

Scilab Textbook Companion for  
Gas Turbines  
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# Book Description

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Scilab numbering policy used in this document and the relation to the above book.

**Exa** Example (Solved example)

**Eqn** Equation (Particular equation of the above book)

**AP** Appendix to Example(Scilab Code that is an Appednix to a particular Example of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means a scilab code whose theory is explained in Section 2.3 of the book.

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# Chapter 5

## Ideal Cycles and their Analysis

Scilab code Exa 5.1 Calculation of MEP and Efficiency

```
1  clc;
2  p1=1; // Pressure before compression in bar
3  T1=350; // Temperature before compression in kelvin
4  T3=2000; // Temperature after combustion in kelvin
5  rp=1.3; // Pressure ratio
6  Cp=1.005; // Specific heat at constant pressure in
   kJ/kg K
7  r=1.4; // Specific heat ratio
8  R=287; // Characteristic gas constant in J/kg K
9
10 T2=T1*(rp)^((r-1)/r); // Temperature at the end of
   the compression
11 T4=T3*(1/rp)^((r-1)/r); // Temperature after
   expansion
12 Wc=Cp*(T2-T1); // Work done during compression
13 WT=Cp*(T3-T4); // Work done during expansion
14 WN=WT-Wc; // Net work done
15 p2=rp*p1; // Pressure at state 2
16 p3=p2; p4=p1; // Constant pressure process
17 V1=R*T1/(p1*10^5); // specific Volume at state 1
18 V2=R*T2/(p2*10^5); // specific Volume at state 2
```

```

19 V3=R*T3/(p3*10^5); // specific Volume at state 3
20 V4=R*T4/(p4*10^5); // specific Volume at state 4
21 imep=WN*10^3/(V4-V2); // Mean effective pressure
22 q=Cp*(T3-T2); // Heat supplied
23 eff=WN/q; // Efficiency of a Joule cycle
24 disp ("bar",imep*10^-5,"Mean effective pressure = ")
    ;
25 disp ("%",eff*100,"Efficiency of a Joule cycle = ");

```

---

### Scilab code Exa 5.2 Calculation of Improvement in Efficiency

```

1  clc;
2  p1=1; // Pressure before compression in bar
3  T1=350; // Temperature before compression in kelvin
4  T3=2000; // Temperature after combustion in kelvin
5  rp=1.3; // Pressure ratio
6  Cp=1.005; // Specific heat at constant pressure in
    kJ/kg K
7  r=1.4; // Specific heat ratio
8  R=287; // Characteristic gas constant in J/kg K
9
10 T2=T1*(rp)^((r-1)/r); // Temperature at the end of
    the compression
11 T4=T3*(1/rp)^((r-1)/r); // Temperature after
    expansion
12 Wc=Cp*(T2-T1); // Work done during compression
13 WT=Cp*(T3-T4); // Work done during expansion
14 WN=WT-Wc; // Net work done
15 T5=T4; // For a perfect heat exchange
16 q=Cp*(T3-T5); // Heat added
17 eff2=WN/q; // Efficiency of a modified Joule cycle
18 eff1=0.072220534; // Efficiency of a joule cycle
19 disp ("%",eff2*100,"Efficiency of a modified Joule
    cycle = ");
20 disp (eff2/eff1,"Improvement in efficiency = ");

```

---

Scilab code Exa 5.3 calculation of net power output of the cycle

```
1  clc;
2  rp=6; // Pressure ratio
3  T1=300; // Inlet air temperature to the compressor
   in kelvin
4  T3=577+273; // Inlet temperature of air at turbine
   in kelvin
5  Vr=240; // Volume rate in m^3/s
6  Cp=1.005; // Specific heat at constant pressure in
   kJ/kg K
7  r=1.4; // Specific heat ratio
8  R=287; // Characteristic gas constant in J/kg K
9  p1=1; // pressure at state 1 in bar
10
11 T2=T1*(rp)^((r-1)/r); // Temperature at the end of
   the compression
12 T4=T3*(1/rp)^((r-1)/r); // Temperature after
   expansion
13 Wc=Cp*(T2-T1); // Work done during compression
14 WT=Cp*(T3-T4); // Work done during expansion
15 WN=WT-Wc; // Net work done
16 q=Cp*(T3-T2); // Heat supplied
17 row1=p1*10^5/(R*T1); // Density of air at state 1
18 P=WN*Vr*row1; // Power output
19 eff=WN/q; // Efficiency of a cycle
20 disp ("MW (roundoff error)",P/1000,"Power Output =
   ");
21 disp ("%",eff*100,"Efficiency of a cycle = ");
```

---

Scilab code Exa 5.4 Calculation of Efficiency and work of compression

```

1  clc;
2  T1=300; // Inlet air temperature to the compressor
      in kelvin
3  p1=1; // pressure at state 1 in bar
4  T2=475; // Temperature at discharge in kelvin
5  p2=5; // Pressure at state 2
6  T5=655; // Temperature after heat exchanger in
      kelvin
7  T3=870+273; // Temperature at he turbine inlet in
      kelvin
8  T4=450+273; // Temperature after turbine in kelvin
9  Cp=1.005; // Specific heat at constant pressure in
      kJ/kg K
10 r=1.4; // Specific heat ratio
11 R=287; // Characteristic gas constant in J/kg K
12
13 Wc=Cp*(T2-T1); // Work done during compression
14 WT=Cp*(T3-T4); // Work done during expansion
15 WN=WT-Wc; // Net work done
16 q=Cp*(T3-T5); // Heat supplied
17 eff=WN/q; // Efficiency of a cycle
18
19 disp ("kJ/kg",WN,"(i). The output per kg of air = ")
      ;
20 disp ("% ",eff*100,"(ii).The efficiency of the cycle
      = ");
21 disp ("kJ/kg",Wc,"(iii). The work required to drive
      the compressor = ");

```

---

### Scilab code Exa 5.5 Calculation of Thermal Efficiency

```

1  clc;
2  p1=1.4; // Pressure at state 1 in bar
3  T1=310; // Temperature at state 1 in kelvin
4  rp=5; // Pressure ratio

```

```

5 Tmax=1050; // Maximum temperatuer in kelvin
6 WN=3000; // Net output in kW
7 Cp=1.005; // Specific heat at constant pressure in
  kJ/kg K
8 r=1.4; // Specific heat ratio
9 R=287; // Characteristic gas constant in J/kg K
10
11 T3=Tmax;
12 T2=T1*(rp)^((r-1)/r); // Temperature at the state 2
13 T4=T3/(rp)^((r-1)/r); // Temperature at the state 4
14 T5=T4; // As regenerator effectiveness in 100 %
15 m=WN/(Cp*((T3-T4)-(T2-T1))); // mass flow rate of
  air
16 eff=(T3-T4-T2+T1)/(T3-T5); // Efficiency of a cycle
17 disp ("%",eff*100,"(i). Thermal efficiency of the
  cycle = ");
18 disp ("kg/min (roundoff error)",m*60,"(ii). The
  mass flow rate of air per minute = ");

```

---

Scilab code Exa 5.6 Calculation of Pressure ratio of compressor and turbine

```

1 clc;
2 T1=290; // Compressor inlet temperature in kelvin
3 T2=460; // Compressor outlet temperature in kelvin
4 T3=900+273; // Turbine inlet temperature in kelvin
5 T4=467+273; // Turbine outlet temperature in kelvin
6 Cp=1.005; // Specific heat at constant pressure in
  kJ/kg K
7 r=1.4; // Specific heat ratio
8 R=287; // Characteristic gas constant in J/kg K
9
10 c=T2/T1; // Temperature ratio
11 rpc=c^(r/(r-1)); // Compression ratio
12 WN=(Cp*((T3-T4)-(T2-T1))); // Specific power
13 T5=T4; // Assuming regenerator effectiveness to be

```

```

100%
14 eff=WN/(Cp*(T3-T5)); // Overall efficiency of the
    cycle
15 Wc=Cp*(T2-T1); // Work required to drive the
    compressor
16 rpt=(T3/T4)^(r/(r-1)); // Turbine pressure ratio
17 disp (rpt," Turbine pressure ratio = ",rpt,"
    Compressor pressure ratio = ",(i).");
18 disp ("kJ/kg",WN,"(ii). Specific power output = ");
19 disp ("%",eff*100,"(iii). Overall efficiency of the
    cycle = ");
20 disp ("kJ/kg",Wc,"(iv). Work required to drive the
    compressor = ");

```

---

Scilab code Exa 5.7 Calculation of temperature drop across the turbine

```

1 clc;
2 nW_WT=0.563; // Ratio of net work to turbine work
3 T1=300; // Inlet temperature to the compressor in
    kelvin
4 eff=0.35; // Thermal efficiency of the unit
5 m=10; // massflow rate in kg/s
6 Cp=1; // Specific heat at constant pressure in kJ/kg
    K
7 r=1.4; // Specific heat ratio
8
9 c=1/(1-eff); // For ideal simple cycle
10 T2=T1*c; // Temperature at state 2
11 Wc=Cp*(T2-T1); // Compressor work
12 WT=Wc/(1-nW_WT); // Turbine work
13 WN=WT-Wc; // Net work
14 q=WN/eff; // Net heat supplied per kg of air
15 T3=(q/Cp)+T2; // Temperature at state 3
16 T4=T3/c; // Temperature at state 4
17 T3_T4=T3-T4; // Temperature drop across the turbine

```

```
18 disp ("K", T3_T4, "Temperature drop across the turbine
    = ");
```

---

Scilab code Exa 5.8 Calculation of turbine pressure ratio

```
1 clc;
2 p=336.5; //specific power output of a turbine in kW/
    kg
3 T4=700; // Temperature at turbine outlet in kelvin
4 Cp=1; // Specific heat at constant pressure in kJ/kg
    K
5 Cv=0.717; // Specific heat at constant volume in kJ/
    kg K
6
7 r=Cp/Cv; // Specific heat ratio
8 T3=T4+(p/Cp); // Temperature at turbine inlet
9 p3_p4=(T3/T4)^(r/(r-1)); // Pressure ratio across
    the turbine
10 disp (round(p3_p4), "Pressure ratio across the
    turbine = ");
```

---

Scilab code Exa 5.9 Estimation of thermal efficiency of the plant

```
1 clc;
2 T1=300; // Minimum operating temperature in kelvin
3 T3=900; // Maximum operating temperature in kelvin
4 p1=1; // Minimum pressure in bar
5 p3=4; // Maximum pressure in bar
6 m=1600; // Mass flowrate in kg/min
7 r=1.4; // Specific heat ratio
8 Cp=1.005; // Specific heat at constant pressure in
    kJ/kg K
9
```

```

10 p2=p3; p4=p1; // Constant pressure process
11 c=(p2/p1)^((r-1)/r);
12 eff=(1-1/c); // The efficiency of the cycle
13 t=T3/T1; // ratio of maximum and minimum temperature
14 W=Cp*T1*(t*(1-1/c)-(c-1)); // Work output per kg of
    air
15 P=(m/60)*W; // Shaft power available
16 disp ("%",eff*100," Thermal efficiency of the plant
    = ");
17 disp ("kW (roundoff error)",P," Shaft power
    available for external Load = ");

```

---

Scilab code Exa 5.10 Determination of the cycle thermal efficiency

```

1 clc;
2 T1=15+273; // Inlet temperature of air at compressor
    inlet in kelvin
3 rp=6; // Compressor pressure ratio
4 T3=750+273; // Maximum permissible temperature in
    kelvin
5 T5=T3; // After reheat
6 Cp=1.005; // Specific heat at constant pressure in
    kJ/kg K
7 r=1.4; // Specific heat ratio
8
9 c=rp^((r-1)/r);
10 T2=T1*c; // Temperature at state 2
11 p3_p4=sqrt(rp); // For maximum expansion work
12 T4=T3/(p3_p4)^((r-1)/r); // Temperature at state 4
13 T6=T4; // As pressure ratio is same
14 Wc=Cp*(T2-T1); // Compressor work
15 WT=Cp*(T3-T4)+Cp*(T5-T6); // Turbine work
16 T7=T4; // Because of 100% regeneration
17 q=Cp*(T3-T7)+Cp*(T5-T4); // Heat supplied
18 WN=WT-Wc; // Net work done

```



```

19 eff=WN/q; // Efficiency of the plant
20 Wratio=WN/WT; // Work ratio
21 disp ("kJ/kg of air",q,"Heat supplied = ");
22 disp ("kW (roundoff error)",WN,"Net shaft work = "
);
23 disp ("%",eff*100,"The cycle thermal efficiency = ")
;
24 disp (Wratio,"Work ratio = ");

```

---

Scilab code Exa 5.11 Calculation of Efficiency under conditions giving maximum work

```

1 clc;
2 Tmin=5+273; // Minimum operating temperature in
kelvin
3 Tmax=839+273; // Maximum operating temperature in
kelvin
4 Cp=1.005; // Specific heat at constant pressure in
kJ/kg K
5 r=1.4; // Specific heat ratio
6
7 eff_carnot=1-Tmin/Tmax; // Efficiency of the carnot
cycle
8 c=1/(1-eff_carnot);
9 p2_p1=c^(r/(r-1)); // Pressure ratio
10 disp (p2_p1,"(i).Pressure ratio at which efficiency
equals Carnot cycle efficiency = ");
11 t=Tmax/Tmin; // Temperature ratio
12 // Pressure ratio for maximum work is obtained when
13 c=sqrt (t);
14 p2_p1=c^(r/(r-1)); // Pressure ratio
15 eff=1-1/c; // Efficiency at maximum work output
16 disp (p2_p1,"(ii).Pressure ratio at which maximum
work is obtained = ");
17 disp ("%",eff*100,"(iii).Efficiency at maximum work
output = ");

