Scilab Manual for Digital Signal Processing Lab by Dr R Kumaraswamy Electronics Engineering Siddaganga Institute Of Technology¹

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Experiment: 1 Discrete-time signals

Scilab code Solution 1.1 Representation of discrete time signals

```
1
2 //scilab 5.5.2 ,OS: Ubuntu 14.04
3 //Generation of signals
4
5 //Unit Sample Sequence
6 clear ;clc ;close ;
7 L = 4;
                                          // \text{length} = 2*L+1
8 n = -L:L;
                                          // Time index
      vector
9 x = [zeros(1,L), 1, zeros(1,L)];
10 figure (1);
11 subplot(421),plot2d3(n,x),xtitle('Unit Sample
      sequence', n', x_1[n]');
12
13 //Unit step function
14 //clear ;clc ;close ;
15 n1=0:5
16 x1=[ones(1,6)];
17 subplot(422),plot2d3(n1,x1),xtitle('Unit Step
      sequence', 'n', 'x_2[n]')
18 //figure(1); plot2d3(n,x);
```

```
19 //xtitle('Discrete Unit Step Sequence', 'n', 'x[n]');
20
21 //Unit ramp function
22 //clear ;clc ;close ;
23 L = 4;
                                        // Length of the
      sequence
24 n2 = -L : L;
25 x2= [zeros(1,L),0:L];
26 , subplot (423), plot2d3(n2,x2), xtitle('Unit Ramp
      sequence', 'n', 'x_2[n]')
27 / plot 2 d 3 (n, x);
  //xtitle(' Discrete Unit Ramp Sequence', 'n', 'x[n]')
28
29
30 //Discrete time Exponential signal
31 //clear ;clc ;close ;
             //For decreasing a<1 and For increasing
32 a = 0.5;
      exponential a>1
33 n3 = 0:10;
34 x3 = (a).^{n3};
35 subplot(424),plot2d3(n3,x3),xtitle('Exponential
      Sequence', 'n', 'x_3[n]')
  //plot2d3(n,x); xtitle('Exponentially Decreasing
36
      Signal ', 'n', 'x[n]');
37
38
39
40 //Sinusoidal signal
41 // clc ; clear ;
42 fm=100; // Frequency 100 Hz or input ('Enter the input
       signal frequency:');
                                          //100
43 k=3;// Number of cycles:3 or input ('Enter the number
       of Cycles of input signal: ');
                                       //3
44 A=1; // Unit amplitude or input('Enter the amplitude
                                       //5
       of input signal: ');
45 tm=0:1/(fm*fm):k/fm;
46 x4=A*cos(2*%pi*fm*tm);
47 subplot(425),plot2d3(tm,x4),xtitle('Sinusoidal
```

```
Signal', 'n', 'x_4 [n]')
48 //figure(1); plot2d3(tm,x);
49 //title('Graphical Representation of Sinusoidal
      Signal');
50 //xlabel('Time'); ylabel('Amplitude');
51 //xgrid(1)
52
53 //Square wave
54 //clc;clear;
55 t=(0:0.1:4*%pi)';
56 x5=4*%pi*squarewave(t);
57 subplot(426),plot2d3(t,x5),xtitle('Square wave','n',
      'x_5[n]')
58
59
60 //Triangular wave
61 // clear ; clc ;
62 A=5// input('enter the amplitude:');
                                                       //5
63 K= 2// input ('enter number of cycles:');
                                                        //2
64 \times 6 = [0:A \quad A-1:-1:1];
65 x7 = x6;
66 \text{ for } i=1: K-1
67 \quad x7 = [x7 \quad x6];
68 end
69 n7=0:length(x7)-1; // Index of the sequence
70 subplot(427),plot2d3(n7,x7);xtitle('Triangular wave'
      , 'time', 'amplitude');
71
72 / Sawtooth wave
73 // clc; clear;
74 A=5//input('enter the amplitude:');
                                                         //5
75 K=2; //input('enter number of cycles:');
                                                         //2
76 x8 = [0:A];
77 x9 = x8;
78 for i=1:K-1
       x9 = [x9 x8];
79
80 end
81 n9=0:length(x9)-1;
```



