getting an even or a prime number')
11
12 E=[11,13,17,19]; //event of choosing a prime number
     between 10 and 20
13 F=[12,14,16,18]; //event of choosing an even number
      between 10 and 20
```

```
14 G=union(E,F); //event of choosing a number which
is prime or even
15 k=length(G);
16 disp(k, 'number of ways of choosing a number which is
prime or even')
```

Scilab code Exa 6.2 Product rule principle

```
1 disp('a license plate contains two letters followed
     by three digits where first digit can not be zero
     ')
2 n=26; //number of english letters
3 n*n; //number of ways of choosing two letters in
     the license plate
4 p=10; //number of digits (0-9)
5 (p-1)*p*p; //number of ways to select the three
     digits with the first digit not being zero
6 k=n*n*(p-1)*p*p;
7 disp(k, 'total number of license plates that can be
     printed ')
9 disp('a president, a secretary and a treasurer has
     to be elected in an orga-nisation of 26 members.
     No person is elected to more than one postion')
10 t=26; //total number of members in the organisation
11 j=t*(t-1)*(t-2);
12 disp(j, 'number of ways to elect the three officers (
     president , secretary , treasurer ')
```

Scilab code Exa 6.3 Factorial notation

```
1 disp('To find: factorial of a 6')
2 facto2=2*1;
```

```
3 facto3=3*facto2
4 facto4=3*facto3
5 facto4=4*facto3
6 facto5=5*facto4
7 facto6=6*facto5
8
9 k=8*7*factorial(6)/factorial(6);
10 disp(k, 'value of 8!/6! is:')
11 j=12*11*10*factorial(9)/factorial(9);
12 disp(j, 'value of 12!/9! is:')
```

Scilab code Exa 6.4 Binomial coefficients

```
1 function [k]=func1(n,r) //calculating binomial
      coefficient
2 k=factorial(n)/(factorial(r)*factorial(n-r));
3 endfunction
4 func1(8,2)
5 \, func1(9,4)
6 \, \text{funcl}(12,5)
7 \, \text{funcl}(10,3)
8 func1(13,1)
9
10 p = factorial(10)/(factorial(10-7)*factorial(7));
     //calculating 10C7
11 q= factorial(10)/(factorial(10-3)*factorial(3)) //
      calculating 10C3
12 disp(p,'value of 10C7 is')
13 / 10-7=3 so 10C7 can also be computed as 10C3
14 //both p and q have same values but second method
      saves time and space
```

Scilab code Exa 6.5 Permutations

- 2 n=6; //total number of letters
- 3 l1=n; //number of ways in which first letter of the word can be chosen
- 4 12=n-1; //number of ways in which second letter of the word can be chosen
- 5 13= n-2; //number of ways in which third letter can be chosen
- 6 k=11*12*13;
- 7 disp(k, 'number of three-letter words possible')

Scilab code Exa 6.6 Permutations with repetitions

```
1 function [k]= funct1(n,p,q)
2 k= factorial(n)/(factorial(p)*factorial(q));
3 endfunction
4 k=funct1(7,3,2) //in "BENZENE" three letters are
        alike(the three Es) and two are alike (the two Ns
        )
5 disp(k, 'The number of seven-letter words that can be
        formed using letters of the word BENZENE')
6
7 disp('a set of 4 indistinguishable red coloured
        flags, 3 indistinguishable white flags and a blue
        flag is given')
8 j=funct1(8,4,3);
9 disp(j, 'number of different signals ,each consisting
        of eight flags')
```

Scilab code Exa 6.7 Combinations

Scilab code Exa 6.8 Combinations

```
1 function [k] = myfunc(n,r)
2 k=factorial(n)/(factorial(n-r)*factorial(r));
3 endfunction
4 k=myfunc(8,3);
5 disp(k, 'the number of committees of three that can
     be formed out of eight people')
6
7 cows=myfunc(6,3) //number of ways that a farmer can
      choose 3 cows out of 6 cows
8 pigs=myfunc(5,2) //number of ways that a farmer can
      choose 2 pigs out of 5 pigs
9 hens=myfunc(8,4) //number of ways that a farmer can
      choose 4 hens out of 8 hens
10 p=cows*pigs*hens;
11 disp(p, 'total number of ways that a farmer can
     choose all these animals')
```

Scilab code Exa 6.9 Combinations with repetitions

```
4 m=factorial(r+(M-1))/(factorial(r+(M-1)-(M-1))*
factorial(M-1));
```

Scilab code Exa 6.14 Ordered partitions

- 1 c1=3; //number of toys that the youngest child
 should get
- 2 c2=2; //number of toys that the third child should get
- 3 c3=2; //number of toys that the second child should get
- 4 c4=2; //number of toys that the eldest son should get
- 5 m=factorial(9)/(factorial(3)*factorial(2)*factorial (2)*factorial(2));
- 6 disp(m, 'number of ways nine toys can be divided between four children with the youngest son getting 3 toys and others getting 2 each ')

Scilab code Exa 6.15 Unordered partitions

```
5 m=r/factorial(t); //number of unordered partitions
6 disp(m, 'number of ways that 12 students can be
        partitioned into three teams so that each team
        consists of 4 students')
```