```

---

Scilab code Exa 5.12 Comparison of basic cycle with modified cycles

```
1  clc;
2  rp=4; // Overall pressure ratio
3  T1=300; // Temperature at state 1 in kelvin
4  T3=1000; // Temperature at state 3 in kelvin
5  Cp=1; // Specific heat at constant pressure in kJ/kg
      K
6  Cv=0.717; // Specific heat at constant volume in kJ/
      kg K
7
8  // Basic cycle
9  r=Cp/Cv; // Specific heat ratio
10 c=rp^((r-1)/r);
11 t=T3/T1; // Temperature ratio
12 WN=Cp*T1*(t*(1-1/c)-(c-1)); // Net work output
13 eff=(1-1/c)*100; // Efficiency of the cycle
14
15 // Basic cycle with heat exchanger
16 WN_he=WN;
17 eff_he=(1-c/t)*100; // Efficiency of the cycle with
      heat exchanger
18 dev_WN1=(WN_he-WN)*100/WN; //Percentage deviation of
      Net work from basic cycle
19 dev_eff1=(eff_he-eff)*100/eff; // Percentage
      deviation of efficiency from basic cycle
20
21 // Basic cycle with intercooled compressor
22 WN_ic=(Cp*T1)*(t*(1-1/c)-2*(sqrt(c)-1));
23 eff_ic=(1-(((t/c)+sqrt(c)-2)/(t-sqrt(c))))*100;
24 dev_WN2=(WN_ic-WN)*100/WN; //Percentage deviation of
      Net work from basic cycle
25 dev_eff2=(eff_ic-eff)*100/eff; // Percentage
      deviation of efficiency from basic cycle
```



```

    kJ/kg K
5  r=1.4; // Specific heat ratio
6
7  t=T3/T1; // Temperature ratio
8  Wmax=Cp*((T3*(1-1/sqrt(t)))-T1*(sqrt(t)-1)); //
    Maximum work
9  eff_wmax=(1-1/sqrt(t)); // Efficiency of brayton
    cycle
10 Tmax=T3; Tmin=T1;
11 eff_carnot=(Tmax-Tmin)/Tmax; // Carnot efficiency
12 disp ("kJ/kg of air",Wmax,"Maximum net work per kg
    of air = ");
13 disp ("%",eff_wmax*100,"Brayton cycle efficiency = "
    );
14 disp ("%",eff_carnot*100,"Carnot cycle efficiency =
    ");

```

---

#### Scilab code Exa 5.15 Calculation of Improvement in Efficiency

```

1  clc;
2  p1=1; // Pressure at state 1 in bar
3  T1=300; // Temperature at state 1 in kelvin
4  p4=5; // Pressure at state 4 in bar
5  T5=1250; // Temperature at state 5 in kelvin
6  Cp=1.005; // Specific heat at constant pressure in
    kJ/kg K
7  r=1.4; // Specific heat ratio
8
9  rp=p4/p1; // pressure ratio
10 p2=sqrt(rp); // Because of perfect intercooling
11 c1=p2^((r-1)/r);
12 T2=T1*c1; // Temperature at state 2
13 T4=T2; T3=T1;
14
15 Wc1=Cp*(T2-T1); // Work of compressor 1

```

```

16 Wc=2*Wc1; // net work of compressor
17 WT1=Wc;
18 T6=T5-(WT1/Cp); // Temperature at state 6
19 p5_p6=(T5/T6)^(r/(r-1)); // Pressure ratio
20 p6=rp/p5_p6; // Pressure at state 6
21 p7=p1; T7=T5;p8=p6;
22 T8=T7*(p7/p8)^((r-1)/r); // Temperature in state 8
23 WT2=Cp*(T7-T8); // Turbine 2 work
24 q=Cp*(T5-T4)+Cp*(T7-T6); // Heat supplied
25 eff=WT2/q; // Efficiency of the cycle
26 // With regenerator
27 T9=T8;
28 q_withregen=Cp*((T5-T9)+(T7-T6)); // Heat supplied
    with regenerator
29 eff_withregen=WT2/q_withregen; // Efficiency of the
    cycle with regenerator
30 I_eff=(eff_withregen-eff)/eff_withregen; //
    Percentage improvement in efficiency
31
32 disp ("%",eff*100,"Efficiency of the cycle = ", "kJ/
    kg",q,"Heat supplied = ", "kJ/kg",WT2,"Work of
    turbine = ", "(i). Without regenerator ");
33 disp ("%",eff_withregen*100,"Efficiency of the cycle
    = ", "kJ/kg (roundoff error)",q_withregen,"Heat
    supplied = ", "(ii). With regenerator" );
34
35 disp ("%",I_eff*100,"Percentage improvement in
    efficiency = ");

```

---

Scilab code Exa 5.16 Calculation of Efficiency ratio of the power plants

```

1 clc;
2 p1=1; // pressure at inlet in bar
3 T1=27+273; // Temperature at inlet in kelvin
4 T4=1200; // Maximum temperature in kelvin

```

```

5 t=T4/T1; // Temperature ratio
6 r=1.4; // Specific heat ratio
7
8 rp=t;
9 c=rp^((r-1)/r);
10 x=(1-sqrt(c)/rp)/(1-c/rp);
11 eff2_1=x;
12 r1=sqrt(rp);
13 r2=r1; r3=r1; r4=r1;
14
15 disp (eff2_1,"Efficiency ratio of power plants = ");
16 disp (r4,"pressure ratio of LPT = ",r3,"pressure
    ratio of HPT = ",r2,"pressure ratio of HPC = ",r1
    ,"pressure ratio of LPC = ");

```

---

#### Scilab code Exa 5.19 Determination of Net power output

```

1 clc;
2 m=30; // Mass flow rate in kg/s
3 p1=1; // pressure of air at compressor inlet in bar
4 T1=273+15; // Temperature of air at compressor inlet
    in kelvin
5 p2=10.5; // Pressure of air at compressor outlet
6 T_R=420; // Temperature rise due to combustion in
    kelvin
7 p4=1.2; // Pressure at turbine outlet in bar
8 Cp=1.005; // Specific heat at constant pressure in
    kJ/kg K
9 r=1.4; // Specific heat ratio
10
11 T2=T1*(p2/p1)^((r-1)/r); // Temperature at state 2
12 T3=T2+T_R; // Temperature at state 3
13 p3=p2;
14 T4=T3/(p3/p4)^((r-1)/r);
15 Wc=m*Cp*(T2-T1); // Compressor work

```

```
16 WT=m*Cp*(T3-T4); // Turbine work
17 WN=WT-Wc; // Net work output
18 Q=m*Cp*(T3-T2); // Heat supplied
19 eff_th=WN/Q; // Thermal efficiency
20
21 disp ("%",eff_th*100,"Thermal efficiency = ", "kW" (
    roundoff error)",WN,"Power output = ", "kW",Q,"
    Heat supplied = ");
```

---

# Chapter 6

## Practical Cycles and their Analysis

Scilab code Exa 6.1 Calculation of Net power and overall efficiency of installation

```
1  clc;
2  p01=1; // Pressure at state 1 in bar
3  T01=30+273; // Temperature at state 1 in kelvin
4  p02=6; // Pressure of air after compressed in bar
5  eff_c=0.87; // Isentropic efficiency of compressor
6  T03=700+273; // Temperature at state 3 in kelvin
7  eff_T=0.85; // Isentropic efficiency of the turbine
8  CV=43.1; // calorific value of fuel in MJ/kg
9  ma=80; // Mass flow rate of air in kg/min
10
11 Cpa=1.005; // Specific heat of air at constant
    pressure in kJ/kg K
12 Cpg=1.147; // Specific heat of fuel at constant
    pressure in kJ/kg K
13 rg=1.33; // Specific heat ratio of fuel
14 r=1.4; // Specific heat ratio of air
15 T_02=T01*(p02/p01)^((r-1)/r); // from T-S diagram
16 T02=T01+(T_02-T01)/eff_c; // Temperature after
    compression
```



```

17 // Neglecting the addition of fuel in the combustion
    chamber we have mf+ma=ma
18 mf=(ma/60)*Cpg*(T03-T02)/(CV*10^3);
19 ma_mf=(ma/60)*(1/mf); // Air fuel ratio
20 A_F=ma_mf;
21 p04=p01;p03=p02;
22 T_04=T03*(p04/p03)^((rg-1)/rg);
23 T04=T03-eff_T*(T03-T_04);
24 WN=(ma/60)*Cpg*(T03-T04)-(ma/60)*Cpa*(T02-T01); //
    The net power of installation
25 eff_th=WN/(mf*CV*10^3); // The overall thermal
    efficiency
26
27 disp (A_F,"(i).Air fuel ratio of the turbine gases =
    ");
28 disp ("K",T04,"(ii).The final temperature of exhaust
    gases = ");
29 disp ("kW",WN,"(iii).The net power of installation =
    ");
30 disp ("%",eff_th*100,"(iv).The overall thermal
    efficiency = ");

```

---

Scilab code Exa 6.2 Calculation of ratio of compressor to turbine work

```

1 clc;
2 p01=1; // Air inlet pressure in bar
3 T01=7+273; // Air inlet temperature in kelvin
4 p02=4; // Pressure at state 2 in bar
5 eff_c=0.82; // Isentropic efficiency of compressor
6 T03=800+273; // Maximum temperature at the turbine
    inlet in kelvin
7 eff_T=0.85; // Isentropic efficiency of the turbine
8 CV=43.1; // calorific value of fuel in MJ/kg
9 Cpa=1.005; // Specific heat of air at constant
    pressure in kJ/kg K

```

```

10 Cpg=1.147; // Specific heat of fuel at constant
    pressure in kJ/kg K
11 rg=1.33; // Specific heat ratio of fuel
12 r=1.4; // Specific heat ratio of air
13 LS=0.85;
14 mf=1; // Let assume mass of fuel to be 1 kg
15
16 T_02=T01*(p02/p01)^((r-1)/r); // from T-S diagram
17 T02=T01+(T_02-T01)/eff_c; // Temperature after
    compression
18 Wc=Cpa*(T02-T01); // Work of compression
19 Q=Cpg*(T03-T02); // Heat supplied
20 p04=p01;p03=p02;
21 T_04=T03*(p04/p03)^((rg-1)/rg);
22 T04=T03-eff_T*(T03-T_04);
23 WT=Cpg*(T03-T04); // Turbine work
24 WN=WT-Wc; // Net work done
25 eff_th=WN/(Q/LS); // The thermal efficiency
26 ma_mf=(LS*CV*10^3/Q)^-1; // AIR FUEL ratio
27 ma=mf*ma_mf;
28 sfc=(3600/(ma_mf*WN)); // specific fuel consumption
29 Wc_WT=(Wc*ma)/(WT*(ma+mf)); // work ratio
30
31 disp ("kJ/kg of air",Wc,"(i).Compressor work = ");
32 disp ("kJ/kg of air",Q,"(ii).Heat supplied = ");
33 disp ("kJ/kg of air",WT,"(iii).Turbine work = ");
34 disp ("kJ/kg of air",WN,"(iv).Net work = ");
35 disp ("%",eff_th*100,"(v).Thermal Efficiency = ");
36 disp (ma_mf,"(vi).Air/Fuel ratio = ")
37 disp ("kg/kWh",sfc,"(vii).Specific fuel consumption
    =");
38 disp (Wc_WT,"(viii).Ratio of compressor work to
    turbine work = ");

```

---

Scilab code Exa 6.3 Calculation of effect of pressure loss

```

1  clc;
2  eff_c=0.82; // Isentropic efficiency of the
      compressor
3  eff_T=0.85; // Isentropic efficiency of the turbine
4  eff_m=0.99; // Mechanical transmission efficiency
5  rp=7; // Pressure ratio
6  T03=1000; // Maximum cycle temperature in kelvin
7  eff_comb=0.97; // Combustion efficiency
8  CV=43.1; // Calorific value in MJ/kg
9  ma=20; // Air mass flow rate in kg/s
10 eff_reg=0.75; // Regenerator effectiveness
11 del_P=0.1; // Regenerator gas side pressure loss in
      bar
12 T01=327; // Ambient temperature in kelvin
13 p01=1; // Ambient pressure in bar
14 Cpa=1.005; // Specific heat of air at constant
      pressure in kJ/kg K
15 Cpg=1.147; // Specific heat of fuel at constant
      pressure in kJ/kg K
16 rg=1.33; // Specific heat ratio of fuel
17 r=1.4; // Specific heat ratio of air
18
19 // (i). With Regeneration and pressure loss
20 T_02=T01*(rp)^((r-1)/r);
21 T02=T01+(T_02-T01)/eff_c;
22 p04=p01+del_P;
23 p03=rp/p01;
24 T_04=T03*(p04/p03)^((rg-1)/rg);
25 T04_1=T03-eff_T*(T03-T_04);
26 T05=T02+eff_reg*(T04_1-T02);
27 mf1=(ma*Cpg*(T03-T05))/(CV*10^3*eff_comb); // By
      neglecting the effect of change in mass flow rate
      due to mf in combustion chamber
28 p03_p04_1=p03/p04;
29 WT1=(ma+mf1)*Cpg*(T03-T04_1); // Turbine work
30 WN1=(ma+mf1)*Cpg*(T03-T04_1)-(ma*Cpa*(T02-T01)/eff_m
      ); // Net work output
31 sfc1=mf1*3600/WN1; // Specific fuel consumption

```





```

6 rp=3; // Pressure ratio in each stage of compression
7 T08=297; // Temperature after intercooler in kelvin
8 ma=15; // Air mass flow in kg/s
9 eff_reg=0.8; // Regenerator effectiveness
10 del_P=0.1; // Regenerator gas side pressure loss in
    bar
11 T01=327; // Ambient temperature in kelvin
12 p01=1; // Ambient pressure in bar
13 T03=1000; // Maximum cycle temperature in kelvin
14 CV=43.1; // Calorific value in MJ/kg
15 Cpa=1.005; // Specific heat of air at constant
    pressure in kJ/kg K
16 Cpg=1.147; // Specific heat of fuel at constant
    pressure in kJ/kg K
17 rg=1.33; // Specific heat ratio of fuel
18 r=1.4; // Specific heat ratio of air
19 p03=rp^2; // Pressre at state 3 in bar
20 T_07=T01*(rp)^((r-1)/r);
21 T07=T01+(T_07-T01)/eff_c;
22 WLPC=ma*Cpa*(T07-T01); // Work of low pressue
    compressor
23 T_02=T08*(rp)^((r-1)/r);
24 T02=T08+(T_02-T08)/eff_c;
25 WHPC=ma*Cpa*(T02-T08);
26 WC=WLPC+WHPC; // Compressor work
27 WCa=WC/eff_trans; // Actual compressor work
28 // Neglecting effect of mf
29 T09=T03-(WCa/(ma*Cpg));
30 T_09=T03-(T03-T09)/eff_PT;
31 p09=p03/(T03/T_09)^(rg/(rg-1));
32 p04=p01+del_P;
33 T_04=T09*(p04/p09)^((rg-1)/rg);
34 T04=T09-eff_PT*(T09-T_04);
35 WTP=ma*Cpg*(T09-T04); // Work output of power
    turbine
36 T05=T02+eff_reg*(T04-T02);
37 mf=(ma*Cpg*(T03-T05))/(CV*10^3);
38 sfc=mf*3600/(WTP); // Specific fuel consumption