Figure 1.1: Representation of discrete time signals

```
82 subplot(428),plot2d3(n9,x9);xtitle('Sawtooth wave','
      time', 'amplitude');
83
  // Complex valued signals
84
85 clc;clear;
86 n = [-10:1:10];
87 a=-0.1+0.3*%i;
88 x=exp(a*n);
89 figure(2);
90 subplot(221), plot2d3(n,real(x)); xtitle('Complex
      valued signal', 'n', 'Real part');
  subplot(223), plot2d3(n,imag(x)); xtitle('Imaginary',
91
      'n');
92 subplot(222), plot2d3(n,abs(x)); xtitle('Magnitude
      part ', 'n ');
93 theta=(180/\%pi)*atan(imag(x), real(x));
94 subplot(224), plot2d3(n,theta); xtitle('Phase part','
     n');
```



Figure 1.2: Representation of discrete time signals

Verification of Sampling Theorem

Scilab code Solution 2.1 To verify Sampling theorem in Time domain

```
1
2 //scilab 5.5.2 , OS: Ubuntu 14.04
3 //Sampling
4 clc;clear;
5 fm=100; //=input('Enter the input signal frequency:')
           //100
     ;
6 k=4;//input('Enter the number of Cycles of input
     signal:'); //2
7 A=1;//input('Enter the amplitude of input signal:');
         //3
8 tm=0:1/(fm*fm):k/fm;
9 x=A*cos(2*%pi*fm*tm);
10 figure(1);
11 subplot(411), plot(tm, x);
12 title('ORIGINAL SIGNAL'); xlabel('Time'); ylabel('
     Amplitude');
13 xgrid(1)
14
15 // Sampling Rate (Nyquist Rate) = 2*fm
```

```
16 fnyq=2*fm;
17
18 // UNDER SAMPLING
19 fs = (3/4) * fnyq;
20 n=0:1/fs:k/fm;
21 xn=A*cos(2*%pi*fm*n);
22 // figure(2);
23 subplot(412),plot2d3('gnn',n,xn);
24 plot(n,xn, 'r');
25 title('Under Sampling');
26 xlabel('Time');
27 ylabel('Amplitude');
28 legend('Sampled Signal', 'Reconstructed Signal');
29 xgrid(1)
30 //NYQUIST SAMPLING
31 fs=fnyq;
32 n=0:1/fs:k/fm;
33 xn=A*cos(2*%pi*fm*n);
34 // figure (3);
35 subplot(413),
36 plot2d3('gnn',n,xn);
37 plot(n,xn,'r');
38 title('Nyquist Sampling');
39 xlabel('Time');
40 ylabel('Amplitude');
41 legend('Sampled Signal', 'Reconstructed Signal');
42 xgrid(1)
43 //OVER SAMPLING
44 fs=fnyq *10;
45 n=0:1/fs:k/fm;
46 xn=A*cos(2*%pi*fm*n);
47 // figure (4);
48 subplot(414)
49 plot2d3('gnn',n,xn);
50 plot(n,xn,'r');
51 title('Over Sampling');
52 xlabel('Time');
53 ylabel('Amplitude');
```



Figure 2.1: To verify Sampling theorem in Time domain

```
54 legend('Sampled Signal', 'Reconstructed Signal');
55 xgrid(1)
56 //Result
57 // Observing plots
```

Impulse response of the LTI system

Scilab code Solution 3.1 To determine the impulse response of a system given a difference equation

```
1 //scilab 5.5.2 , OS: Ubuntu 14.04
2 //To determine the impulse response of a LTI system,
      given the difference equation y[n]=b2 x(n-2)+b1
     x(n-1)+b0x(n) +a(1)y(n-1)
3 clear all;clc;close;
4 b=input('Enter the coefficients of input x[n] = ');//
       [1]
5 a=input ('Enter the coefficients of output y[n]=');
     //[1 -1 0.9]
6 x=[1 zeros(1,9)]; // generate impulse sequence of
     length 10
7 n=0:9;
8 h=filter(b,a,x);
9 figure; plot2d3(n,h),
10 xtitle('Impulse response h[n]', 'Time index n', 'h[n]
      ', '');
11 //Example: y[n]-y[n-1]+0.9y[n-2]=x[n]; a=[1] b=[1 -1]
      0.9]
```