```
Scilab code Exa 6.16 Inclusion exclusion principle revisited
```

- 1 U=1000; //number of elements in the set of positive integers not exceeding 1000
- 2 A=U/3; //number of elements in the subset of integers divisible by 3
- 3 B=U/5; //number of elements in the subset of integers divisible by 5
- 4 C=U/7; //number of elements in the subset of integers divisible by 7
- 5 AandB=floor(U/(3*5)) //number of elements in the subset containing numbers divisible by both 3 and 5
- 6 AandC=floor(U/(3*7)) //number of elements in the subset containing numbers divisible by both 3 and 7
- 7 BandC=floor(U/(5*7)) //number of elements in the subset containing numbers divisible by both 5 and 7
- 8 AandBandC=floor(U/(3*5*7)) //number of elements in the subset containing numbers divisible by 3,5 and 7
- 9 s=U-(A+B+C)+(AandB+AandC+BandC)-(AandBandC); // By inclusion-exclusion principle

```
10 S=round(s);
```

11 disp(S, 'The number of integers in the set U, which are not divisible by 3,5 and 7 is ')

Chapter 7

Probability Theory

Scilab code Exa 7.1 Sample space and events

1	1 S=[1,2,3,4,5,6]; //s	ample space for the	
	rolling of a die		
2		event that an even number	
	occurs		
3	3 B=[1,3,5]; //ev	rent that an odd number	
	occurs		
4	4 C=[2,3,5]; $//eve$	ent that a prime number	
	occurs		
5	5 <pre>disp(union(A,C),'sample sp</pre>	ace for the event that an	
	even or a prime number	occurs ')	
6	<pre>disp(intersect(B,C), 'sample space for the event that</pre>		
	an odd prime number oc	curs')	
7	disp(setdiff(S,C), 'sample space for the event that a		
	prime number does not	occur') //It is the	
	complement of the set C	•	
8	8 intersect(A,B) //It is	a null set or null vector	
	since there can't occu	r an even and an odd	
	number simultaneously		
9	•		
10	0 H=0; //"head"	face of a coin	

11 T=1; //"tail" face of a coin

- 12 S=["000","001","010","011","100","101","110","111"]
 ; //sample space for the toss of a coin three
 times
- 13 A=["000","001","100"]; //event that two more or more heads appear consecutively
- 14 B=["000","111"]; //event that all tosses are the same
- 15 disp(intersect(A,B), 'sample space for the event in which only heads appear')
- 16
- 17 disp('Experiment:tossing a coin until a head appears and then counting the number of times the coin is tossed')
- 18 S=[1,2,3,4,5,%inf] //The sample space has infinite elements in it
- 19 disp("Since every positive integer is an element of S, the sample space is infinite")

Scilab code Exa 7.2 Finite probability spaces

- 2 S=[0,1,2,3]; //the sample space for the experiment where 0 implies no heads,1 implies only one head out of the three coins and so on
- 3 disp("the probability space is as follows ")
- 4 PO=1/8; //probability of getting no head on any of the coins i.e TTT
- 5 P1=3/8; //probability of getting only one head on any of the coins, out of the three coins i.e HTT, THT,TTH
- 6 P2=3/8; //probability of getting two heads, out of the three coins i.e THH, HTH, HHT
- 7 P3=1/8; //probability of getting all the three heads i.e HHH

```
8 disp("A is the event that atleast one head appears
and B is the event that all heads or all tails
appear ")
9 A=[1,2,3]; // HHH,HHT,HTH,HTT,THH,THT,TTH
10 B=[0,3]; //HHH,TTT
11 PA=P1+P2+P3;
12 disp(PA, 'probability of occurrence of event A')
13 PB=P0+P3;
14 disp(PB, 'probability of occurrence of event B')
```

Scilab code Exa 7.3 Equiprobable spaces

```
1 disp("Experiment: a card is selected from a deck of
     52 cards ")
2 disp("A is the event of the selected card being a
     spade ")
3 disp("B is the event of the selected card being a
     face card ")
               //the total number of cards
4 t=52 ;
5 s=13;
              //number of spades
6 PA= s/t;
7 disp(PA, 'probability of selecting a spade')
            //number of face cards(jack,queen,king)
8 f=12;
9 PB=f/t;
10 disp(PB, 'probability of selecting a face card')
            //number of spade face cards
11 sf=3;
12 Psf=sf/t;
13 disp(Psf," probability of selecting a spade face card
      is:")
```

Scilab code Exa 7.4 Addition principle

1	disp("Experiment: selection of a student out of 100
	students ")
2	M=30; //no of students taking mathematics
3	C=20; //no of students taking chemistry
4	T=100; //total no. of students
5	PM = M/T //probability of the selected student
	taking mathematics
6	PC = C/T //probability of the selected student
	taking chemistry
7	MnC=10; //no of students taking mathematics and
	chemistry
8	PMnC = MnC/T //probability of the selected student
	taking mathematics and chemistry both
9	PMorC = PM+PC-PMnC;
10	disp(PMorC,'probability of the selected student
	taking mathematics or chemistry')