```

```

39 eff_th=WTP/(mf*CV*10^3); // Thermal efficiency
40
41
42 disp ("kW (roundoff error)",WTP,"Work output of
    power turbine = ");
43 disp ("kg/kW h",sfc,"Specifc fuel consumption = ");
44 disp ("% ",eff_th*100,"Thermal efficiency = ");

```

---

**Scilab code Exa 6.5** Calculation of the thermal efficiency and air rate

```

1  clc;
2  Wplant=1850; // Plant work output in KW
3  p01=1; // Ambient pressure in bar
4  T01=27+273; // Ambient temperature in kelvin
5  T03=720+273; // Maximum cycle temperature in kelvin
6  rp=2.5; // Pressure ratio
7  eff_T=0.80; // Turbine and compressor efficiency
8  eff_reg=0.75; // Regenerator effectiveness
9  eff_comb=0.98; // Combustion efficiency
10 CV=43.1; // Calorific value in MJ/kg
11 del_p=0.03; // Pressure drop
12 p02=6.25; // Pressure in bar
13 Cpa=1.005; // Specific heat of air at constant
    pressure in kJ/kg K
14 Cpg=1.147; // Specific heat of fuel at constant
    pressure in kJ/kg K
15 rg=1.33; // Specific heat ratio of fuel
16 r=1.4; // Specific heat ratio of air
17
18 T_07=T01*rp^((r-1)/r);
19 T07=T01+(T_07-T01)/eff_T;
20 T02=T07;
21 WLPC=Cpa*(T07-T01); // Work of low pressure
    compressor
22 WHPT=WLPC;

```

```

23 T09=T03-WHPT/Cpg;
24 T_09=T03-(T03-T09)/eff_T;
25 p03=(1-del_p)^2*p02
26 p09=p03/(T03/T_09)^(rg/(rg-1));
27 p10=p09*(1-del_p);
28 T10=T03;
29 p04=p01+del_p;
30 T_04=T10*(p04/p10)^((rg-1)/rg);
31 T04=T10-eff_T*(T10-T_04);
32 Wlpt=Cpg*(T10-T04);
33 WN=Wlpt-WHPT;
34 ma=Wplant/WN;
35 T05=T02+eff_reg*(T04-T02);
36 Q=Cpg*(T03-T05+T10-T09);
37 eff_th=WN/Q;
38 WHPT_1=ma*WHPT;
39 Wlpt_1=ma*Wlpt;
40 mf=ma*Q*3600/(eff_comb*CV*10^3);
41 sfc=mf/Wplant;
42
43 disp ("K",T_07,"T_07 = ");
44 disp ("K",T07,"T07 = ");
45 disp ("K",T09,"T09 = ");
46 disp ("K",T_09,"T_09 = ");
47 disp ("K",T_04,"T_04 = ");
48 disp ("K",T04,"T04 = ");
49 disp ("K",T05,"T05 = ");
50 disp ("bar",p03,"P03 = ");
51 disp ("bar",p09,"P09 = ");
52 disp ("bar",p10,"P10 = ");
53 disp ("kg/s",ma,"Mass flow rate = ");
54 disp ("%",eff_th*100,"The overall efficiency = ");
55 disp ("kg of fuel/kW h",sfc,"Specific fuel
consumption = ");

```

---



Scilab code Exa 6.6 Calculation of Compressor efficiency and the temperature ratio

```
1  clc;
2  rp=11.3137; // Pressure ratio
3  WN=0; // Net work output
4  Q=476.354; // Heat added per kg of air mass in kJ
5  T01=300; // Inlet air total temperature in kelvin
6  eff_T=0.71; // turbine efficiency
7  Cpa=1.005; // Specific heat of air at constant
   pressure in kJ/kg K
8  Cpg=1.147; // Specific heat of fuel at constant
   pressure in kJ/kg K
9  rg=1.33; // Specific heat ratio of fuel
10 r=1.4; // Specific heat ratio of air
11
12 T_02=T01*rp^((r-1)/r);
13 T03_T02=Q/Cpa;
14 T03_T_04=rp^((r-1)/r);
15 T04_T03=1-(eff_T*(1/T03_T_04)*(T03_T_04-1));
16 T04=T01+(T03_T02);
17 T03=T04/T04_T03;
18 t=T03/T01; //Temperature ratio
19 T02=T03-T03_T02;
20 eff_C=(T_02-T01)/(T02-T01); // Compressor efficiency
21
22 disp ("%",eff_C*100,"Compressor Efficiency = ",);
23 disp (t,"Temperature ratio = ");
```

---

Scilab code Exa 6.7 Calculation of suitable pressure ratio

```
1  clc;
2  eff_C=0.7042; // Efficiency of the compressor
3  eff_T=0.71; // Efficiency of the turbine
4  Q=476.354; // Head added in kJ/kg
5  WR=0.0544; // Work ratio
```

```

6 T01=300; // Total inlet temperature in kelvin
7 Cpa=1.005; // Specific heat of air at constant
  pressure in kJ/kg K
8 Cpg=1.147; // Specific heat of fuel at constant
  pressure in kJ/kg K
9 rg=1.33; // Specific heat ratio of fuel
10 r=1.4; // Specific heat ratio of air
11
12 c_t=(1-WR)*(eff_T*eff_C);
13 t=((Q/(Cpg*T01))+1-1/eff_C)/(1-c_t/eff_C); //
  Temperature ratio
14 c=c_t*t;
15 rp=c^(r/(r-1)); // Pressure ratio
16
17 disp (rp,"Pressure ratio = ");
18 disp (t,"Temperature ratio = ");

```

---

Scilab code Exa 6.8 Calculation of minimum temperature ratio

```

1 clc;
2 WR=0.3; // Work ratio
3 rp=12; // Pressure ratio
4 t=4; // Temperature ratio
5 Cpa=1.005; // Specific heat of air at constant
  pressure in kJ/kg K
6 Cpg=1.147; // Specific heat of fuel at constant
  pressure in kJ/kg K
7 rg=1.33; // Specific heat ratio of fuel
8 r=1.4; // Specific heat ratio of air
9
10 c=rp^((r-1)/r);
11 eff_C_T=1/((1-WR)*t/c);
12 tmin=c/eff_C_T;
13 eff=1-1/c;
14

```

```

15 disp (tmin,"Minimum Temperature ratio = ");
16 disp ("%",eff*100," Efficiency = ");

```

---

**Scilab code Exa 6.9** Calculation of Isentropic efficiency of Turbine

```

1 clc;
2 eff_pe=0.85; // Polytropic efficiency of the
   compressor
3 T_02_T01=2;
4 Cpa=1.005; // Specific heat of air at constant
   pressure in kJ/kg K
5 Cpg=1.147; // Specific heat of fuel at constant
   pressure in kJ/kg K
6 rg=1.33; // Specific heat ratio of fuel
7 r=1.4; // Specific heat ratio of air
8
9 rc=(T_02_T01)^(r/(r-1));
10 eff_C=(T_02_T01-1)/(((rc^(((r-1)/r)*(1/eff_pe))))-1))
   ; // Compressor efficiency
11 eff_T=(1-(1/rc)^(eff_pe*(r-1)/r))/(1-(1/rc)^((r-1)/r
   )); // Turbine efficiency
12
13
14 disp ("%",eff_C*100," Isentropic compressor
   efficiency = ");
15 disp ("%",eff_T*100," Isentropic Turbine efficiency
   = ");

```

---

**Scilab code Exa 6.10** Plotting variation of Isentropic efficiency over a range of p

```

1 clc;
2 eff_C=0.85; // Isentropic efficiency of the
   compressor

```

```

3 rp=4; // Pressure ratio
4 r=1.4; // specific heat ratio
5 eff_pc=((r-1)/r)*log(rp)/log(((rp^((r-1)/r)-1)/
    eff_C)+1);
6 disp ("%",eff_pc*100," Polytropic efficiency = ");
7 disp ("variation of compressor efficiency with
    compression ratio is shown in window1");
8 xset('window',1);
9 function eff_c=f(rc)
10     eff_c=(rc^0.286-1)/(rc^0.326-1);
11 endfunction
12 rc=linspace(2,10,4);
13 plot(rc,f);
14 title("variation of compressor efficiency with
    compression ratio","fontsize",4,"color","blue");
15 xlabel("compression ratio (rc)","fontsize",4,"color"
    ,"blue");
16 ylabel("Compressor efficiency","fontsize",4,"color"
    ,"blue");

```

---

Scilab code Exa 6.11 Calculation of the power output thermal efficiency and the he

```

1 clc;
2 eff_pe=0.88; // Compressor and turbine polytropic
    efficiencies
3 T01=310; // Temperature at LP compressor inlet in
    kelvin
4 p01=14; // Pressure at LP compressor inlet in bar
5 rp=2; // Compressor pressure ratio
6 T03=300; // Temperature at HP compressor inlet in
    kelvin
7 m=180; // Mass flow of Helium in kg/s
8 Q=500; // Heat input to gas turbine in MW
9 T07=700; // Helium Temperature at entry to reactor
    channels in kelvin

```

```

10 P_precoller=0.34; // Pressure loss in pre-cooler and
    intercooler in bar
11 P_loss_HE=0.27; // Pressure loss in heat exchanger
    in bar
12 P_loss_RC=1.03; // Pressure loss in reactor channel
    in bar
13 eff_pc=0.88; // Polytropiic efficiency
14 Cp=5.19; // Specific heat at constant pressure in
    kJ/kg K
15 r=1.66; // Specific heat ratio
16
17 n_1_n=((r-1)/r)*(1/eff_pc);
18 T02=T01*rp^n_1_n;
19 T04=T03*rp^n_1_n;
20 T05=((Q*10^3)/(m*Cp))+T07;
21 T_press_loss=P_precoller+P_loss_HE+P_loss_RC; //
    Total pressure loss
22 p05=56-T_press_loss;
23 p06=p01+P_precoller+P_loss_HE;
24 n__1_n=eff_pc*((r-1)/r);
25 T06=T05/(p05/p06)^n__1_n;
26 WC=m*Cp*((T02-T01)+(T04-T03)); // Work of compressor
27 WT=m*Cp*(T05-T06); // Work of Turbine
28 WN=WT-WC; // Net work output
29 eff_th=WN/(Q*10^3); // Efficiency
30 eff=(T07-T04)/(T06-T04); // Effectiveness
31
32 disp ("MW (roundoff error)",WN/1000,"Power output
    = ");
33 disp ("% (roundoff error)",eff_th*100,"Thermal
    efficiency = ");
34 disp ("% (roundoff error)",eff*100,"Effectiveness
    = ");

```

---

Scilab code Exa 6.12 Calculation of the isentropic efficiency of the turbine and t

```

1  clc;
2  rp=4; // Pressure ratio
3  WN=1500; // Net work output in kW
4  T01=25+273; // Inlet temperature in kelvin
5  p01=1; // Inlet pressure in bar
6  p03=4; // Turbine inlet pressure in bar
7  T03=700+273; // turbine inlet temperature in kelvin
8  eff_c=0.85; // Compressor efficiency
9  eff_over=0.21; // Overall efficiency
10 Cp=1.005; // Specific heat of air at constant
    pressure in kJ/kg K
11 r=1.4; // Specific heat ratio of air
12
13 T02=T01+T01*(rp^((r-1)/r)-1)/eff_c;
14 Q=WN/eff_over;
15 m=Q/(Cp*(T03-T02));
16 Wn=WN/m; // Net work per kg
17 T04=T03-T02+T01-(Wn/Cp);
18 T_04=T03/rp^((r-1)/r);
19 eff_T=(T03-T04)/(T03-T_04);
20
21 disp ("kg/s",m,"Mass flow rate = ");
22 disp ("%",eff_T*100,"Isentropic efficiency of the
    Turbine = ");

```

---

**Scilab code Exa 6.13** Determination of pressure of the gas entering the low pressure

```

1  clc;
2  rp=4; // Pressure ratio
3  eff_c=0.86; // Compressor efficiency
4  eff_Thp=0.84; // High pressure turbine efficiency
5  eff_Tlp=0.8; // Low pressure turbine efficiency
6  eff_M=0.92; // Mechanical efficiency
7  T03=660+273; // in kelvin
8  T05=625+273; // In kelvin

```

```

 9 T01=15+273; // Inlet temperature in kelvin
10 p01=1; // Inlet pressure in bar
11 Cp=1.005; // Specific heat of air at constant
    pressure in kJ/kg K
12 r=1.4; // Specific heat ratio of air
13 eff= 0.75; // Heat exchanger effectiveness
14
15 T_02=T01*(rp)^((r-1)/r);
16 T02=((T_02-T01)/eff_c)+T01;
17 T04=T03-((T02-T01)/eff_M);
18 // In HP turbine
19 T_04=T03-((T03-T04)/eff_Thp);
20 p_04=rp/(T03/T_04)^(r/(r-1));
21 // In LP turbine
22 p05=p_04;p_06=p01;
23 T_06=T05/(p05/p_06)^((r-1)/r);
24 T06=T05-(eff_Tlp*(T05-T_06));
25 T07=T02+eff*(T06-T02);
26 Q=Cp*(T03-T07+T05-T04);
27 Wc=Cp*(T02-T01);
28 WT=Cp*(T03-T04+T05-T06);
29 eff_th=(WT-Wc)/Q;
30
31 disp ("bar",p_04,"(i).Pressure of gas entering low
    pressure turbine = ");
32 disp ("%",eff_th*100,"Overall efficiency = ");

```

---

Scilab code Exa 6.14 Calculation of pressure ratio and cycle efficiency

```

1 clc;
2 T01=38+273; // Inlet temperature of compressor in
    kelvin
3 eff_c=0.82; // Compressor efficiency
4 T03=650+273; // Turbine inlet temperature in kelvin
5 eff_T=0.8; // Turbine efficiency