Figure 3.1: To determine the impulse response of a system given a difference equation

12 //n determines the length of the impulse response required 13 //Result:10 samples of h[n]=[1,1,0.1,-0.8,-0.89,-0.17,0.631,0.784, 0.2161,-0.4895]

Frequency response of the LTI system

Scilab code Solution 4.1 To plot the frequency response of a Digital system

```
1 //scilab 5.5.2 , OS: Ubuntu 14.04
2 //To determine the frequency response of a discrete -
     time system from its difference equation
3
4 //Design steps: Given a0 y[n] = -a2 y[n-2] - a1 y[n
     -1 + b0 x [n] + b1 x [n-1] + b2 x [n-2]
  //1. System function H(z) = b0 + b1 - z - 1 + b2
5
                                                     \mathbf{Z}
     -2 / 1 + a1 z -1 + a2 z -2
6 //2. Put z = e (jw) to get the frequency response
7 //Design example: Plot the magnitude and phase
     response of the system represented by
  //6y[n]+5y[n-1]+y[n-2] = 18x[n] + 8x[n-1]
8
9
10
11 clear; clc;
12 close;
13 b=input('Enter the coefficients of x[n]');//[1 -1]]
14 a=input ('Enter the coefficients of y[n]');//[1 -0.5]
```



Figure 4.1: To plot the frequency response of a Digital system

```
15 / b = [18, 8];
16 //a = [6 \ 5 \ 1];
17 m= 0: length(b)-1; p=0:length(a)-1;
18 w=-2*%pi:%pi/100:2*%pi;//Plot over a interval of 4pi
       to observe periodicity
19 num = b * \exp(-\%i * m' * w);
20 den = a * exp(-\%i * p' * w);
21 H= num./den;
22 magH = abs(H); angH= atan(imag(H), real(H));
23 figure;
24 subplot(211), plot(w, magH);
25 xtitle('Magnitude response', 'Frequency in rad', '
      Magnitude');
26 subplot(212),plot(w, angH);
27 xtitle('Phase Response', 'Frequency in rad', 'Phase');
28 //Expected result
29 //H = [5, 3.5802695 - 1.3881467i, 2.6 - i, 2.253303 - 
      0.4785341i, 2.1666667, 2.253303 + 0.4785341i, 2.6 +
      i, 3.5802695 + 1.3881467i, 5]
```

Linear and Circular convolution

Scilab code Solution 5.1 To determine linear convolution

```
1\ //scilab\ 5.5.2 , OS: Ubuntu 14.04
2 // Linear Convolution in time and frequency domain
3
4 clc ;clear all;close ;
5
6 x=[1 2 3 4];//input ('enter the input sequence
      values x(n) = '; // [1 2 3 4]
7 h=[1 -1 0 -1]; //input('enter the impulse sequence
      values h(n) = '); ... / [1 -1 0 -1]
8
9 L1 = length(x);
10 L2 = length(h);
11
12 //Method 1 Using Direct Convolution Sum Formula
13 for i = 1: L1 +L2 -1
14 \quad \operatorname{conv}_{\operatorname{sum}} = 0;
15
   for j = 1: i
16
    if ((( i - j +1) <= L2 ) &( j <= L1 ) )</pre>
    conv_sum = conv_sum + x (j) * h (i - j + 1);
17
18
    end ;
19 y(i) = conv_sum;
```

```
20 \text{ end};
21 end ;
22
23 disp(y,' Convolution Sum using Direct Formula Method
     = ')
24
    //Method 2 Using In built Function
25
26 f = convol(x,h)
27 disp(f, ' Convolution Sum Result using Inbuilt
      Function = ')
28
29 //Method 3 Using frequency Domain multiplication
30 N = L1 + L2 - 1;
                                                      //
      Linear convolution output length
31 x = [x zeros(1, N - L1)];
32 h = [h zeros(1, N - L2)];
33 f1 = fft(x)
34 \ f2 = fft(h)
                                                      //
35 f3 = f1.* f2;
      Multiplication in frequency domain
36 \, \text{f4} = \text{ifft(f3)}
37~\mbox{disp} (f4 , 'Convolution Sum Result DFT and IDFT
      method = ')
38
39 //To plot input, impulse and output signals.
40 subplot (5,1,1) ;plot2d3(x);xtitle('Input signal x '
      , 'n', 'x[n]');
41 subplot(5,1,2) ;plot2d3(h);xtitle('Impulse signal h'
      , 'n', 'h[n]');
42 subplot(5,1,3) ;plot2d3(y);xtitle('Liner Convolution
       using formula', 'n', 'y1[n]');
  subplot(5,1,4) ;plot2d3(f);xtitle('Linear
43
      Convolution using Inbuilt function', 'n', 'y2[n]');
44 subplot(5,1,5) ;plot2d3(f);xtitle('Linear
      Convolution using DFT method', 'n', 'y3[n]');
45
46 // Expected result
                     0. - 6. - 3. - 4.
47 //1. 1.
               1.
```