```
Scilab code Exa 7.5 Conditional probability
```

```
1
2
3
  //EXAMPLE 7.5 (a)
4
5
    disp(" Experiment: A die is tossed and the outcomes
6
        are observed");
7
8
9
    disp("To find: probability (PM) of an event that
      one of the dice is 2 if the sum is 6");
10
11
12 E = ["(1,5)","(2,4)","(3,3)","(4,2)","(5,1)"]
     event that the sum of the two numbers on the two
      dice is 6
```

```
14
15 A = ["(2,1)", "(2,2)", "(2,3)", "(2,4)", "(2,5)", "(2,6)", "
      (1,2)","(3,2)","(4,2)","(5,2)","(6,2)"] //event
      that 2 appears on atleast one die
16
17
18 B= intersect(A,E) // possible combination of
      numbers on two die such that their sum is 6 and 2
       appears atleast on one die
19
20
21 PM=2/5 //since E has 5 elements and B has 2
      elements
22
23
24
25
26
27 / EXAMPLE 7.5(b)
28
29 disp("A couple has two children");
30
31
32 b=1; //boy child
33
34 g=2;
        //girl child
35
36 S=[11,12,21,22]; //sample space where 11 implies
       both children being boys, 12 implies first child
      being a boy and the second child being a girl
                                  and so on
37
38 disp("To find: probability(PM) that both children
      are boys ");
39
40
41
```

13

```
42 //7.5(b).i
43
44 L=S(:, 1:3)
                  //reduced sample space if it is known
       that one of the children is a boy
45
46
  PM=1/length(L)
47
48
49
50 //7.5(b).ii
51
                  //reduced sample space if it is known
52 R=S(:,1:2)
      that the older child is a boy
53
54
55 PM=1/length(R)
```

Scilab code Exa 7.6 Multiplication theorem for conditional probability

- 2 s=12; //total itmes in the bag
- 3 d=4; //defective items in the bag

```
4 Pf=(s-d)/s ; //probability that the first item
drawn is non defective
```

```
5 Pe=Pf*[(s-d-1)/(s-1)]*[(s-d-2)/(s-2)];
```

- 6 disp(Pe, 'probability that all three items are non defective')
- 7 //after the first item is chosen, the second item is to be chosen from 1 less than the original number of items in the box and similarly the number of non defective items gets decreased by 1. Similarly , for the third draw of item from the box

Scilab code Exa 7.7 Independent events

```
1 H=1;
          //heads of a coin
2 T=2;
         //tails of the coin
3 S=[111,112,121,122,211,212,221,222] //sample space
      for the toss of a coin three times. 111 implies
     heads all three times, 112 implies heads on first
     two tosses and tails on the third toss
4 A=[111,112,121,122]; //event that first toss is
      heads
  B=[111,112,211,212]; //event that second toss is
5
     heads
6 \quad C = [112, 211];
                         //event that exactly two heads
      appear in a row
7 PA=length(A)/length(S);
8 disp(PA, 'probability of A is ')
9 PB=length(B)/length(S);
10 disp(PB, 'probability of B is ')
11 PC=length(C)/length(S);
12 disp(PC, 'probability of C is ')
13 AnB=intersect(A,B)
14 AnC=intersect(A,C)
15 BnC=intersect(B,C)
16 PAnB= length(AnB)/length(S);
17 disp(PAnB, 'probability of the event AnB')
18 PAnC= length(AnC)/length(S);
19 disp(PAnC, 'probability of the event AnC')
20 PBnC= length(BnC)/length(S);
21 disp(PBnC, 'probability of the event BnC')
22 if ((PA*PB) == PAnB),
   disp("A and B are independent")
23
24 else
25
    disp("A and B are dependent")
26 end
```

```
27 if((PA*PC)==PAnC),
28 disp("A and C are independent")
29 else
30 disp("A and C are dependent")
31 end
32 if((PB*PC)==PBnC),
33 disp("B and C are independent")
34 else
35 disp("B and C are dependent")
36 end
```

Scilab code Exa 7.8 Independent events

```
1 disp("Experiment: A and B both shoot at a target")
2 PA=1/4; //given probability of A hitting the target
3 PB=2/5; //given probability of B hitting the target
4 disp("A and B are independent events so PA*PB will
            be equal to probability of the event of A and B
            both hitting the target i.e PAnB")
5 PAnB=PA*PB;
6 PAorB=PA+PB-PAnB;
7 disp(PAorB, 'probability of atleast one of them
            hitting the target')
```

Scilab code Exa 7.9 Independent repeated trials

```
1 disp("Experiment: Three horses race together twice")
2 Ph1=1/2; //probability of first horse winning the
    race
3 Ph2=1/3; //probability of second horse winning the
    race
4 Ph3=1/6; //probability of third horse winning the
    race
```

- 5 S=[11,12,13,21,22,23,31,32,33] //sample space where 11 implies first horse winning the first and second race both,12 implies first horse winning the first race and second horse winning the second race and so on
- 6 P11=Ph1*Ph1 //probability of first horse winning both races
- 7 P12=Ph1*Ph2 //probability of first horse winning the first race and second horse winning the second race
- 8 P13=Ph1*Ph3 //probability of first horse winning the first race and third horse winning the second race
- 9 P21=Ph2*Ph1 // probability of second horse winning the first race and first horse winning the second race
- 10 P22=Ph2*Ph2 //probability of second horse winning both the races
- 11 P23=Ph2*Ph3 //probability of second horse winning the first race and third horse winning the second race
- 12 P31=Ph3*Ph1 //probability of third horse winning the first race and first horse winning the second race
- 13 P32=Ph3*Ph2 //probability of third horse winning the first race and second horse winning the second race
- 14 P33=Ph3*Ph3 //probability of third horse winning both the races
- 15 disp(P31, 'probability of third horse winning the first race and first horse winning the second race is ')

Scilab code Exa 7.10 Repeated trials with two outcomes