```

```

6 Cpa=1.005; // Specific heat of air at constant
   pressure in kJ/kg K
7 Cpg=1.147; // Specific heat of fuel at constant
   pressure in kJ/kg K
8 rg=1.33; // Specific heat ratio of fuel
9 r=1.4; // Specific heat ratio of air
10
11 t=T03/T01;
12 // For maximum specific work we know that
13 ropt=(sqrt(t*eff_c*eff_T))^(r/(r-1));
14 T_02=T01*ropt^((r-1)/r);
15 T02=T01+(T_02-T01)/eff_c;
16 T_04=T03/ropt^((rg-1)/rg);
17 T04=T03-eff_T*(T03-T_04);
18 eff_th=((Cpg*(T03-T04))-(Cpa*(T02-T01)))/(Cpg*(T03-
   T02));
19
20 disp(ropt,"Optimum pressure ratio = ");
21 disp("%",eff_th*100,"Overall efficiency = ");

```

---

**Scilab code Exa 6.15** Estimation of the temperature of the gases at entry to the turbine

```

1 clc;
2 p01=1; // Stagnation pressure at entry in bar
3 pa=0.93; // Static pressure at entry in bar
4 T1=10+273; // Static temperature in entry in kelvin
5 p02=6; // Pressure at state 2 in bar
6 T02=230+273; // Temperature at state 2 in kelvin
7 P=5100; // Turbine output power in kW
8 A=0.1; // Compressor entry area in m^2
9 Cpa=1.005; // Specific heat of air at constant
   pressure in kJ/kg K
10 Cpg=1.147; // Specific heat of fuel at constant
   pressure in kJ/kg K
11 rg=1.33; // Specific heat ratio of fuel

```



```

12 r=1.4; // Specific heat ratio of air
13 R=287; // Characteristic constant in J/kg K
14 T04=460+273; // Exhaust pipe temperature in kelvin
15
16 M=sqrt (((p01/pa)^((r-1)/r)-1)/((r-1)/2));
17 T01=T1*(1+(r-1)/2*M^2);
18 T_02=T01*(p02/p01)^((r-1)/r);
19 eff_c=(T_02-T01)/(T02-T01);
20 row_s=(pa*10^5)/(R*T1);
21 a=sqrt (r*R*T1);
22 V=M*a;
23 m=row_s*A*V;
24 T03=(P/(m*Cpg))+T04;
25
26 disp ("%", eff_c*100, "Compressor efficiency = ");
27 disp ("kg/s", m, "Mass flow rate = ");
28 disp ("K (roundoff error)", T03, "Turbine inlet
    stagnation temperature = ");

```

---

Scilab code Exa 6.16 Calculation of efficiency and work ratio of modern turbines a

```

1 clc;
2 T01=27+273; // Inlet temperature in kelvin
3 p01=1; // Inlet pressure in bar
4 rp=3; // Pressure ratio
5 Cpa=1.005; // Specific heat of air at constant
    pressure in kJ/kg K
6 Cpg=1.147; // Specific heat of fuel at constant
    pressure in kJ/kg K
7 rg=1.33; // Specific heat ratio of fuel
8 r=1.4; // Specific heat ratio of air
9 R=287; // Characteristic constant in J/kg K
10
11 T_02=T01*rp^((r-1)/r);
12 // Turbines 70 years ago

```

```

13 eff_c=0.65; // Compressor efficiency
14 eff_T=0.7; // Turbine efficiency
15 T03=700+273; // in kelvin
16 T02=T01*(1+((rp^((r-1)/r)-1)/eff_c));
17 T04=T03*(1-eff_T*(1-(1/rp^((rg-1)/rg))));
18 eff_th=(Cpg*(T03-T04)-Cpa*(T02-T01))/(Cpg*(T03-T02))
    ;
19 WR=(Cpg*(T03-T04)-Cpa*(T02-T01))/(Cpg*(T03-T04));
20
21 disp (WR,"Work ratio = ",eff_th*100,"The Efficiency
    = ", "(i).70 years ago");
22
23 //Modern turbines
24 eff_c=0.85; // Compressor efficiency
25 eff_T=0.9; // Turbine efficiency
26 T03=1000+273; // in kelvin
27 T02=T01+(T_02-T01)/eff_c;
28 T_04=T03/rp^((rg-1)/rg);
29 T04=T03-eff_T*(T03-T_04);
30 Wc=Cpa*(T02-T01);
31 WT=Cpg*(T03-T04);
32 WN=WT-Wc;
33 eff_th=WN/(Cpg*(T03-T02));
34 WR=WN/WT;
35
36 disp (WR,"Work ratio = ", "%", eff_th*100,"The
    Efficiency = ", "(ii).Modern turbines");

```

---

Scilab code Exa 6.17 Determination of necessary mass flow rate

```

1 clc;
2 rp=7; // Pressure ratio
3 T03=1000; // Maximum temperature in kelvin
4 eff_c=0.85; // Compressor efficiency
5 eff_T=0.9; // Turbine efficiency

```

```

6 T01=288; // Air entering temperature in kelvin
7 PN=750; // Power output in kW
8 Cpa=1.005; // Specific heat of air at constant
    pressure in kJ/kg K
9 Cpg=1.147; // Specific heat of fuel at constant
    pressure in kJ/kg K
10 rg=1.33; // Specific heat ratio of fuel
11 r=1.4; // Specific heat ratio of air
12 R=287; // Characteristic constant in J/kg K
13
14 // Actual cycle
15 T02=T01*(1+((rp^((r-1)/r)-1)/eff_c));
16 T04=T03*(1-(eff_T*(1-(1/rp^((r-1)/r)))));
17 WN_a=(Cpa*(T03-T04)-Cpa*(T02-T01));
18 eff_th=WN_a/(Cpa*(T03-T02));
19 disp ("%",eff_th*100,"The Efficiency = ","kJ/kg",
    WN_a,"Net work = ",(i).Actual cycles");
20
21 // Ideal cycle
22 WN=Cpa*((T03*(1-(1/rp^((r-1)/r))))-T01*((rp^((r-1)/r
    )-1)));
23 eff_th=1-(1/rp^((r-1)/r));
24 ma=PN/WN_a;
25
26 disp ("kg/s",ma,"Mass flow rate = ","%",eff_th*100,
    "The Efficiency = ","kJ/kg",WN,"Net work = ",(ii
    ).Ideal cycles");

```

---

Scilab code Exa 6.18 Estimation of intermediate pressure and temperature between t

```

1 clc;
2 m=5; // Mass flow rate in kg/s
3 p01=1; // Pressure at state 1 in bar
4 p02=5; // Pressure at state 2 in bar
5 eff_c=0.85; // Compressor efficiency

```

```

6  eff_Thp=0.87; // High pressure turbine efficiency
7  eff_Tlp=0.82; // Low pressure turbine efficiency
8  T03=675+273; // HP turbine inlet temperature in
    kelvin
9  eff=0.7; // Effectiveness of the heat exchanger
10 T01=15+273; // Temperature at state 1 in kelvin
11 Cpa=1.005; // Specific heat of air at constant
    pressure in kJ/kg K
12 r=1.4; // Specific heat ratio of air
13 R=287; // Characteristic constant in J/kg K
14 p03=p02;
15
16 T_02=T01*(p02/p01)^((r-1)/r);
17 T02=T01+(T_02-T01)/eff_c;
18 T04=T01-T02+T03;
19 T_04=T03-(T03-T04)/eff_Thp;
20 p04=p03/(T03/T_04)^(r/(r-1));
21 p05=p01;
22 T_05=T04/(p04/p05)^((r-1)/r);
23 T05=T04-eff_Tlp*(T04-T_05);
24 T0x=eff*(T05-T02)+T02;
25 Wlpt=Cpa*(T04-T05);
26 Plpt=Wlpt*m;
27 Q=Cpa*(T03-T0x);
28 eff_th=Wlpt/Q;
29
30 disp ("Intermediate pressure p04 and temperature T04
    between the two turbine stages ");
31 disp ("K",T04,"To4 = "," bar",p04," P04 = ");
32 disp ("kW",Plpt,"Power output of LP turbine = ");
33 disp ("kJ/kg",Q,"Heat supplied = ");
34 disp ("%",eff_th*100,"The Overall efficiency = ");

```

---

Scilab code Exa 6.19 Determination of the percentage of the total air intake that

```

1  clc;
2  rlp=3; // Pressure ratio
3  rhp=rlp;
4  eff_c=0.82; // Compressor efficiency
5  T04=650+273; // Temperature at state 4 in kelvin
6  T05=540+273; // Temperature at state 5 in kelvin
7  eff_T=0.87; // Efficiency of turbine
8  T01=15+273; // Temperature at compressor inlet in
   kelvin
9  Cpa=1.005; // Specific heat of air at constant
   pressure in kJ/kg K
10 Cpg=1.147; // Specific heat of fuel at constant
   pressure in kJ/kg K
11 rg=1.33; // Specific heat ratio of fuel
12 r=1.4; // Specific heat ratio of air
13
14 T02=T01*(1+(rlp^((r-1)/r)-1)/eff_c);
15 T03=T02*(1+(rhp^((r-1)/r)-1)/eff_c);
16 T_06=T05/(rlp^(2*(rg-1)/rg));
17 T06=T05-eff_T*(T05-T_06);
18 x1=1-((T02-T01)/(((Cpg/Cpa)*(T05-T06)-(T03-T02))));
19 x=abs(x1);
20 T07=T04*(1-(eff_T*(1-(1/rhp^((rg-1)/rg)))));
21 eff_th=(x*Cpg*(T04-T07))/((1-x)*Cpg*(T05-T03)+x*Cpg
   *(T04-T02));
22
23 disp ("%", (x)*100, "Percentage of the total air
   intake that passes to the power turbine = ");
24 disp ("% (Roundoff error)", (eff_th)*100, "The
   overall efficiency = ");

```

---

Scilab code Exa 6.20 Calculation of the Thermal efficiency

```

1  clc;
2  rp=2; // Pressure ratio

```

```

3 T01=15+273; // Inlet temperature in kelvin
4 p01=1; // Inlet pressure in bar
5 T05=700+273; // Temperature at state 5 in kelvin
6 T07=T05;
7 eff_c=0.85; // compressor efficiency
8 eff_T=0.85; // Turbine efficiency
9 eff=0.5; // Effectiveness of heat exchanger
10 Cp=1.147; // Specific heat at constant pressure in kJ
    /kg K
11 rg=1.33; // Specific heat ratio of fuel
12 r=1.4; // Specific heat ratio of air
13
14 T03=T01;
15 // p02/p01=p04/p03=rp
16 //p04/p01=p05/p08=rp^2
17 T_02=T01*(rp)^((r-1)/r);
18 T02=T01+(T_02-T01)/eff_c;
19 T04=T02;
20 T_06=T05/rp^((rg-1)/rg);
21 T06=T05-eff_T*(T05-T_06);
22 T08=T06;
23 T09=T04+eff*(T08-T04);
24 WN=Cp*(T07-T08);
25 Q=Cp*(2*T05-T06-T09);
26 eff_th=WN/Q;
27
28 disp ("kJ/kg",WN,"Net work done = ");
29 disp ("%",eff_th*100,"The overall efficiency = ");

```

---

Scilab code Exa 6.21 Calculation of cycle thermal efficiency

```

1 clc;
2 T01=270+273; // Temperature at state 1 in kelvin
3 T03=T01;
4 p01=1; // Inlet pressure in bar

```

```

5 rp=6; // Pressure ratio
6 eff_c=0.85; // Compressor efficiency
7 T05=1150+273; // Temperature at inlet to expansion
   in kelvin
8 eff_T=0.9; // Turbine efficiency
9 n=1.24; // Polytropic index
10 R=10.05; // in kJ/kg K
11
12 T_02=T01*rp^((n-1)/n);
13 T02=T01+(T_02-T01)/eff_c;
14 Cv=R/(n-1);
15 Cp=R+Cv;
16 Wc=2*Cp*(T02-T01);
17 T_06=T05/rp^((n-1)/n);
18 T06=T05-eff_T*(T05-T_06);
19 WT=2*Cp*(T05-T06);
20 Q=Cp*(T05-T02)+Cp*(T05-T06);
21 WN=WT-Wc;
22 eff_th=WN/Q;
23
24 disp ("%",eff_th*100,"The Cycle efficiency = ");

```

---

## Chapter 7

# Jet Propulsion Cycles and Their Analysis

Scilab code Exa 7.1 Calculation of Thrust power and Heat Input

```
1  clc;
2  CV=43; // Calorific value of fuel in MJ/kg
3  mf=0.18*9000/3600; // Fuel consumption in kg/s
4  F=9; // Thrust in kN
5  ci=500; // Aircraft velocity in m/s
6  ma=27; // Mass of air passing through compressor in
      kg/s
7
8  A_F=ma/mf; // Air fuel ratio
9  PT=F*ci; // Thrust power
10 Q=mf*(CV*103); // Heat supplied
11 eff=PT/Q; // Overall efficiency
12 disp (A_F,"Air fuel ratio = ");
13 disp ("%",eff*100,"Overall efficiency = ");
```

---

Scilab code Exa 7.2 Calculation of The Total Design Thrust



```

1  clc;
2  T03=1200; // Maximum turbine inlet temperature in
           kelvin
3  rc=4.25; // Pressure ratio across compressor
4  ma=25; // Mass flow rate in kg/s
5  eff_C=0.87; // Isentropic efficiency of the
           compressor
6  eff_T=0.915; // Isentropic efficiency of turbine
7  eff_n=0.965; // Propelling nozzle efficiency
8  eff_Tr=0.985; // Transmission efficiency
9  del_pcomb=0.21; // Combustion chamber pressure loss
           in bar
10 Cpa=1.005; // Specific heat at constant pressure of
           air in kJ/kg K
11 ra=1.4; // Specific heat ratio of air
12 Cpg=1.147; // Specific heat of fuel in kJ/kg K
13 rg=1.33; // Specific heat of fuel
14 T01=293; // Ambient temperature in kelvin
15 p01=1; // Ambient pressure in bar
16 A_F=50; // Air Fuel ratio
17 p02=rc/p01;
18
19 T02=(T01*((rc)^((ra-1)/ra)-1)/eff_C)+T01; // Actual
           temperature at state 2
20 T04=T03-((Cpa*(T02-T01))/(eff_Tr*Cpg)); //
           Temperature at state 4
21 rt=(1/(1-((T03-T04)/(eff_T*T03))))^(1/((rg-1)/rg));
           // Pressure ratio across turbine
22 p04=(p02-del_pcomb)/rt; // Pressure at 4
23 p5=p01;
24 T_5=T04/(p04/p5)^((rg-1)/rg); // Temperature at 5
25 T5=T04-eff_n*(T04-T_5);
26 c5=sqrt (2*Cpg*10^3*(T04-T5));
27 F=ma*c5; // Total design thrust
28 p04_pc=1/(1-((1/eff_n)*((rg-1)/(rg+1))))^(rg/(rg-1))
29 pc=p04*(1/p04_pc);
30 Tc=T04*(1/p04_pc)^((rg-1)/rg);
31 R=Cpg*10^3*(rg-1)/rg;