Figure 5.1: To determine linear convolution

Scilab code Solution 5.2 Circular convolution in time domain and using DFT relations

```
1
2 //scilab 5.5.2 , OS: Ubuntu 14.04
3 // Circular convolution of given discrete sequences
     in time domain (Matrix method)
4 clear;clc;
5 x1=input ('enter the first sequence values x1(n) = ')
        // [1 2 3 4]
6 x2=input('enter the second sequence values x2(n) = '
     ); //[1 -1 0 -1]
7 L1 = length(x1);
                                            //length of
     first sequence
                                            //length of
8 L2 = length(x2);
      second sequence
9
```

```
10 if (L1 >L2)
                                                 //To make
      length of x1 and x2 are Equal
       for i = L2 + 1 : L1
11
12
         x2(i) = 0;
13
       end
14 elseif (L2>L1)
       for i = L1 + 1 : L2
15
16
         x1(i) = 0;
17
       end
18 end
19
20 \text{ N} = \text{length}(x1);
                                                      //x3 =
21 x3 = zeros(1,N);
       Circular convolution result
22 a(1) = x2(1);
23 \text{ for } j = 2: \mathbb{N}
     a(j) = x2(N-j+2);
24
25 \text{ end}
26 for i =1:N
27
     x3(1) = x3(1) + x1(i) * a(i);
28 end
29 X(1,:)=a;
30
31 //Calculation of circular convolution
32 \text{ for } k = 2:N
33
        for j = 2: N
34
           x2(j) = a(j-1);
35
        end
36
           x2(1) = a(N);
           X(k,:) = x2;
37
        for i = 1:N
38
39
             a(i) = x2(i);
             x3(k) = x3(k) + x1(i) * a(i);
40
41
        end
42 end
43 disp(X, 'Circular Convolution Matrix x2[n] = ')
44 disp(x3, 'Circular Convolution Result x3[n] = ')
45 // Expected result
```

46 // Circular Convolution Matrix x2[n] =4748 // 1. - 1. 0. - 1.49 // - 1. 1. - 1.0. $50 \ // 0. - 1. 1. - 1. 51 \ // - 1. 0. - 1. 1.$ 52//Circular Convolution Result x3[n] = 5354// -5. -2. -3. 0.555657 // Circular Convolution in frequency domain (DFT-IDFT method) 58 clear all;clc;close; 59 x1=input ('enter the first sequence values x1(n) =') ; // [1 2 3 4] 60 x2=input('enter the second sequence values x2(n) ='); //[1 -1 0 -1]61 L=input ('enter the length of the sequence values L= '); //4 62//Computing DFT 63//-1 for direct 64 X1 = fft(x1, -1); \mathbf{FFT} 65 X2 = fft(x2, -1);66 disp(X1, 'DFT of x1[n] is X1(k)=') 67 disp(X2, 'DFT of x2[n] is X2(k)=') 68 69 // Multiplication of 2 DFTs 70 X3 = X1.*X2;71 disp(X3, 'DFT of x3[n] is X3(k)=') 72 x3 = (fft(X3,1)) // Circular Convolution Result ,1 for IFFT 73 disp(x3, 'Circular Convolution x3[n] =') 74 //// Expected result 75 //DFT of x1[n] is X1(k) = 10. -2. + 2.i - 2.- 2. - 2. i