```
//number of times a fair coin is tossed and
1 n=6;
      getting a heads is a success
2 p=1/2; //probability of getting a heads
3 q=1/2 ; //probability of not getting a heads
4 P2=(factorial(6)/(factorial(6-2)*factorial(2)))*p^2*
      q^{(6-2)};
5 disp(P2, 'probability of getting exactly two heads (i
      k = 2)')
6
7 P4=(factorial(6)/(factorial(6-4)*factorial(4)))*p^4*
      q<sup>(6-4)</sup>; //probabilty of getting four heads
8 P5=(factorial(6)/(factorial(6-5)*factorial(5)))*p^5*
      q<sup>(6-5)</sup>; //probabilty of getting five heads
9 P6=(factorial(6)/(factorial(6-6)*factorial(6)))*p^6*
      q<sup>(6-6)</sup>; //probabilty of getting five heads
10 PA = P4 + P5 + P6;
11 disp(PA, 'probability of getting atleast four heads(i
      k = 4, 5 \text{ or } 6) ')
12
13 Pn=q^6
                   //probability of getting no heads
14 Pm=1-Pn;
15 disp(Pm, 'probability of getting one or more heads')
```

Scilab code Exa 7.12 Random variables

- 3 s=factorial(12)/(factorial(12-3)*factorial(3));
- 4 disp(s, 'number of elements in the sample space where samples are of size 3')
- 5 //X denotes the number of defective items in the sample
- 6 x=[0,1,2,3]; //range space of the random variable X

Scilab code Exa 7.13 Probability distribution of a random variable 1 r=[1,2,3,4,5,6,5,4,3,2,1]; 2 //number of outcomes whose sum is 2,3,4,5,6,7,8,9,10,11,12 respectively such that there is only 1 outcome i.e (1,1) whose sum is 2, two outcomes (1,2) and (2,1) whose sum is 3 and so on //total number of 3 t=36;elements in the sample space of the experiment of tossing a pair of dice 4 for i=1:11; 5 p=r(i)/t; $6 \operatorname{disp}(p)$ 7 end8 0.0277778 //probability of getting a sum of 2 //probability of getting a 9 0.0555556 sum of 3 10 0.0833333 //probability of getting a sum of 4 11 0.1111111 //probability of getting a sum of 5 12 0.1388889 //probability of getting a sum of 6 13 0.1666667 //probability of getting a sum of 7 //probability of getting a sum 14 0.1388889 of 8 15 0.1111111 //probability of getting a sum of 9 16 0.0833333 //probability of getting a sum of 10 //probability of getting a sum 17 0.0555556
21 disp(D, 'distribution table of X where first row gives the range space and second row gives the respective probabilities is as follows')

```
Scilab code Exa 7.14 Probability distribution of a random variable
1 disp("a box contains 12 items of which three are
     defective")
2 disp("A sample of three items is selected from the
     box")
3 r=factorial(9)/(factorial(9-3)*factorial(3))
                                                  11
     number of samples of size 3 with no defective
     items
4 t=220;
                                                  //
     number of different samples of size 3 i.e the
     number of elements in the sample space
5 PO=r/t
                                                 //
     probability of getting no defective item
6 r1=3*(factorial(9)/(factorial(9-2)*factorial(2)))
           //number of samples of size 3 getting 1
     defective item
7 P1=r1/t
```

```
//probability of getting 1 defective item
8 r2=9*(factorial(3)/(factorial(3-2)*factorial(2)))
```

```
//number of samples of size 3 getting 2
      defective item
9 P2=r2/t
                                                       11
      probability of getting 2 defective item
10 r3=1:
                               //number of samples of
      size 3 getting 3 defective item
11 P3=r3/t
                              //probability of getting 3
       defective item
12 x = [0, 1, 2, 3];
13 p=[P0,P1,P2,P3];
14 D=[0,1,2,3;P0,P1,P2,P3];
15 disp(D, 'distribution table for random variable X the
       upper row being values of X')
```

```
Scilab code Exa 7.15 Expectation of a random variable
```

```
1 disp("A fair coin is tossed six times");
2 x=[0,1,2,3,4,5,6]; //number of heads which can
     occur
3 p=[1/64,6/64,15/64,20/64,15/64,6/64,1/64]; //
     probability of occurring of heads where 1/64 is
     probability for occurrence of a single head, 6/64
     that of occurrence of two heads and so on.
4 r=0;
5 for i=1:7;
6 r = r + (x(i)*p(i));
7 end
8 disp(r, 'mean or expected number of heads are')
9
10 disp("X is a random variable which gives possible
     number of defective items in a sample of size 3")
11 //Box contains 12 items of which three are defective
12 x=[0,1,2,3]; //possible number of defective items
```