```

```

32  cj=sqrt (rg*R*Tc);
33  row_c=(pc*10^5)/(R*Tc);
34  A=ma/(row_c*cj); // Area of the propelling nozzle
35  d=sqrt (4*A/3.14); // Diameter of the nozzle
36  pa=p01;
37  Fp=(pc-pa)*10^5*A; // Pressure thrust
38  Fm=ma*cj;
39  Ft=Fp+Fm; // Total thrust
40  sfc=(ma/A_F)*3600/Ft;
41
42  disp ("N (roundoff error)",F," Total design thrust
/s = ");
43  disp ("N (roundoff error)",Ft," Total thrust /s = "
);
44  disp ("kg/ N thrust h",sfc, " Specific fuel
consumption = ");

```

---

**Scilab code Exa 7.3** Calculation of the velocity leaving the nozzle

```

1  clc;
2  p03=4.5; // Pressure at turbine inlet in bar
3  T03=800+273; // Temperature at turbine inlet in
kelvin
4  p04=1.75; // Pressure at turbine outlet in bar
5  eff_T=0.75; //Turbine efficiency
6  p05=1.03; // Pressure at state 5 in bar
7  Cp=1.05; // Specific heat at constant pressure in
kJ/kg K
8  r=1.38; // Specific heat ratio
9
10 T04=T03*(1-eff_T*(1-(1/(p03/p04)^((r-1)/r)))); //
Temperature at state 4
11 cj=sqrt (2*Cp*10^3*T04*(1-(1/(p04/p05)^((r-1)/r))));
// Velocity leaving nozzle
12

```

```

13 disp ("K",T04,"(i).Temperature of the gas entering
    the jet (nozzle) = ");
14 disp ("m/s",cj,"(ii).Velocity of gas leaving the jet
    = ");

```

---

#### Scilab code Exa 7.4 Calculation of propulsive efficiency

```

1  clc;
2  cj=2700; // The effective jet velocity from jet
    engine in m/s
3  ci=1350; // Flight velocity in m/s
4  ma=78.6; // Air flow rate in m/s
5
6  a=ci/cj;
7  F=ma*(cj-ci); // Thrust
8  P=F*ci; // Thrust power
9  eff_P=2*a/(a+1); // Propulsive efficiency
10
11 disp ("N",F,"(i).Thrust = ");
12 disp ("MN",P/10^6,"(ii). Thrust power = ");
13 disp ("%",eff_P*100,"(iii). Propulsive efficiency =
    ");

```

---

#### Scilab code Exa 7.5 Calculation of the thrust and Specific fuel consumption

```

1  clc;
2  pa=0.458; // Ambient pressure in bar
3  Ta=248; // Ambient temperature in kelvin
4  Ci=805*1000/3600; // Speed of the aircraft in m/s
5  rp=4; // Pressure ratio
6  DelP_comb=0.21; // Combustion chamber pressure loss
    in bar
7  T03=1100; // Turbine inlet temperature in kelvin

```

```

8  eff_ram=0.95; // Intake duct efficiency
9  eff_c=0.85; // Compressor efficiency
10 eff_T=0.90; // Turbine efficiency
11 eff_m=0.99; // Mechanical efficiency of transmission
12 eff_nozzle=0.95; // Nozzle efficiency
13 CV=43; // Low calorific value in MJ/kg
14 Ac=0.0935; // Nozzle outlet area in m^2
15 Cpa=1.005; // Specific heat of air at constant
    pressure in kJ/kg K
16 Cpg=1.147; // Specific heat of fuel at constant
    pressure in kJ/kg K
17 rg=1.33; // Specific heat ratio of fuel
18 r=1.4; // Specific heat ratio of air
19 R=287; // Characteristic gas constant in J/kg K
20
21 p01=pa*(1+eff_ram*((1+Ci^2/(2*Cpa*Ta*10^3))^(r/(r-1)
    )-1));
22 p02=p01*rp;
23 T01=Ta+Ci^2/(2*Cpa*10^3);
24 T02=T01+T01*(rp^((r-1)/r)-1)/eff_c;
25 T04=T03-(Cpa*(T02-T01))/(Cpg*eff_m);
26 p03=p02-DelP_comb;
27 T_04=T03-(T03-T04)/eff_T;
28 p04=p03*(T_04/T03)^(r/(r-1));
29 p04_pc=1/(1-(((rg-1)/(rg+1))/eff_nozzle))^(rg/(rg-1)
    );
30 Tc=T04*(1/p04_pc)^((rg-1)/rg);
31 pc=p04/p04_pc;
32 row_c=(pc*10^5)/(R*Tc);
33 cj=sqrt (rg*R*Tc);
34 m=row_c*Ac*cj;
35 F=m*(cj-Ci)+Ac*(pc-pa)*10^5; // Total thrust
36 mf=(m*Cpg*(T03-T02))/(CV*10^3);
37 sfc=mf*3600/F; // specific fuel consumption
38
39 disp ("N (roundoff error)",F,"Total thrust = ");
40 disp ("kg/N h (roundoff error)",sfc,"specific fuel
    consumption = ");

```

---

Scilab code Exa 7.6 Calculation of specific power output

```
1  clc;
2  ci=600*1000/3600; // Velocity in m/s
3  Cpa=1.005; // Specific heat of air at constant
   pressure in kJ/kg K
4  Cpg=1.147; // Specific heat of fuel at constant
   pressure in kJ/kg K
5  rg=1.33; // Specific heat ratio of fuel
6  r=1.4; // Specific heat ratio of air
7  R=287; // Characteristic gas constant in J/kg K
8  pa=0.458; // Ambient pressure in bar
9  Ta=-15+273; // Ambient temperature in kelvin
10 rp=9; // pressure ratio
11 T03=1200; // Maximum temperature in kelvin
12 eff_ram=0.9; // Intake duct efficiency
13 eff_c=0.89; // Compressor efficiency
14 eff_T=0.93; // Turbine efficiency
15 eff_m=0.98; // Mechanical efficiency of transmission
16
17 cj=ci
18 T_01=Ta+(ci^2/(2*Cpa*10^3));
19 p_01=pa*(T_01/Ta)^(r/(r-1));
20 p01=eff_ram*(p_01-pa);
21 p02=rp*p01;
22 T01=T_01;
23 T_02=T01*rp^((r-1)/r);
24 T02=T01+(T_02-T01)/(eff_c);
25 T_04=T03*(1/rp)^((rg-1)/rg);
26 T04=T03-eff_T*(T03-T_04);
27 WN=Cpg*(T03-T04)-Cpa*(T02-T01)/eff_m; // net work
   done
28 eff_th=WN/(Cpg*(T03-T02)); // Thermal efficiency
29
```

```

30 disp ("kJ/kg (roundoff error)",WN,"Net work done =
      ");
31 disp ("%",eff_th*100,"Thermal efficiency = ");

```

---

### Scilab code Exa 7.7 Determination of rate of fuel consumption

```

1  clc;
2  pa=0.7; // Ambient pressure in bar
3  Ta=1+273; // Ambient temperature in kelvin
4  Ci=800*1000/3600; // Speed of the aircraft in m/s
5  rp=5; // Pressure ratio
6  eff_ram=1.00; // Intake duct efficiency
7  eff_c=0.85; // Compressor efficiency
8  eff_T=0.90; // Turbine efficiency
9  eff_comb=0.98; //Combustion efficiency
10 eff_nozzle=0.95; // Nozzle efficiency
11 rp_T=2.23; // Turbine pressure ratio
12 CV=43; // Low calorific value in MJ/kg
13 Cpa=1.005; // Specific heat of air at constant
      pressure in kJ/kg K
14 Cpg=1.005; // Specific heat of fuel at constant
      pressure in kJ/kg K
15 rg=1.4; // Specific heat ratio of fuel
16 r=1.4; // Specific heat ratio of air
17 R=287; // Characteristic gas constant in J/kg K
18 F=25000; // Thrust in N
19
20 cj=2*Ci;
21 T_01=Ta+(Ci^2/(2*Cpa*10^3));
22 T01=T_01;
23 T02=T01+(T01*((rp)^((r-1)/r))-1)/eff_c;
24 p_01=pa*(1+Ci^2/(2*Cpa*10^3*Ta))^(r/(r-1));
25 p01=eff_ram*(p_01-pa);
26 p02=rp*p01;
27 T03=(T02-T01)/(eff_T*(1-1/rp_T^((r-1)/r)));

```

```

28 ma=F/(cj-Ci);
29 // Neglecting the effect of the mass addition of
    fuel on the right hand side
30 mf=(ma*Cpa*(T03-T02))/(eff_comb*CV*10^3);
31
32 disp ("kg/s",ma,"Mass flow rate of air = ");
33 disp ("kg/s (roundoff error)",mf,"Mass flow rate
    of fuel = ");

```

---

### Scilab code Exa 7.8 Calculation of the take off thrust

```

1  clc;
2  Ta=288; // Ambient temperature in kelvin
3  pa=1.01; // Ambient pressure in bar
4  p04=2.4; // Stagnation pressure in bar
5  T04=1000; // Stagnation temperature in kelvin
6  m=23; // Mass flow rate in kg/s
7  rp=1.75; // Pressure ratio
8  eff_f=0.88 ; // Efficiency of the fan
9  eff_ft=0.9; // Efficiency of the fan turbine
10 Cpa=1.005; // Specific heat of air at constant
    pressure in kJ/kg K
11 Cpg=1.147; // Specific heat of fuel at constant
    pressure in kJ/kg K
12 rg=1.33; // Specific heat ratio of fuel
13 r=1.4; // Specific heat ratio of air
14 R=284.6; // Characteristic gas constant in J/kg K
15 T01=Ta;
16 p01=pa;
17 pc=p04*(2/(r+1))^(r/(r-1));
18 // since pc>pa the nozzle will choke
19 Tc=T04*(2/(r+1));
20 row_c=pc*10^5/(R*Tc);
21 cj=sqrt (r*R*Tc);
22 A=m/(row_c*cj);

```

```

23 p1=pa;
24 F=m*cj+(A*(pc-p1)*10^5);
25 // For fan engine
26 T_02=T01*(rp)^((r-1)/r);
27 T02=T01+(T_02-T01)/eff_f;
28 // For cold nozzle
29 m_nozzle=2*m; // Flow through cold nozzle
30 pc1=p01*rp*(2/(r+1))^(r/(r-1));
31 F_cold=m_nozzle*sqrt (2*Cpa*10^3*(T02-T01));
32 // Fan Turbine
33 T05=T04-((m_nozzle*Cpa*(T02-T01))/(m*Cpg));
34 T_05=T04-(T04-T05)/eff_ft;
35 p_05=p04*(T_05/T04)^(rg/(rg-1));
36 pc=p_05*(2/(rg+1))^(rg/(rg-1));
37 F_hot=m*sqrt (2*Cpg*10^3*(T05-T01));
38 Takeoffthrust= F_cold + F_hot;
39
40 disp ("m^2 (roundoff error)",A,"Nozzle Exit area =
      ");
41 disp ("N (roundoff error)",F,"Total Thrust = ");
42 disp ("N (roundoff error)",Takeoffthrust,"Take-off
      Thrust = ");

```

---

Scilab code Exa 7.9 Calculation of thrust provided by the engine and the thrust po

```

1 clc;
2 ma=18.2; // Massflow rater in m/s
3 Mi=0.6; // Mach number
4 pa=0.55; // Ambient pressure in bar
5 Ta=255; // Ambient temperature in kelvin
6 rp=5; // Pressure ratio
7 T03=1273; // Maximum temperature in kelvin
8 eff_c=0.81; // Compressor efficiency
9 eff_T=0.85; // Turbine efficiency
10 eff_nozzle=0.915; // Nozzle efficiency

```



```

11 eff_ram=0.9; // Intake duct efficiency
12 CV=45870; // Low calorific value in kJ/kg
13 Cpa=1.005; // Specific heat of air at constant
    pressure in kJ/kg K
14 Cpg=1.147; // Specific heat of fuel at constant
    pressure in kJ/kg K
15 rg=1.33; // Specific heat ratio of fuel
16 r=1.4; // Specific heat ratio of air
17 R=284.6; // Characteristic gas constant in J/kg K
18
19 ci=Mi*sqrt(r*R*Ta);
20 T_01=Ta+ci^2/(2*Cpa*10^3);
21 T01=T_01;
22 p_01=pa*(T01/Ta)^(r/(r-01));
23 p01=eff_ram*(p_01-pa)+pa;
24 p02=rp*p01;
25 T02=T01*(1+((rp^((r-1)/r))-1)/eff_c);
26 Wc=ma*Cpa*(T02-T01);
27 WT=Wc;
28 mf=ma/((CV/(Cpg*(T03-T02)))-1);
29 f1=mf/ma;
30 T04=T03-(WT/((ma+mf)*Cpg));
31 rp_T=(1/(1-((1-(T04/T03))/eff_T)))^(r/(r-1));
32 p03=p02;
33 p04=p03/rp_T;
34 p04_pc=1/(1-((rg-1)/((rg+1)*eff_nozzle)))^(rg/(rg-1)
    );
35 pc=p04_pc/p04;
36 Tc=T04*(1/p04_pc)^((rg-1)/rg);
37 cj=sqrt(r*R*Tc);
38 row_c=pc*10^5/(R*Tc);
39 An=(ma+mf)/(row_c*cj);
40 F=(ma+mf)*cj-ma*ci+An*(pc-pa);
41 Fp=F*ci;
42
43 disp ("kW (roundoff error)",Wc,"Work of
    compression = ");
44 disp ("kW (roundoff error)",WT,"Power output of

```

```

    the turbine = ");
45 disp (f1,"Fuel-Air ratio = ");
46 disp ("N    (roundoff error)",F,"Thrust = ");
47 disp ("kW    (roundoff error)",Fp/1000,"Thrust power
    = ");