76

-1. 1. 3. 1. //DFT of x1[n] is X2(k)= 7778// DFT of x3[n] is X3(k) =-10. - 2. + 2.i796. - 2. - 2.i80 //Circular Convolution x3[n]= -5.-2.81 -3.0. 82////Performing Linear Convolution using Circular 83 Convolution 84 clear; clc; 85 x=input ('enter the input sequence values x(n) ='); // [1 2 3 4] 86 h=input('enter the impulse sequence values h(n) = ') //[1 -1 0 -1]: //Length of input signal 87 N1 = length(x); 88 N2 = length(h); //Length of impulse response 89 // Length of 90 N = N1 + N2 - 1output response 91 disp(N, 'Length of Output Response y(n)') 9293 //Padding zeros to Make Length of 'h' and 'x' equal to length of output response 'y' 9495 h1 = [h, zeros(1, N-N2)];96 x1 = [x, zeros(1, N-N1)];97 98 H = fft(h1, -1);99 X = fft(x1, -1);100 // Multiplication of 2 DFTs 101 Y = X.*H $102 \ y = (fft(Y, 1))$ //Linear Convolution Result 103104 disp(X, 'DFT of i/p X(k) = ') 105 disp(H, 'DFT of impulse sequence H(k) =') 106 disp(Y, 'DFT of Linear Filter o/p Y(k) = ') 107 disp(y, 'Linear Convolution result y[n] = ')

108 109 //Expected output 110 //Length of Output Response y(n)7. 111 112//DFT of i/p X(k) = 10. - 2.0244587 -6.2239817 i , 0.3460107 + 2.4791213 i, 0.1784479 - 2.4219847i, 0.1784479 +2.4219847 i , 0.3460107 - 2.4791213 i, 2.0244587 + 6.2239817 i //DFT of impulse sequence H(k) =113- 1. 1.2774791 + 1.2157152i , , 0.5990311 +0.1930964 i , 2.1234898 + 1.4088117 i, 2.1234898 - 1.4088117 i, 0.5990311 -0.1930964 i , 1.2774791 - 1.2157152 i//DFT of Linear Filter o/p Y(k) = -10. 114 4.9803857 - 10.412171 i, - 0.2714383 +1.5518843 i , 3.7910526 - 4.8916602i3.7910526 + 4.8916602i, -0.2714383 - $1.5518843 \,\mathrm{i}$, $4.9803857 + 10.412171 \,\mathrm{i}$, //Linear Convolution result y[n] = 1. 1151. 1. 0. -6. -3.-4.

Spectral analysis using DFT

Scilab code Solution 6.1 To demonstrate spectral leakage

1 2 //scilab 5.5.2 , OS: Ubuntu 14.04 3 // Spectral Leakage 4 //Check the result for the following cases 5 // case (1): fm=10; fs=125;m=1;m=number of cycles 6 / (case(2)): fm = 10; fs = 125; m = 2;7 // case(3): fm=200; fs=10000;m=2.5; 8 / (case (4)): fm = 75; fs = 250; m = 3;9 10 clc;clear;close; 11 //fm=input('Enter the frequency of the input signal ');//message frequency in Hz 12 //fs=input('Enter the sampling frequency');// sampling frequency in Hz 13 //m=input('Enter the number of cycles of the input signal');// Number of cycles 14 //Case2:No spectral leakage 15 fm=10;fs=125;m=2;//Oversampling and integer number of cycles 16 t=0.0001:1/fs:m/fm; 17 x=3*cos(2*%pi*fm*t); //signal

```
//should be non-
18 N=(m*fs/fm);
      integer to obtain spectral leakage
19 for k=1:N
    X1(k) = 0;
20
    for n=1:length(x)
21
22
     X1(k) = X1(k) + x(n) \cdot \exp((-\%i) \cdot 2 \cdot \%pi \cdot (n-1) \cdot (k-1))
         ./N);
23
    end
24
    end
25 k=0:N-1
                     //frequency axis in Hz
26 f=k*fs/N;
27 figure(1), subplot(221), plot2d3(t,x), xlabel('time'),
      ylabel('x(n)'),title('No leakage: m=2, f=10 and
      Fs=125 Hz'), subplot(223), plot2d3(f, abs(X1)),
      xlabel('freq in Hz'), ylabel('Mag'); //Case 3:
      Spectral leakage
     fm=10;fs=125;m=2.5;//Oversampling and integer
28
        number of cycles
29 t=0.0001:1/fs:m/fm;
30 x=3*cos(2*%pi*fm*t);
                                   //signal
31 N=(m*fs/fm);
                                            //should be non-
      integer to obtain spectral leakage
32 \text{ for } k=1:N
33
    X1(k) = 0;
34
    for n=1:length(x)
35
     X1(k) = X1(k) + x(n) \cdot \exp((-\%i) \cdot 2 \cdot \%pi \cdot (n-1) \cdot (k-1))
         ./N);
36
    end
37
    end
38 k=0:N-1
39 f=k*fs/N;
                     //frequency axis in Hz
40 figure(1), subplot(222), plot2d3(t,x), xlabel('time'),
      ylabel('x(n)'),title('Spectral leakage: m=2.5, f
      =10 and Fs=125 Hz'), subplot(224), plot2d3(f, abs(X1
      )),xlabel('freq in Hz'),ylabel('Mag')
```