```
in a smaple of size 3
13 p=[84/220,108/220,27/220,1/220]; //probability of
     occurrence of each number in x respectively where
      84/220 is the probability for getting no
     defective item, 108/220 is that of getting 1
      defective item and so on.
14
   r = 0;
15 for i=1:4;
16 r = r + (x(i)*p(i));
17 end
18 disp(r, 'expected number of defective items in a
     sample of size 3 are')
19
               //probability of winning the race by
20 Ph1=1/2;
     first horse
21 Ph2=1/3;
               //probability of winning the race by
     second horse
22 Ph3=1/6;
               //probability of winning the race by
     third horse
23 //X is the payoff function for the winning horse
24 X1=2;
             //X pays $2 as first horse wins the rac
             //X pays $6 as second horse wins the race
25 X2=6;
            //X pays $9 as third horse wins the race
26 X3=9;
27 E=X1*Ph1+X2*Ph2+X3*Ph3;
28 disp(E, 'expected pay off for the race is')
```

Scilab code Exa 7.16 Variance and standard deviation of a random variable

1	u=3;	//mean of	distribution	of random
	variable X			
2	x = [0, 1, 2, 3, 4, 5, 6];	//values	of X in the	
	distribution as :	x where it	is the number	r of times
	heads occurs wh	en a coin É	is tossed six	times
3	p=[1/64,6/64,15/64,	20/64,15/6	4,6/64,1/64];	//
	probabilities of	occurrence	e of each valu	ie of X (x

```
) in the distribution such that 1/64 gives the
     probability of occurrence of no heads at all ,6/64
       gives that of occurrence of heads for only one
     time and so on
4 k = 0;
5 for i=1:7;
6 k=k+((x(i)-u)^2)*p(i);
7 end
8 disp(k, 'Variance of X is')
9 s=sqrt(k);
10 disp(s, 'Standard deviation of X is ')
11
12 u=0.75;
            //mean
13 x = [0, 1, 2, 3];
                //values of random variable X as x in
     the probability distribution of X
14 p=[84/220,108/220,27/220,1/220]; //probability of
     values in x which appear in distribution table of
      Х
15 g=0;
16 for i=1:4;
17 g=g+((x(i))^2)*p(i);
18 end
19 h=g-(u*u);
20 disp(h, 'variance of X is')
21 sd=sqrt(h);
22 disp(sd, 'Standard deviation for X')
```

Scilab code Exa 7.17 Binomial diatribution

1	p=1/5; //probability of the man hitting a target
2	q=1-1/5; //probability of the man not hitting the
	target
3	n=100; //number of times the man fires
4	e=n*p;
5	disp(e, 'expected number of times the man will hit

```
the target')
6 r=sqrt(n*p*q);
7 disp(r, 'Standard deviation')
8
9 p=1/2; //probability of guessing the correct answer
in a five question true-false exam
10 n=5; //number of questions in the exam
11 g=n*p;
12 disp(g, 'expected number of correct answers in the
exam')
```

Scilab code Exa 7.18 Chebyshev inequality

```
//mean of a random variable X
1 u=75;
2 n=5;
            //standard deviation of X
               //for k=2
3 k=2;
4 l1=u-k*n
5 12=u+k*n
6 P1=1-(1/k)^2
7 disp("thus the probability that a value of X lies
     between 65 and 85 is atleast 0.75 according to
     Chebyshev inequality")
                     //for k=3
8 k=3;
9 11=u-k*n
10 12=u+k*n
11 P2=1-(1/k)^2
12 disp("thus the probability that a value of X lies
     between 60 and 90 is atleast 0.8888889 according
     to Chebyshev Inequality")
```

Scilab code Exa 7.19 Sample mean and Law of large numbers

```
1 disp(" a die is tossed 5 times with the following
outcomes")
2 x1=3;
3 x2=4;
4 x3=6;
5 x4=1;
6 x5=4;
7 xmean=(x1+x2+x3+x4+x5)/5 //mean of the outcomes
8 disp('for a fair die the mean is 3.5.So law of large
numbers tells us that as number of outcomes
increase for this experiment, there is a greater
likelihood that themean will get closer to 3.5')
```

Graph Theory

Scilab code Exa 8.1 Paths and connectivity

- 1 // refer to page 8.6
- 2 disp('given a graph with 6 nodes viz. node1, node2 node6')
- 4 disp(A, 'The adjacency matrix for A is ')
- 5 disp('sequence A is a path from node4 to node6; but it is not a trail since the edge from node1 to node2 is used twice')
- 7 disp(B, 'The adjacency matrix for B is ')
- 8 disp('sequence B is not a path since there is no edge from node2 to node6 is used twice')
- 10 disp(C, 'The adjacency matrix for C is ')
- 11 disp('sequence C is a trail since is no edge is used
 twice')

Scilab code Exa 8.2 Minimum spanning tree