```

---

Scilab code Exa 7.10 Calculation of exit speed of the gases and the thrust develop

```

1  clc;
2  ma=(12*10^4)/3600; // Air flow rate in kg/s
3  T01=15+273; // Temperature in kelvin
4  rp=4; // pressure ratio
5  p01=1.03; // Pressure in bar
6  T02=182+273; // Temperature in kelvin
7  T03=815+273; // Temperature in kelvin
8  T04=650+273; // Temperature in kelvin
9  ci=800*1000/3600; // Velocity in m/s
10 eff_nozzle=0.90; // Nozzle efficiency
11 Cpa=1.005; // Specific heat of air at constant
    pressure in kJ/kg K
12 Cpg=1.147; // Specific heat of fuel at constant
    pressure in kJ/kg K
13 rg=1.33; // Specific heat ratio of fuel
14 r=1.4; // Specific heat ratio of air
15 p03=4.12; // in bar
16
17 eff_c=1/((T02-T01)/(T01*((rp^((r-1)/r))-1)));
18 eff_T=eff_c;
19 Wc=ma*Cpa*(T02-T01);
20 rp_T=(1/(1-((T03-T04)/(eff_T*T03))))^((r/(r-1)));
21 p04=p03/rp_T;
22 p04_pc=1/(1-((rg-1)/((rg+1)*eff_nozzle)))^(rg/(rg-1)
    );
23 p5=p01;
24 T_5=T04*(p5/p04)^((rg-1)/rg);

```

```
25 T5=T04-eff_nozzle*(T04-T_5);
26 cj=sqrt(2*Cpg*10^3*(T04-T5));
27 F=ma*(cj-ci);
28
29 disp ("%",eff_c*100," Efficiency of the compressor =
    ");
30 disp ("%",eff_T*100," Efficiency of the Turbine = ");
31 disp ("kW",Wc," Compressor work = ");
32 disp ("m/s (roundoff error)",cj,"The exit speed of
    gases = ");
33 disp ("N (roundoff error)",F,"Thrust developed = "
    );
```

---

# Chapter 8

## Centrifugal Compressors

Scilab code Exa 8.1 Calculation of compressor efficiency

```
1  clc ;
2  N=11500; // Speed in rpm
3  T01=21+273; // Inlet total temperature in kelvin
4  p01=1; // Inlet total pressure in bar
5  p02=4; // Outlet total pressure in bar
6  D=0.75; // impeller diameter in m
7  mu=0.92; // slip factor
8  Cp=1.005; // specific heat at constant pressure in
   kJ/kg K
9  r=1.4; // Specific heat ratio
10
11 u=3.14*D*N/60;
12 W=mu*u^2;
13 T02=W/(Cp*10^3)+T01;
14 T_02=T01*(p02/p01)^((r-1)/r);
15 eff_c=(T_02-T01)/(T02-T01);
16
17 disp ("%",eff_c*100," Efficiency of the compressor =
   ");
```

---

Scilab code Exa 8.2 Estimation of the probable axial width of the impeller

```
1  clc;
2  m=35; // mass flow rate of air in kg/s
3  D=0.76; // Impeller diameter in m
4  N=11500; // speed in rpm
5  eff_c=0.8; // Efficiency of the compressor
6  rp=4.2; // Pressure ratio
7  cr=120; // Radial velocity in m/s
8  p01=1; // Inlet pressure in bar
9  T01=47+273; // Inlet temperature in kelvin
10 Cp=1.005; // specific heat at constant pressure in
    kJ/kg K
11 r=1.4; // Specific heat ratio
12 R=287; // Characteristic gas constant in J/kg K
13
14 T_02=T01*rp^((r-1)/r);
15 T02=T01+(T_02-T01)/eff_c;
16 // ignoring the effects of the velocity of flow
17 p02=rp/p01;
18 row2=p02*10^5/(R*T02);
19 Atip=m/(row2*cr);
20 AW=Atip/(3.14*D); // Axial width
21
22 disp ("cm",AW*100," Axial Width = ");
```

---

Scilab code Exa 8.3 Calculation of theoretical blade angles

```
1  clc;
2  D=0.15; // Inlet eye diameter in m
3  N=20000; // Speed in rpm
4  ca1=107; // Axial velocity in m/s
```

```

5 T01=294; // Inlet temperature in kelvin
6 p01=1.03; // Inlet pressure in kg/cm^2
7 Cp=1.005; // specific heat at constant pressure in
    kJ/kg K
8 r=1.4; // Specific heat ratio
9 R=287; // Characteristic gas constant in J/kg K
10
11 u1=3.14*D*N/60;
12 beta_1=atand (ca1/u1); // Blade angle
13 cr=u1/cosd (beta_1);
14 a=sqrt (r*R*(T01-ca1^2/(2*Cp*10^3)));
15 M=cr/a; // Mach number at the tip
16
17 disp ("degree",beta_1,"(i).Theoretical angle of the
    blade at this point = ");
18 disp (M,"(ii).Mach number of the flow at the tip of
    the eye = ");

```

---

**Scilab code Exa 8.4** Calculation of final temperature of the gases and the work done

```

1 clc;
2 T01=0+273; // Inlet gas temperature in kelvin
3 p01=0.7; // Inlet pressure in bar
4 p02=1.05; // Delivery pressure in bar
5 eff_c=0.83; // Compressor efficiency
6 Cp=1.005; // Specific heat at constant pressure in
    kJ/kg K
7 Cv=0.717; // Specific heat at constant volume in kJ
    /kg K
8 r=1.4; // Specific heat ratio
9
10 T_02=T01*(p02/p01)^((r-1)/r);
11 T02=T01+(T_02-T01)/eff_c; // Final temperature of
    the gas
12 Wc=Cp*(T02-T01); // Work of compression

```

```

13
14 // With additional compressor
15 T_03=T02*(p02/p01)^((r-1)/r);
16 T03=T02+(T_03-T02)/eff_c;
17 T_03=T01*(p02/p01)^(2*(r-1)/r);
18 eff_overall=(T_03-T01)/(T03-T01);
19
20 disp ("K",T02,"Final temperature of the gas = ");
21 disp ("kJ/kg",Wc,"Work of compression = ");
22 disp ("%",eff_overall*100,"Overall efficiency = ");

```

---

Scilab code Exa 8.5 Calculation of impeller diameters and the width at the impeller

```

1 clc;
2 N=12500; // Speed in rpm
3 m=15; // Mass flow rate in kg/s
4 rp=4; // Pressure ratio
5 eff_c=0.75; // Isentropic efficiency
6 mu=0.9; // Slip factor
7 pi=0.3; // Flow coefficient at impeller exit
8 D=0.15; // Hub diameter in m
9 ca2=150; // Axial velocity in m/s
10 T01=275; // Inlet temperature in kelvin
11 p01=1; // Inlet pressure in bar
12 Cp=1.005; // Specific heat at constant pressure in
    kJ/kg K
13 Cv=0.717; // Specific heat at constant volume in kJ
    /kg K
14 r=1.4; // Specific heat ratio
15 R=287; // Characteristic gas constant in J/kg K
16
17 u2=ca2/pi;
18 P=m*mu*u2^2/1000; // Power output
19 D2=u2*60/(3.14*N);
20 T1=T01-ca2^2/(2*Cp*10^3);

```

```

21 p1=p01*(T1/T01)^(r/(r-1));
22 row1=p1*10^5/(R*T1);
23 A1=m/(row1*ca2);
24 D1=sqrt ((A1*4/(3.14))+D^2);
25 p3_p1=rp;
26 p2=2*p1;
27 T_2=T1*(p2/p1)^((r-1)/r);
28 T2=T1+(T_2-T1)/eff_c;
29 row2=p2*10^5/(R*T2);
30 W2=(m)/(row2*ca2*3.14*D2);
31
32 disp ("kW",P,"Power = ");
33 disp (" Impeller Diameters");
34 disp ("cm",D2*100,"D2 = ", "cm    (roundoff error)",D1
    *100,"D1 = ");
35 disp (" Impeller width")
36 disp ("cm    (roundoff error)",W2*100,"W2 = ");

```

---

**Scilab code Exa 8.6** Calculation of the minimum possible depth of the diffuser

```

1  clc;
2  m=14; // mass flow rate in kg/s
3  rp=4; // pressure ratio
4  N=12000; // Speed in rpm
5  T01=288; // Inlet temperature in kelvin
6  p01=1.033; // Inlet pressure in bar
7  Cp=1.005; // Specific heat at constant pressure in
    kJ/kg K
8  Cv=0.717; // Specific heat at constant volume in kJ
    /kg K
9  r=1.4; // Specific heat ratio
10 R=287; // Characteristic gas constant in J/kg K
11 mu=0.9; // Slip factor
12 chi=1.04; // Power input factor
13 eff_c=0.8; // Compressor efficiency

```



```

14
15 T03=((rp^((r-1)/r))-1)*T01/eff_c)+T01;;
16 U=sqrt ((T03-T01)*Cp*10^3/(chi*mu));
17 D=U*60/(3.14*N);
18
19 T3=T03/1.2;
20 c2=sqrt (r*R*T3);
21 ca2=sqrt (c2^2-(mu*U)^2);
22 T02=eff_c*(T03-T01)+T01;
23 Loss=T03-T02;
24 T2=T3-Loss/2
25 p2=p01*(T2/T01)^(r/(r-1));
26 row2=p2*10^5/(R*T2);
27 A=m/(row2*ca2);
28 Depth=A/(2*3.14*D/2);
29
30 disp ("cm",D*100," Overall diameter of the Impeller
      = ");
31 disp ("cm (roundoff error)",Depth*100," Depth of
      the diffuser = ");

```

---

Scilab code Exa 8.7 Calculation of impeller and diffuser blade angles at inlet

```

1  clc;
2  N=10000; // Speed in rpm
3  Q=600; // Flow rate m^2/min
4  rp=4; // Pressure ratio
5  eff_c=0.82; // Compressor efficiency
6  T01=293; // Inlet temperature in kelvin
7  p01=1.0; // Inlet pressure in bar
8  Cp=1.005; // Specific heat at constant pressure in
      kJ/kg K
9  Cv=0.717; // Specific heat at constant volume in kJ
      /kg K
10 r=1.4; // Specific heat ratio

```

```

11 R=287; // Characteristic gas constant in J/kg K
12 ca=60; // Axial velocity in m/s
13 D2_D1=2 ;// Diameter ratio
14
15 T_03=T01*rp^((r-1)/r);
16 T03=T01+(T_03-T01)/eff_c;
17 u2=sqrt (Cp*10^3*(T03-T01));
18 Wc=u2^2; // Work of compression
19 D2=(u2*60/(3.14*N));
20 D1=D2/D2_D1;
21 T1=T01-(ca^2/(2-Cp*10^3));
22 p1=p01*(T1/T01)^(r/(r-1));
23 row1=p1*10^5/(R*T1);
24 Wroot=(Q/60)*(1/(ca*3.14*D1));
25 u1=3.14*N*D1/60;
26 alpha_root=atand (ca/u1);
27 alpha_tip= atand (ca/u2);
28
29 disp ("(i).Power input ");
30 disp ("kW/kg/s",Wc/1000,"Wc = ");
31 disp ("(ii).Impeller Diameters");
32 disp ("m",D2,"D2 = ", "m",D1,"D1 = ");
33 disp ("(iii).Impeller and diffuser blade angles at
inlet");
34 disp ("degree",alpha_tip,"alpha_tip = ", "degree",
alpha_root,"alpha_root = ");

```

---

### Scilab code Exa 8.8 Calculation of slip factor

```

1 clc;
2 rp=4; // Pressure ratio
3 eff_c=0.8; // Compressor efficiency
4 N=15000; // Speed in rpm
5 T01=293; // Inlet temperature in kelvin
6 De=0.25; // Diameter of eye in m

```

```

7 C1=150; // Absolute velocity in m/s
8 Di=0.6; // Impeller diameter in m
9 a1=25; // in degree
10 Cp=1.005; // Specific heat at constant pressure in
    kJ/kg K
11 Cv=0.717; // Specific heat at constant volume in kJ
    /kg K
12 r=1.4; // Specific heat ratio
13 R=287; // Characteristic gas constant in J/kg K
14
15 T02=T01*rp^((r-1)/r);
16 DelT_actual=(T02-T01)/eff_c;
17 P=Cp*10^3*DelT_actual; // Power input
18 u1=3.14*De*N/60;
19 ct1=C1*sind (a1);
20 // At Exit
21 u2=3.14*Di*N/60;
22 ct2=(P+(u1*ct1))/u2;
23 mu=ct2/u2; // Slip factor
24
25 disp (mu," Slip Factor = ");

```

---

Scilab code Exa 8.9 Determination of number of radial impeller vanes

```

1 clc;
2 P=180*10^3; // Power input in J
3 N=15000; // Speed in rpm
4 a1=25; // in degrees
5 De=0.25; // Mean dia of the eye in m
6 Di=0.6; // Impeller tip diameter in m
7 c1=150; // Absolute air velocity at inlet in m/s
8
9 u1=3.14*De*N/60;
10 u2=3.14*Di*N/60;
11 ct1=c1*sind (a1);

```

```

12 ct2=(P+(u1*ct1))/u2;
13 mu=ct2/u2;
14 z=(1.98)/(1-mu); // Number of impeller vanes
15 disp(z,"Number of impeller vanes using Stanitz
    formulae = ");

```

---

Scilab code Exa 8.10 Calculation of the torque power required and the head develop

```

1  clc;
2  m=30; // mass flow rate in kg/s
3  N=15000; // Speed in rpm
4  r2=0.3; // Radius in m
5  D2=r2*2; // Diameter in m
6  w2=100; // Relative velocity in m/s
7  beta_1=80; // in degrees
8  p01=1; // Inlet pressure in bar
9  T01=300 // Inlet temperature in kelvin
10 Cp=1.005; // specific heat at constant pressure in
    kJ/kg K
11 r=1.4; // Specific heat ratio
12 R=287; // Characteristic gas constant in J/kg K
13
14 u2=3.14*D2*N/60;
15 ct2=u2-(w2*cosd(beta_1));
16 Fr=m*ct2*r2;
17 P=Fr*(2*3.14*N/60);
18 W=u2*ct2;
19 P02=p01*(1+(W*10^-3/(Cp*T01)))^(r/(r-1));
20
21 disp ("Nm" ,Fr," Torque = ");
22 disp ("kW" ,P/1000," Power = ");
23 disp ("bar" ,P02," Head Developed = ");