Figure 6.1: To demonstrate spectral leakage

Scilab code Solution 6.2 To demonstrate effects of zeropadding and zero insertion on the spectrum

```
13 X_pad= abs(fft(x_pad));
14 figure(1);
15 subplot(221),plot2d3(x),title(' Original sequence'),
      subplot(223),plot2d3 (f,X), title('Spectrum of
      Original sequence');
16 subplot(222), plot2d3(x_pad), title('Zero-padded
      sequence'), subplot(224), plot2d3 (f1, X_pad), title
      ('Spectrum of Zero-padded sequence')
17 //// Effect of inserting zeros in between samples (
      Interpolation)
18 x= input ('enter the input sequence values x(n) = ');
          //[1 \ 2 \ 3 \ 4]
19 k= input ('enter the number of zeros to be inserted=
       '); //2 (Vary and observe effect of zero
      interpolation)
20 x_mod=[];
21 N=length(x);
22 //
23 for i= 1: N
24 x_mod=[x_mod, x(i), zeros(1,k)];
25 end
26 N1=length(x_mod);
27 f = 0: N - 1;
28 f1=0:N1-1;
29 X = abs(fft(x));
30 X_mod= abs(fft(x_mod));
31 figure(2); subplot(221), plot2d3(x), title(' Original
      sequence'), subplot(223), plot2d3 (f,X), title('
      Spectrum of Original sequence');
32 subplot(222), plot2d3(x_mod), title('Zero-interpolated
       sequence'), subplot(224), plot2d3 (f1,X_mod),
     title('Spectrum of Zero-inserted sequence')
```



Figure 6.2: To demonstrate effects of zeropadding and zero insertion on the spectrum



Figure 6.3: To demonstrate effects of zeropadding and zero insertion on the spectrum