```
1 disp('to find: minimal spanning tree')
2 disp('the adjacency matrix for the weighted graph(
     nodeA, nodeB... nodeF) of 6 nodes is : ')
3 K=[0 0 7 0 4 7;0 0 8 3 7 5;7 8 0 0 6 0;0 3 0 0 0 4;4
       7 6 0 0 0;7 5 0 4 0 0]
4 disp('edges of the graph')
5 AC=7;
6 \text{ AE}=4;
7 \text{ AF} = 7;
8 BC=8;
9 BD=3;
10 BE=7;
11 BF=5;
12 CE=6;
13 DF = 4;
14 M=[AC,AE,AF,BC,BD,BE,BF,CE,DF]; //set of all edges
15 V=int32(M);
16 L=gsort(V) //edges sorted in decreasing order of
      their weights
17 disp('deleting edges without disconnecting the graph
       until 5 edges remain')
18 N = [BE, CE, AE, DF, BD];
                        //edges in minimum spanning
      tree
19 Sum = sum(N);
20 disp(Sum, 'weight of the minimal spanning tree is ')
21
22
23 disp('another method of finding a minimal spanning
      tree is :')
```

- 24 K=gsort(V,'g','i') //edges sorted in increasing order
- 25 N2=[BD,AE,DF,CE,AF]; //edges in minimum spanning tree
- 26 Sum2=sum(N2);
- 27 disp(Sum2, 'weight of the minimal spanning tree is ')

Directed graphs

Scilab code Exa 9.6 Adjacency matrix

Scilab code Exa 9.8 Path matrix

```
1 A=[0 0 0 1;1 0 1 1;1 0 0 1;1 0 1 0];
2 disp(A, 'adjacency matrix of graph G is')
3 A4=A^4;
4 A3=A^3;
5 A2=A^2;
6 B4=A+A2+A3+A4;
7 B4=[4 11 7 7 0 0 0 0 3 7 4 4 4 11 7 7];
8 for i=1:16
9 if(B4(i)~=0) then
```

```
10 B4(i)=1;
11 end
12 end
13 disp(B4, 'Replacing non zero entries of B4 with 1 ,we
    get path (reachability) matrix P is:')
14 disp('there are zero entries in P, therefore the
    graph is not strongly connected')
```

Properties of the integers

Scilab code Exa 11.2 Division algorithm

```
1 disp('Division Algorithm')
2 a=4461; //dividend
3 b=16; //divisor
4 r=modulo(a,b) //remainder
5 k=fix(a/b) //quotient
6 j=b*k+r //dividend=divisor*quotient+remainder
7
8 a=-262; //dividend
9 b=3; //divisor
10 k=fix(a/b) //remainder
11 r=modulo(a,b) //quotient
12 j=b*k+r //dividend=divisor*quotient+remainder
13 disp('a and j have equal values.Hence division
algorithm is proved')
```

Scilab code Exa 11.4 Primes

1 disp('Divisibility and Primes')

```
2 x=50;
3 disp('prime numbers less than 50 are')
4 y=primes(x)
5
6 disp('the prime factorisation of 21,24 and 1729
respectively are:')
7 k=factor(21)
8 l=factor(24)
9 n=factor(1729)
```

Scilab code Exa 11.5 Greatest Common Divisor

```
1 disp('the GCD of the following numbers is:')
2 V=int32([12,18]);
3 [thegcd]=gcd(V)
4 V=int32([12,-18]);
5 [thegcd]=gcd(V)
6 V=int32([12,-16]);
7 [thegcd]=gcd(V)
8 V=int32([29,15]);
9 [thegcd]=gcd(V)
10 V=int32([14,49]);
11 [thegcd]=gcd(V)
```

Scilab code Exa 11.6 Euclidean algorithm

```
1 disp('Euclidean Algorithm')
2 a=[540,168,36,24];
3 b=[168,36,24,12];
4 for i=1:4
5 V=int32([a(i),b(i)]);
6 thegcd=[];
7 thegcd(i)=gcd(V);
```

```
8 disp(thegcd(i))
9 end
10
11 function []=myf(dividend,divisor)
12 quotient=floor(dividend/divisor);
13 rem=modulo(dividend,divisor);
14 k=quotient*divisor+rem;
15 disp(k)
16 if (rem\sim=0) then
        myf(divisor,rem)
17
18 end
19 endfunction
20
21 myf(540,168)
22
23 disp('for the equation 540*x+168*y=12, we are given')
24 a=540;
25 b=168;
26 c = 24;
27 d=36;
28 \, d=a-3*b;
                //Eqn(1)
                  //Eqn (2)
29 c=b-4*d;
                //Eqn (3)
30 \ k=d-1*c;
                 //Eqn (4)
31 5*d-1*b;
32 \ k=d-b+4*d;
                   // substituting value of c in Eqn (3)
     from Eqn (2)
33 r=5*a-16*b;
34 if(r==k) then
35
       disp('x=5 and y=16');
36 end
```

Scilab code Exa 11.9 Fundamental theorem of Arithmetic

```
1 a=2<sup>4</sup>*3<sup>3</sup>*7*11*13
2 b=2<sup>3</sup>*3<sup>2</sup>*5<sup>2</sup>*11*17
```

```
3 V=int32([a,b]);
4 [d]=gcd(V)
5 lcm1=2^4*3^3*5^2*7*11*13*17 //lcm is the product
        of those primes which appear in either a or b
```

Scilab code Exa 11.12 Congruence relation