```

---

# Chapter 9

## Axial Flow Compressors

Scilab code Exa 9.1 Estimation of blade angles

```
1  clc;
2  n=10; // No of stages in the axial flow compressor
3  rp=5; // Overall pressure ratio
4  eff_C=0.87; // Overall isentropic efficiency
5  T1=15+273; // Temperature of air at inlet in kelvin
6  u=210; // Blade speed in m/s
7  ca=170; // Axial velocity in m/s
8  wf=1; // Work factor
9  r=1.33; // Specific heat ratio
10 Cp=1.005; // Specific heat in kJ/kg K
11
12 Del_Tstage=(T1*(rp^((r-1)/r)-1))/(n*eff_C); //
    Temperature increase per stage
13 // By property relations and let us assume
14 // tan_beta1-tan_beta2=Del_Tstage*Cp/(wf*u*ca)
15 // tan_beta1+tan_beta2=u/ca for 50% reaction
16 // To solve this above equations using matrix method
17 a=[1, -1; 1, 1]; c=[(Del_Tstage*Cp*10^3/(wf*u*ca)); u/ca
    ];
18 b=a\c;
19 beta1=atand(b(1)); // Blade angles at inlet
```

```

20 beta2=atand(b(2)); // Blade angles at outlet
21
22 disp ("degree (roundoff error)",beta2,"Blade angle
    at outlet = ", "degree (roundoff error)",beta1,
    "Blade angle at inlet = ");

```

---

Scilab code Exa 9.2 Calculation of mass flow rate and degree of reaction

```

1  clc;
2  P1=1.0132; // Inlet air pressure in bar
3  T01=288; // Inlet air temperature in kelvin
4  ca=150; // axial velocity in m/s
5  dtip=60; // Tip diameter of rotor in cm
6  dhub=50; // Hub diameter of rotor in cm
7  N=100; // Speed of rotor in rps
8  t_angle=30; // Deflected angle of air in degree (in
    question it is 30.2 but in solution it is 30)
9  P2_P1=1.2; // Stage pressure ratio
10 Cp=1005; // Specific heat in J/kg K
11 r=1.4; // Specific heat ratio
12 R=287; // Characteristic gas constant in J/kg K
13
14 u=(3.142857*(dhub+dtip)*10^-2*N)/2; // Mean blade
    velocity
15 beta_1=atand(u/ca); // Blade angle at inlet
16 beta_2=beta_1-t_angle; // As air is deflected by 30
17 // from velocity triangle
18 x=ca*tand(beta_2);
19 alpha_2=atand ((u-x)/ca);
20 C1=ca;
21 T1=T01-(C1^2/(2*Cp)); // Static temperature at inlet
22 P2=P1*P2_P1; // Pressure at outlet
23 T2=T1*(P2/P1)^((r-1)/r); // Static temperature at
    outlet
24 row_2=(P2*10^5)/(R*T2); // Density at outlet

```

```

25 m=3.14*(dtip^2-dhub^2)*ca*row_2*10^-4/4; // Mass
    flow rate
26 wf=1; // Work factor
27 P=wf*u*ca*m*(tand(beta_1)-tand(beta_2))/1000; //
    Power developed
28 R=ca*(tand(beta_1)+tand(beta_2))/(2*u); // Degree of
    reaction
29
30 disp ("kg/s",m,"Mass flow rate = ");
31 disp ("kW (Error due to more decimal values in
    expression)",P,"Power developed = ");
32 disp (R,"Degree of Reaction = ");

```

---

### Scilab code Exa 9.3 Estimation of number of stages of the compressors

```

1  clc;
2  beta_1=45; // Inlet blade angle in degree
3  beta_2=10; // Outlet blade angle in degree
4  rp=6; // Compressor pressure ratio
5  eff_C=0.85; // Overall isentropic efficiency
6  T1=37+273; // Inlet static temperature in kelvin
7  u=200; // Blade speed in m/s
8  Cp=1005; // Specific heat in J/kg K
9  r=1.4; // Specific heat ratio
10 R=287; // Characteristic gas constant in J/kg K
11
12 // (i). wf=1
13 wf=1; // Work factor
14 ca=u/(tand(beta_1)+tand(beta_2)); // Axial velocity
15 Del_Tstage=wf*u*ca*(tand(beta_1)-tand(beta_2))/Cp;
    // Stage temperature drop
16 Del_Toverall=(T1*(rp^((r-1)/r)-1))/eff_C; // Overall
    temperature drop
17 n=Del_Toverall/Del_Tstage; // No of stages
18

```

```

19 disp (n,"Number of stages required = ", "(i).wf = 1")
    ;
20
21 // (ii).wf = 0.87
22 wf =0.87; // Work factor
23 ca=u/(tand(beta_1)+tand(beta_2)); // Axial velocity
24 Del_Tstage=wf*u*ca*(tand(beta_1)-tand(beta_2))/Cp;
    // Stage temperature drop
25 Del_Toverall=T1*(rp^((r-1)/r)-1)/eff_C; // Overall
    temperature drop
26 n=Del_Toverall/Del_Tstage; // No of stages
27
28 disp (n,"Number of stages required = ", "(ii).wf =
    0.87");

```

---

**Scilab code Exa 9.4** Determination of Mach number relative to Rotor

```

1 clc;
2 rp=4; // Total head pressure ratio
3 eff_0=0.85; // Overall total head isentropic
    efficiency
4 T01=290; // Total head inlet temperature in kelvin
5 alpha_1=10; // Inlet air angle in degree
6 alpha_2=45; // Outlet air angle in degree
7 u=220; // Blade velocity in m/s
8 wf=0.86; // Wok done factor
9 R=284.6; // Characteristic gas constant in kJ/kg K
10 Cp=1005; // Specific heat in J/kg K
11 r=1.4; // Specific heat ratio
12
13 eff_P=1/(log10(((rp^((r-1)/r)-1)/eff_0)+1)/(log10(rp
    )*((r-1)/r))));
14 // From velocity triangle
15 ca=u/(tand(alpha_1)+tand(alpha_2)); // Axial
    velocity

```



```

16 Del_Tstage=wf*u*ca*(tand(alpha_2)-tand(alpha_1))/Cp;
    // Stage temperature rise
17 T02=T01*(rp)^((r-1)/(r*eff_P)); // Total head
    temperature
18 T02_T01=T02-T01; // Total temperature rise
19 n=T02_T01/Del_Tstage; // Total number of stages
20 // from velocity triangles
21 w1=ca/cosd(alpha_2);
22 c1=ca/cosd(alpha_1);
23 T1=T01-c1^2/(2*Cp); // Static temperature
24 M=w1/sqrt(r*R*T1); // Mach number at inlet
25
26 disp (eff_P*100,"Polytropic efficiency of the
    compressor = ");
27 disp (n,"Total number of stages = ");
28 disp (M,"Mach number at inlet = ");

```

---

Scilab code Exa 9.5 Calculation of pressure rise per blade ring and the power input

```

1 clc;
2 Q=1000; // Flow rate of free air in m^3/min
3 P1=0.98; // Inlet pressure in bar
4 T1=15+273; // Inlet temperature in kelvin
5 Dm=0.6; // Mean diameter in m
6 h=6.75; // blade length in cm
7 CL=0.6; CD=0.05; // At zero angle of incidence
8 Cp=1.005; // Specific heat in kJ/kg K
9 r=1.4; // Specific heat ratio
10 R=287; // Characteristic gas constant in J/kg K
11 k=1-0.1; // Blade occupies 10% of axial area
12 N=6000; // speed in rpm
13 Ac=19.25*10^-4; // Projected area in m^2
14 n=50;
15 eff_C=1; // Efficiency of compressor
16

```

```

17 row=(P1*10^5)/(R*T1); // Density
18 A=k*3.14*Dm*h*10^-2; // Area of axial
19 ca=Q/(60*A); // Axial velocity
20 u=3.14*Dm*N/60; // Blade velocity
21 beta_1=atand(u/ca); // Blade angle at inlet
22 w=sqrt(ca^2+u^2); // From velocity triangle
23 L=CL*row*w^2*Ac/2;
24 D=CD*row*w^2*Ac/2;
25 P=(L*cosd(beta_1)+D*sind(beta_1))*u*n*10^-3; //
    Power input / stage
26 m=Q*row/60; // mass flow rate
27 rp=((P*eff_C/(m*Cp*T1))+1)^(r/(r-1)); // pressure
    ratio
28 P2=rp*P1; // Pressure
29
30 disp ("kW (Roundoff error)",P,"Power input/stage
    = ");
31 disp ("bar",P2,"Pressure at outlet = ");

```

---

Scilab code Exa 9.6 Determination of the direction of the air entry to and exit from

```

1 clc;
2 T1=290; // Temperature at inlet in kelvin
3 n=10; // Number of stages
4 rp=6.5; // Pressure ratio
5 m=3; // mass flow rate in kg/s
6 eff_C=0.9; // isentropic efficiency of the
    compression
7 ca=110; // Axial velocity in m/s
8 u=180; // Mean blade velocity in m/s
9 Cp=1.005; // Specific heat in kJ/kg K
10 r=1.4; // Specific heat ratio
11 R=287; // Characteristic gas constant in J/kg K
12
13 T_2=(rp)^((r-1)/r)*T1; // temperature after

```

```

    isentropic compression
14 T2=((T_2-T1)/eff_C)+T1; // Temperature after actual
    compression
15 P=m*Cp*(T2-T1); // Power given to the air
16 Del_Tstage=(T2-T1)/n; // Temperature rise per stage
17 Del_ct=Cp*10^3*Del_Tstage/u; // For work done per kg
    of air per second
18 // To find blade angles let solve the following
    equations
19 // Del_ct=ca(tan beta_1-tan beta_2) for symmetrical
    stages
20 // u=ca(tan beta_1=tan beta_2) for degree of
    reaction = 0.5
21 // Solving by matrix method
22 A=[1, -1; 1, 1]; C=[Del_ct/ca; u/ca];
23 B=A\C;
24 // Blade angles at entry and exit
25 beta_1=atand(B(1));
26 beta_2=atand(B(2));
27
28 disp ("kW (roundoff error)",P,"Power given to the
    air = ");
29 disp ("degree",beta_2,"Blade angle at exit = ","
    degree",beta_1,"Blade angle at inlet = ");

```

---

**Scilab code Exa 9.7** Calculation of the rotational speed and the length of the last

```

1 clc;
2 rp=4; // Overall pressure ratio
3 m=3; // mass flow rate in kg/s
4 eff_pc=0.88; // Polytropic efficiency
5 Del_Tstage=25; // The stagnation temperature
    pressure rise in kelvin
6 c1=165; // Absolute velocity in m/s
7 alpha_1=20; // air angle from axial direction in

```

```

        degree
8 wf=0.83; // Workdone factor
9 D=18; // Mean diameter of the last stage rotor in cm
10 P01=1.01; // Ambient pressure in bar
11 T01=288; // Ambient temperature in kelvin
12 Cp=1005; // Specific heat in J/kg K
13 r=1.4; // Specific heat ratio
14 R=287; // Characteristic gas constant in J/kg K
15
16 n=1/(1-(r-1)/(r*eff_pc));
17 T02=T01*(rp)^((n-1)/n); // Total pressure at stage 2
18 Del_Toverall= T02-T01; // Overall temperature
    difference
19 Ns=Del_Toverall/Del_Tstage; // Number of stages
20 eff_C=((rp^((r-1)/r)-1)/(rp^((r-1)/(r*eff_pc))-1));
    // Efficiency of compressor
21 rp1=(1+(eff_C*Del_Tstage/T01))^(r/(r-1)); //
    Pressure ratio across first stage
22 Del_Tstage1=Del_Toverall/Ns; // Temperature rise
    across stage 1
23 T01s=T02-Del_Tstage1; // Temperature at inlet to
    last stage
24 rpl1=(1+(eff_C*Del_Tstage1/T01s))^(r/(r-1)); //
    Pressure ratio across last stage
25 // For symmetrical blade, R=0.5
26 beta_2=alpha_1;
27 ca=c1*cosd(alpha_1); // Axial velocity
28 beta_1=atand(sqrt(((Cp*Del_Tstage1/(wf*ca))/ca)+(
    tand(beta_2))^2)); // blade angle
29 u=ca*(tand(beta_1)+tand(beta_2)); // mean velocity
    of blade
30 N=60*u/(3.14*D*10^-2*60); // Speed in rps
31 Po=rp/rpl1; // Total pressure at inlet to the last
    stage
32 T0=T01s; // Total temperature to the last stage
33 Tst=T0-c1^2/(2*Cp); // Static temperature
34 Pst=Po/(T0/Tst)^((r-1)/r); // Static pressure
35 row=(Pst*10^5)/(R*Tst); // Density

```

```

36 h=m/(ca*row*3.14*D*10^-2); // Length of last stage
37
38 disp (Ns,"Number of stages = ");
39 disp (rp1,"Pressure ratio across first stage = ");
40 disp (" (roundoff error)",rpls,"Temperature at
inlet to last stage = ");
41 disp ("degree (roundoff error)",beta_1,"beta1=" );
42 disp ("rps (roundoff error)",N,"Speed = ");
43 disp ("cm (roundoff error)",h*100,"Length of last
stage = ");

```

---

Scilab code Exa 9.8 Calculation of the stage stagnation pressure ratio and the power

```

1 clc;
2 N=6000; // Speed in rpm
3 Del_rise=20; // Stagnation temperature rise in
kelvin
4 wf=0.93; // Work done factor eff_c=0.89; //
Isentropic efficiency of the state
5 c1=140; // Inlet velocity in m/s
6 p01=1.01; // Ambient pressure in bar
7 T01=288; // Ambient temperature in kelvin
8 M1=0.95; // Mach number
9 Cp=1.005; // Specific heat in J/kg K
10 r=1.4; // Specific heat ratio
11 R=287; // Characteristic gas constant in J/kg K
12 H_T_ratio=0.6; // Hub tip ratio in
13 eff_s=0.89; // Stage efficiency
14 T1=T01-c1^2/(2*Cp*10^3);
15 w1=M1*sqrt (r*R*T1);
16 beta_1=acosd (c1/w1);
17 u=w1*sind (beta_1);
18 beta_2=atand (tand(beta_1)-((Cp*10^3*Del_rise)/(u*wf
*c1)));
19 p1=p01/(T01/T1)^(r/(r-1));