FIR filter design

Scilab code Solution 7.1 Design of FIR filter using Windowing method

1 2 //scilab 5.5.2 , OS: Ubuntu 14.04 3 //Design of FIR filters using windowing 4 // Design a digital FIR low pass filter with following specifications. 5 //a) Pass band cut-off frequency :wp= _____radians 6 //b) Pass band ripple : rp=____dB 7 //c) Stop band cut-off frequency :ws= _____radians 8 //d) Stop band attenuation : rs =_____d B 9 //Choose an appropriate window function and determine impulse response and provide a plot of frequency response of the designed filter. 10 11 // Design example: 12 //Design a digital FIR low pass filter with following specifications. 13 //a) Pass band cut-off frequency :0.3 rad 14 //b) Pass band ripple :0.25 dB

```
15 //c) Stop band cut-off frequency :0.45 rad
16 //d) Stop band attenuation
                                              : 50 \text{ dB}
17 clc;
18 clear;
19 close;
20 wp=input('enter the pass band edge in rad');
21 ws=input('enter the stop band edge in rad');
22 rs=input('enter the stop band ripple in dB');
23 freq_points=1024;
24 freq_divs=(freq_points/2)-1;
25 k=4; //Hamming window (decided based on stop band
      attenuation)
26 \text{ trw=ws-wp};
27 N=(k*2*%pi/trw);
28 N=ceil(N);
29 remainder=N-fix(N./2).*2
30 if remainder==0
31
       N = N + 1;
32 end
33
34 \text{ wc=wp};
35 \text{ aph}=(N-1)/2;
36 for n=0:N-1
       if n==aph
37
38
           hdn_minusalph(n+1)=wc/%pi;
39
40
    else
        hdn_minusalph(n+1) = sin(wc.*(n-aph))./(%pi.*(n-
41
           aph));
42
43 \text{ end}
44 end
45 n=0:N-1;
46 wndw=window('hm',N);
47
48 hn=hdn_minusalph.*wndw';
49 figure(1); subplot(311); plot2d3(n,wndw); xlabel('n');
      ylabel('wndw');title('Hamming Window function');
```

```
50 subplot(312); plot2d3(n,hdn_minusalph);xlabel('n');
      ylabel('hdn_minusalph');title('Impulse response
      of IIR filter ');
51 subplot(313); plot2d3(n,hn);xlabel('n');ylabel('hn')
      ;title('Impulse response of FIR filter');
52 / \text{omega} = 0: \% \text{pi} / \text{freg} \cdot \text{divs} : \% \text{pi};
53 h=[hn' zeros(1,freq_points-length(hn))];;//For a
      1024 point DFT
54 H=fft(h);
55 H_mag=20*log10(abs(H));
56 H_ang=atan(imag(H), real(H));
57 H_phase=unwrap(H_ang);
58 w=(0:freq_divs)./(freq_points);
59 w1=w*%pi;
60 figure(2); subplot(211), plot2d(w1, H_mag(1:512));
61 xtitle('Magnitude response', 'w (rad)', 'Magnitude(dB)
      ');
62 subplot(212),plot2d(w1,H_phase(1:512));
63 xtitle('Phase Response', 'w (rad)', 'Phase (rad)');
64
65
66
  //Problems:
67
68
  //1. Design a digital FIR low pass filter with
69
      following specifications.
70 //a) Pass band cut-off frequency
                                           :0.4
                                                   rad
71 //b) Pass band ripple
                                                   :0.25 dB
72 //c) Stop band cut-off frequency
                                                   rad
                                           :0.6
                                                : 44 dB
73 //d) Stop band attenuation
74
75 //2. Design a digital FIR low pass filter with
      following specifications.
76 //a) Pass band cut-off frequency
                                           :0.25
                                                    rad
77 //b) Pass band ripple
                                                   :0.25 dB
78 //c) Stop band cut-off frequency
                                           :0.3
                                                   rad
79 //d) Stop band attenuation
                                                : 50 dB
```



Figure 7.1: Design of FIR filter using Windowing method



Figure 7.2: Design of FIR filter using Windowing method

Design of Hilbert transformer using FIR filter

Scilab code Solution 8.1 Design of a digital Hilbert Transformer using FIR filter

- $1\ //scilab\ 5.5.2$, OS: Ubuntu 14.04
- 2 //Design a differentiator using a Hamming window of length N=21. Plot the time and frequency domain responses.

```
3 //Design a length -25 digital Hilbert transformer using a Hann window.
```

5 //Design of Hilbert transformer

```
6 //The ideal frequency response of a linear phase
Hilbert transformer is given by
```

$$7 //Hd(e jw) = -j e(-j w)$$
, $0 < w < pi$

$$\frac{1}{2} \frac{1}{2} \frac{1}$$

4

10 //The ideal impulse response is given by

```
15
16 // Scilab Program
17 //Inputs: Window length and type of window
18 clc;clear;close;
19
20 N = 41; //input("enter the window length");
                                                      //55
21 freq_points=1024;
22 windowfn =window('hm',N);// Hamming window ()Window
      type can be changed here)
23 m = 0: N-1;
24 \text{ aph} = (N-1)/2;
25 \text{ for } n=0:N-1
26
       if n==aph
27
            hd(n+1) = 0;
28
29
    else
         hd(n+1)=(2/%pi)*((sin((%pi/2)*(n-aph)).^2)./(n-
30
            aph));
31
32 end
33 end
34 n = 0: N - 1;
   hn = hd.*windowfn';
35
36
37
    omega=-%pi:2*%pi/(freq_points-1):%pi;
38
    z = %z;
39
40 den1=real(z^{(N-1)});
41 num=0;
42 \text{ for } n=0:N-1
43
        num = num + (hn(n+1).*z^{(N-n-1)});
44 end
45 num1=real(num);
46 Hz=num1./den1;
47 w = \exp(\% i * \text{omega});
48 rep=freq(Hz("num"),Hz("den"),w);
49 magH=abs(rep);
```