```
1 x=poly(0, 'x');
2 g=3*x^2-7*x+5
3 m=horner(g,2) //value of polynomial at 2
4 n=horner(g,8) //value of polynomial at 8
5 j=m-n
6 disp(n,"for n = ")
7 if(modulo(j,6)==0) then
8 mprintf('%i is congruent to %i(mod 6)',m,n)
9 end
```

Scilab code Exa 11.19 Linear congruence equation

```
14
   disp('k is the unique solution of the equation ')
15
16 for i=0 : m1
17 x=i;
18 p=f(x);
19 if (modulo(p,m1) == 0)
20 k=x
21 break;
22 end
23 end
24
25 \ s1=k;
26 s2=k+m1;
27 s3=k+(m1*2);
28 s4=k+(m1*3);
29 disp('solutions of the original equation at d=4')
30 disp(s1)
31 disp(s2)
32 disp(s3)
33 disp(s4)
```

Algebraic Systems

Scilab code Exa 12.4 Properties of operations

```
1 a = (8-4) - 3
2 b=8-(4-3)
3 disp('since a and b are not equal so subtraction is
      non-commutative on Z(set of integers)')
4
5 a = [1 2; 3 4]
6 b = [5 6; 0 -2]
7 g= a*b
8 k = b * a
9 disp('since g and k are not equal matrix
      multiplication is non-commutative')
10
11 h=(2<sup>2</sup>)<sup>3</sup>
12 j=2^(2^3)
13 disp('since h and j are not equal so exponential
      operation is non associative on the set of
      positive integers N')
```

Scilab code Exa 12.17 Roots of polynomial

```
1 t=poly(0, 't');
2 f=t^3+t^2-8*t+4
3 g=factors(f)
4 disp(r=roots(f), 'roots of f(t) are as follows:')
5
6 t=poly(0, 't');
7 h=t^4-2*t^3+11*t-10
8 disp(r=roots(h), 'the real roots of h(t) are 1 and -2
')
```

Scilab code Exa 12.18 Roots of polynomial

```
1 t=poly(0, 't');
2 f=t^4-3*t^3+6*t^2+25*t-39
3 g=factors(f)
4 disp(r=roots(f), 'roots of f(t) are as follows:')
```

Boolean Algebra

Scilab code Exa 15.1 Basic definitions in boolean algebra

```
1 / 0 denotes False and 1 denotes true
2 b=[0,1];
3 //binary operation + on the set of bits
4 for i=1:2
5 for j=1:2
6 \ k = b(i) \& b(j);
7 \operatorname{disp}(k)
8 end
9 \text{ end}
10 //binary operation * on the set of bits
11 for i=1:2
12 for j=1:2
13 k = b(i) | b(j);
14 disp(k)
15 \text{ end}
16 end
17 //unary operation ' on the set of bits
18 k=~b
19 clear;
20 D=[1,2,5,7,10,14,35,70];
21 a=35;
```

```
22 b=70;
23 V=int32([a,b]);
24 thelcm=lcm(V) //a+b=lcm(a,b)
25 V=int32([a,b])
26 thegcd=gcd(V) //a*b=gcd(a,b)
27 abar=70/a //a'=70/a
```

Scilab code Exa 15.2 Boolean algebra as lattices

```
1 D=[1,2,5,7,10,14,35,70];
2 a = 2; //a and b belong to D
3 b = 14;
4 V=int32([a,b]);
5 thelcm=lcm(V)
6 V=int32([a,b]);
7 thegcd=gcd(V)
8 abar=70/a
9 bbar=70/b
10 j=[abar,b];
11 h=[a,bbar];
12 V=int32([j])
13 lcm1=lcm(V)
14 K=int32([h])
15 lcm2=lcm(K)
```

Recurrence relations

Scilab code Exa 16.14 Linear homogenous recurrence relations with constant coeffic

```
1 a=[];
2 a(1)=1; //initial condition
3 a(2)=2; //initial condition
    disp('for recurrence relation a(n) = 5*a(n-1)-4*a(n-1)
 4
        -2)+n<sup>2</sup>) //this is a second order recurrence
        relation with constant coefficients. It is non
       homogenous because of the n<sup>2</sup>
 5 for n=3:4
 6 a(n) = 5*a(n-1) - 4*a(n-2) + n^2;
 7 mprintf('Value of a(\%i) is: \%i \setminus n', n, a(n))
8 end
9
10 a=[];
11 a(1)=1; //initial condition
12 a(2)=2; //initial condition
13 disp('for recurrence relation a(n)=2*a(n-1)*a(n-2)+n
       ^2') //this recurrence relation is not linear
14 for n=3:4
15 a(n) = 2*a(n-1)*a(n-2)+n^2;
16 mprintf('Value of a(\%i) is: \%i \setminus n', n, a(n))
17 end
```