```

```

20 row_1=(p1*10^5)/(R*T1);
21 Rtip=60*u/(2*3.14*N);
22 Rroot=H_T_ratio*Rtip;
23 Rm=(Rtip+Rroot)/2;
24 h=Rtip-Rroot;
25 m=row_1*2*3.14*Rm*h*c1;
26 rp=(1+(eff_s*Del_rise)/(T01))^(r/(r-1));
27 P=m*Cp*Del_rise;
28 uroot=2*3.14*Rroot*N/60;
29 beta_1root=atand (uroot/c1);
30 beta_2root=atand (tand (beta_1root)-((Cp*10^3*
    Del_rise)/(wf*uroot*c1)));
31
32 disp ("degree",beta_2,"beta 2 = ","degree",beta_1,"
    beta 1 = ","Rotor air angles at tip:","m",Rtip,"
    Tip Radius = ","(i).");
33 disp ("kg/s (Roundoff error)",m,"Mass flow rate =
    ","(ii).");
34 disp ("kW",P,"Power input = ",rp,"Stagnation
    pressure ratio = ","(iii).");
35 disp ("degree",beta_2root,"beta 2 = ","degree",
    beta_1root,"beta 1 = ","Rotor air angles at root
    sections","(iv).");

```

---

Scilab code Exa 9.9 Determination of the stage efficiency and the work done factor

```

1 clc;
2 rp=1.35; // Actual pressure ratio
3 DelT_rise=30; // Actual temperature rise in K
4 beta_1=47; // Inlet blade angle in degree
5 beta_2=15; // Outlet blade angle in degree
6 u=225; // Peripheral velocity in m/s
7 ca=180; // Axial velocity in m/s
8 T01=27+273; // Ambient temperature in kelvin
9 Cp=1.005; // Specific heat in KJ/kg K

```

```

10 r=1.4; // Specific heat ratio
11 R=287; // Characteristic gas constant in J/kg K
12
13 eff_s=(rp^((r-1)/r)-1)*T01/DelT_rise;
14 wf=(DelT_rise*Cp*10^3)/(u*ca*(tand(beta_1)-tand(
    beta_2)));
15
16 disp ("%","eff_s*100,"Stage Efficiency = ");
17 disp (wf,"Work done factor = ");

```

---

#### Scilab code Exa 9.10 Determination of blade and air angle

```

1 clc;
2 u=250; // Mean blade speed in m/s
3 rp=1.3; // Pressure ratio
4 ca=200; // Axial velocity in m/s
5 p01=1; // Inlet pressure in bar
6 T01=300; // Inlet temperature in kelvin
7 R1=0.5; // Degree of reaction
8 Cp=1.005; // Specific heat in KJ/kg K
9 r=1.4; // Specific heat ratio
10 R=287; // Characteristic gas constant in J/kg K
11
12 Del_T=(rp^((r-1)/r)-1)*T01;
13 //tan_beta1+tan_beta2=(R*2*u/ca);
14 //tan_beta1-tan_beta2=(Del_T*Cp*10^3/(u*ca));
15 A=[1 1;1 -1]; B=[(R1*2*u/ca) ;(Del_T*Cp*10^3/(u*ca))
    ];
16 tan_beta=A\B;
17 beta_1=atand (tan_beta(1));
18 beta_2=atand (tan_beta(2));
19 alpha_1=beta_2; alpha_2=beta_1;
20
21 disp ("degree",beta_2,"beta2 = ","degree",beta_1,"
    beta1 = ");

```

```

22 disp ("degree",alpha_2,"alpha2 = ", "degree",alpha_1,
        "alpha1 = ");

```

---

### Scilab code Exa 9.11 Calculation of rotational speed

```

1  clc;
2  n=4; // Number of stage
3  rp=10; // Pressure ratio
4  eff_p_ac=0.92; // Ploytropic efficiency of axial
        compressor
5  eff_p_cc=0.83; // Polytropic efficiency of
        centrifugal compressor
6  Del_Trise=30; // Axial compressor stage temperature
        in kelvin
7  R=0.5; // Reaction stage
8  beta_2=20; // Outlet stator angle in degree
9  D=0.25; // Mean diameter of each stage in m
10 wf=0.8; // Work done factor
11 ca=150; // Axial velocity in m/s
12 Di=0.33; //Impeller diameter in m
13 mu=0.9; // Slip factor
14 p01=1.01; // Ambient pressure in bar
15 T01=288; // Ambient temperature in kelvin
16 pif=1.04; // Power input factor
17 Cp=1.005; // Specific heat in KJ/kg K
18 r=1.4; // Specific heat ratio
19 R=287; // Characteristic gas constant in J/kg K
20
21 beta_1=atand (sqrt ((Cp*10^3*Del_Trise/(wf*ca^2))+
        tand(beta_2)^2));
22 u=ca*(tand (beta_1)+tand(beta_2));
23 Nac=(u/(3.14*D));
24 r1=(1+n*Del_Trise/T01)^(eff_p_ac*r/(r-1)); // Total
        pressure ratio across the axial compressor
25

```



```
26 r2=rp/r1; // Pressure ratio across centrifugal
    compressor
27 T02=T01*r1^((r-1)/(eff_p_ac*r));
28 T03=T02*r2^((r-1)/(eff_p_cc*r));
29 Del_Tsc=T03-T02;
30 u=sqrt ((Del_Tsc*Cp*10^3)/(pif*mu));
31 Ncc=u/(3.14*Di);
32
33 disp ("rps (roundoff error)",Nac,"Speed of the
    axial compressor = ");
34 disp ("rps (roundoff error)",Ncc,"Speed of the
    centrifugal compressor = ");
```

---

# Chapter 11

## Impulse and Reaction Turbines

Scilab code Exa 11.1 Estimation of maximum number of stages required

```
1  clc;
2  p02=6; // Inlet pressure in bar
3  T02=900; // Inlet temperature in kelvin
4  p0fs=1; // Outlet pressure in bar
5  eff_isenT=0.85; // isentropic efficiency of turbine
6  alpha_2=75; // Nozzle outlet angle in degree
7  u=250; // Mean blade velocity in m/s
8  Cp=1.15*10^3; // Specific heat in J/ kg K
9  r=1.333; // Specific heat ratio
10
11  T0fs=T02/(p02/p0fs)^((r-1)/r); // Isentropic
    temperature at the exit of the final stage
12  Del_Toverall=eff_isenT*(T02-T0fs); // Actual overall
    temperature drop
13  c2=2*u/sind (alpha_2); // absolute velocity
14  c3= c2*cosd (alpha_2); // absolute velocity
15  c1=c3; // From velocity triangles
16  Del_Tstage=(c2^2-c1^2)/(2*Cp); // Stage temperature
    drop
17  n=Del_Toverall/Del_Tstage; // Number of stages
18
```

```
19 disp (round (n), "Number of stages n =");
```

---

Scilab code Exa 11.2 Determination of output power developed by the turbine shaft

```
1 clc;
2 N=10000; // Speed of gas turbine in rpm
3 T01=700+273.15; // Total head temperature at nozzle
   entry in kelvin
4 P01=4.5; // Total head pressure at nozzle entry in
   bar
5 P02=2.6; // Outlet pressure from nozzle in bar
6 p3=1.5; // Pressure at turbine outlet annulus in bar
7 M=0.5; // Mach number at outlet
8 alpha_2=70; // outlet nozzle angle in degrees
9 D=64; // Blade mean diameter in cm
10 m=22.5; // Mass flow rate in kg/s
11 eff_T=0.99; // turbine mechanical efficiency
12 Cp=1.147; // Specific heat in kJ/kg K
13 r=1.33; // Specific heat ratio
14 fl=0.03; // frictional loss
15 R=284.6; // characteristic gas constant in J/kg K
16
17 eff_N=1-fl; // Nozzle efficiency
18 T_02=(P02/P01)^((r-1)/r)*T01; // Isentropic
   temperature after expansion
19 T02=T01-eff_N*(T01-T_02); // Actual temperature
   after expansion
20 c2=sqrt (2*Cp*10^3*(T01-T02)); // Absolute velocity
21 u=(3.14*D*10^-2*N)/60; // Mean blade velocity
22 // From velocity triangles
23 wt2=c2*sind (alpha_2)-u;
24 ca=c2*cosd (alpha_2);
25 beta_2=atand((wt2)/ca);
26 T3=T02/(P02/p3)^((r-1)/r); // Assuming rotor losses
   are negligible
```

```

27 c3=M*sqrt (r*R*T3); // Absolute velocity
28 beta_3=atand(u/c3);
29 ct2=c2*sind(alpha_2);
30 P=eff_T*m*(ct2)*u/1000; // Power developed
31
32 disp ("degree",beta_3,"Gas angle at exit = ", "degree
      ",beta_2,"Gas angle at entry", "(i).");
33 disp ("kW (roundoff error)",P,"Power developed = "
      ,(ii).");

```

---

Scilab code Exa 11.3 Estimation of the blade angle and power produced

```

1 clc;
2 alpha_2=65; // Nozzle discharge angle in degree
3 c3=300; // Absolute velocity in m/s
4 alpha_3=30; // in degrees
5
6 ca2=c3*cosd (alpha_3); // Axial velocity
7 c2=ca2/cosd(alpha_2); // Absolute velocity
8 // ca3=ca2=ca and equal blade angles then
9 ca=ca2;
10 beta_2=atand((c2*sind(alpha_2)+c3*sind(alpha_3))/(2*
      ca)); // Blade angle
11 beta_3=beta_2; // equal blade angles
12 u=c2*sind(alpha_2)-ca2*tand(beta_2); // Mean blade
      velocity
13 // From velocity triangles
14 ct2=c2*sind(alpha_2);
15 ct3=c3*sind(alpha_3);
16 WT=u*(ct2+ct3)/1000; // Work done
17 sigma=u/c2; // optimum speed ratio
18 eff_B=4*(sigma*sind(alpha_2)-sigma^2);
19
20 disp ("degree",beta_2,"Blade angle = beta_2= beta_3
      = ");

```

```

21 disp ("kJ/kg (roundoff error)",WT,"Power Produced
    = ");
22 disp ("%",eff_B*100,"Blade efficiency = ");

```

---

Scilab code Exa 11.4 Calculation of blade angle used and the mass flow rate required

```

1  clc;
2  P01=7; // Pressure at inlet in bar
3  T01=300+273.15; // Temperature at inlet in kelvin
4  P02=3; // Pressure at outlet in bar
5  alpha_2=70; // Nozzle angle in degree
6  eff_N=0.9; // Isentropic efficiency of nozzle
7  WT=75; // Power Produced in kW
8  Cp=1.15; // Specific heat in kJ/kg K
9  r=1.33; // Specific heat ratio
10
11 T_02=T01*(P02/P01)^((r-1)/r); // Isentropic
    temperature after expansion
12 T02=T01-eff_N*(T01-T_02); // Actual temperature
    after expansion
13 c2=sqrt (2*Cp*10^3*(T01-T02)); // Absolute velocity
14 // For optimum blade speed ratio
15 u=(c2*sind (alpha_2)/2); // Mean blade velocity
16 beta_2=atand((c2*sind(alpha_2)-u)/(c2*cosd(alpha_2))
    ); // Blade angle
17 // From velocity triangles
18 ct2=c2*sind(alpha_2);
19 w2=c2*cosd(alpha_2)/cosd(beta_2);
20 w3=w2; // Equal inlet and outlet angles
21 beta_3=54; // in degrees
22 ct3=w3*sind(beta_3)-u;
23 m=(WT*10^3)/(u*(ct2+ct3)); // Gas mass flow rate
24
25 disp ("degree",beta_2,"Blade angle = ");
26 disp ("kg/s",m,"Gas Mass Flow Rate = ");

```

---

Scilab code Exa 11.5 Determination of gas temperature velocities and discharge angle

```
1  clc;
2  P01=4.6; // Total head inlet pressure in bar
3  T01=700+273.15; // Total head inlet temperature in
   kelvin
4  P2=1.6; // Static head pressure at mean radius in
   bar
5  Dm_h=10; // Mean blade diameter/blade height
6  lc=0.1; // Nozzle losses coefficient
7  alpha_2=60; // Nozzle outlet angle in degree
8  Cp=1.147; // Specific heat in kJ/kg K
9  r=1.33; // Specific heat ratio
10 m=20; // Mass flow rate in kg/s
11 R=284.6; // characteristic gas constant in J/kg K
12
13 T_2=T01*(P2/P01)^((r-1)/r); // Isentropic
   temperature after expansion
14 T2=(lc*T01+T_2)/(1+lc); // Actual temperature after
   expansion
15 c2=sqrt(2*Cp*10^3*(T01-T2)); // Absolute velocity
16 // From velocity triangles
17 ca=c2*cosd(alpha_2);
18 row=P2*10^5/(R*T2); // Density of gas
19 A=m/(ca*row); // Area
20 Dm=sqrt(A*Dm_h/3.14); // Mean Diameter
21 h=Dm/10; // Blade height
22 rm=Dm/2; // Mean radius
23 // At root
24 r_root=(Dm-h)/2;
25 //At the tip
26 r_tip=(Dm+h)/2;
27 // Free vorte flow
28 ct_mean=c2*sind(alpha_2);
```

```

29 // At the root
30 ct2_root=(ct_mean*rm)/r_root;
31 alpha2_root=atand(ct2_root/ca);
32 c2_root=ct2_root/sind (alpha2_root);
33 T2_root=T01-c2_root^2/(2*Cp*10^3);
34 // At the tip
35 ct2_tip=ct_mean*rm/r_tip;
36 alpha2_tip = atand (ct2_tip/ca);
37 c2_tip=ct2_tip/sind(alpha2_tip);
38 T2_tip=T01-c2_tip^2/(2*Cp*10^3);
39
40 disp ("degree",alpha2_root," Discharge angle at the
      root = ", "m/s",c2_root," Gas velocity at the root
      = ", "K",T2_root," Gas Temperature at the root = ",
      "A the Root");
41 disp ("degree",alpha2_tip," Discharge angle at the
      tip = ", "m/s",c2_tip," Gas velocity at the tip = "
      ,"K",T2_tip," Gas Temperature at the tip = ", "A
      the tip");

```

---