```
18
19 a=[];
           //initial condition
20 a(1)=1;
21 a(2)=2; //initial condition
22 disp('for recurrence relation a(n)=n*a(n-1)+3*a(n-2)
          //this is a homogenous linear second order
      ')
      recurrence relation without constant coefficients
       because the coefficient of a[n-1] is n, not a
      constant
23 for n=3:4
24 a(n)=n*a(n-1)+3*a(n-2);
25 mprintf('Value of a(\%i) is: \%i \setminus n',n,a(n))
26 end
27
28
29 a=[];
30 a(1)=1;
                //initial condition
31 a(2)=2;
               //initial condition
                //initial condition
32 a(3)=1;
33 disp('for recurrence relation a(n)=2*a(n-1)+5*a(n-2)
      -6*a(n-3)') //this is a homogenous linear third
      order recurrence relation with constant
      coefficients. Thus we need three, not two, initial
      conditions to yield a unique solution of the
      recurrence relation
34 for n=4:6
35 a(n) = 2*a(n-1) + 5*a(n-2) - 6*a(n-3);
36 mprintf('Value of a(\%i) is: \%i \ n',n,a(n))
37 end
```

Scilab code Exa 16.15 Solving linear homogenous recurrence relations with constant

```
1 disp('recurrence relation of Fibonacci numbers f[n]=
    f[n-1]+f[n-2]')
2 x=poly(0, 'x');
```

```
3 g=x^2-x-1;
4 disp(g, 'characterstic equation of the recurrence
      relation is: ')
5 j=[];
6 j = roots(g);
7 disp(j, 'roots of the characterstic equation j1, j2')
8 disp('for general equation fn=Ar^n+Br^n, values of
      Aand B respectively are calculated as: ')
9 disp('initial condition at n=0 and n=1 respectively
      are: ')
10 f1=1;
11 f2=1;
12 //putting the values of f1 and f2 we get the
      equations to solve
13 D=[ 1.6180340 -0.618034; (1.6180340)<sup>2</sup> (-0.618034)
      ^2];
14 K=[1 1]';
15 c=[];
16 c=D\setminus K;
17 A = c(1)
18 B=c(2)
19
20 disp('thus the solution is f[n]
      =0.4472136*((1.618034)^{n}-(-0.4472136)^{n}) ')
```

Scilab code Exa 16.16 Solving linear homogenous recurrence relations with constant

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```
1 disp('The recurrence relation t[n]=4(t[n-1]-t[n-2])'
      )
2 x = poly(0, 'x');
3 disp(g=x^2-4*x+4, 'characterstic polynomial equation
       for the above recurrence relation ')
4 j=[];
5 j = roots(g);
6 disp(j, 'roots of the characterstic equation j1, j2')
7 disp('the general solution is t[n]=n*2^n)
8 \operatorname{disp}(\operatorname{'initial} condition at n=0 and n=1 respectively
      are: ')
9 t0=1;
10 t1=1;
11 // putting the values of t0 and t1 we get the
       equations to solve
12 D=\begin{bmatrix} 1 & 0; 2 & 2 \end{bmatrix}
13 K=\begin{bmatrix} 1 & 1 \end{bmatrix}'
14 c=linsolve(D,K)
```

```
15 D=[1 0;2 2]
16 K=[1 1]'
17 c=[];
18 c=D\K;
19 c1=c(1)
20 c2=c(2)
21 disp('thus the solution is t{n}=2*n-n*2^(n-1)')
```

Scilab code Exa 16.18 Solving linear homogenous recurrence relations with constant

```
1 disp('The recurrence relation a[n]=2*a[n-1]-3a[n-2]'
      )
2 x=poly(0, 'x');
3 disp(g=x^2-2*x-3, 'characterstic polynomial equation
      for the above recurrence relation ')
4 j=[];
5 j = roots(g);
6 disp(j, 'roots of the characterstic equation j1, j2')
7 disp('the general solution is a[n]=c1*3^n+c2*(-1)^n'
      )
8 disp('initial condition at n=0 and n=1 respectively
      are: ')
9 // putting the values of t0 and t1 we get the
      equations to solve
10 a0=1;
11 a1=2;
12 D=[1 1;3 -1]
13 K=[1 2]'
14 c=[];
15 c=DK;
16 c1 = c(1)
17 c2=c(2)
18 disp('thus the solution is a[n] = 0.75 * (3^n) + 0.25 * (1^n)
      ) ')
```

Scilab code Exa 16.19 Solving general homogenous linear recurrence relations

```
1 disp('The recurrence relation a[n]=11*a[n-1]-39*a[n]
      -2]+45*a[n-3]')
2 x=poly(0, 'x');
3 disp(g=x^3-11*x^2+39*x-45, 'characterstic polynomial
      equation for the above recurrence relation ')
4 j=[];
5 j=roots(g);
6 disp(j, 'roots of the characterstic equation j1, j2')
7 disp('hence the general solution is:a[n]=c1*(3^n)+c2
      *n*(3^n)+c3*(5^n)')
8 disp('initial condition at n=0 and n=1 respectively
      are: ')
9 // putting the values of t0 and t1 we get the
      equations to solve
10 a0=5;
11 a1=11;
12 a2=25;
13 D=[1 0 1;3 3 5;9 18 25];
14 \text{ K} = [5 11 25]'
15 c=[];
16 c=D\setminus K;
17 c1 = c(1)
18 c2=c(2)
19 c3=c(3)
20 disp('thus the solution is a[n]=(4-2*n)*(3^n)+5^n')
```