14



Figure 8.1: Design of a digital Hilbert Transformer using FIR filter

```
50 figure; subplot(211), plot2d3(m,hn), xtitle('Impulse
response', 'n''h[n]')
```

```
51 , subplot(212),plot2d(omega,magH);
```

```
52 xtitle('Magnitude response', 'w (rad)', 'Magnitude');
```

```
53 //Expected result
```

```
54 //Magnitude response graph
```

Design of digital differentiator using FIR filter

Scilab code Solution 9.1 Design of Digital Differentiator using a FIR filter

1 2 11//scilab 5.5.2 , OS: Ubuntu 14.04 3 //Design a differentiator using a Hamming window of length N=21. Plot the time and frequency domain response 4 //Inputs: Window length and Type of window 5 //The frequency response of a linear-phase ideal differentiator is given by 6 //Hd(e jw) = j , 0 << -jw, - < < 07 // 8 //The ideal impulse response of a digital differentiator shifted by with linear phase is given by 9 //hd(n) = cos(n) / (n-), n10 // 0, n =11 12 // Scilab Program:

```
13 clc;clear;close;
14 N = 41; // input ("enter the window length"); //55
15 freq_points=1024;
16 windowfn =window('hm',N);//Hamming wuindow (Try with
        different windows)
17 m = 0: N-1;
18 aph = (N-1)/2;
19 for n=0:N-1
20
        if n==aph
            hd(n+1) = 0;
21
22
23
    else
24
         hd(n+1) = cos(%pi*(n-aph))./(n-aph);
25
26 \text{ end}
27 end
28 n=0:N-1;
29
   hn = hd.*windowfn';
30
31 omega=-%pi:2*%pi/(freq_points-1):%pi;
32
33 z = \% z;
34 \text{ den1}=\text{real}(z^{(N-1)});
35 \text{ num}=0;
36 \text{ for } n=0:N-1
37
       num = num + (hn(n+1).*z^{(N-n-1)});
38 end
39 num1=real(num);
40 Hz=num1./den1;
41 w=exp(%i*omega);
42 rep=freq(Hz("num"), Hz("den"), w);
43 magH=abs(rep);
44 figure; subplot(211), plot2d3(m, hn), xtitle('Impulse
      response ', 'n ', 'h[n] '), subplot (212), plot2d (omega,
      magH);
45 xtitle('Magnitude response', 'w (rad)', 'Magnitude');
46 //Expected result
47 // Magnitude response graph
```

```
39
```



Figure 9.1: Design of Digital Differentiator using a FIR filter

Design of IIR filter

Scilab code Solution 10.1 Design of digital Butterworth lowpass filter

 $1\ //scilab\ 5.5.2$, OS: Ubuntu 14.04 2 // Program To Design the Digtial Butterworth IIR Filter 3 //Design a digital IIR low pass filter with following specifications. 4 //a) Pass band cut-off frequency :1000 Hz 5 //b) Pass band ripple :-1 dB 6 //c) Stop band cut-off frequency :3000 Hz 7 //d) Stop band attenuation : -15 dB8 //Sampling frequency: 15000 Hz 9 10 clear all; clc; close; 11 f1=1000; //input('Enter the pass band edge(Hz)='); 12 f2=3000; //input ('Enter the stop band edge(Hz)= '); 13 k1=-1; //input('Enter the pass band attenuation(dB)= '); 14 k2=-15;//input('Enter the stop band attenuation(dB)= 15 fs=10000; //input('Enter the sampling rate(Hz)='); 1617 // Digital filter specifications (rad)

```
18 w1=2*%pi*f1*1/fs;
19 w2=2*%pi*f2*1/fs;
20
21 //Pre warping
22 \text{ ol}=2*fs*tan(w1/2)
23 \text{ o2=2*fs*tan}(w2/2)
24
25 //Design of analog filter
26 n=log10((((10.^(-k1/10))-1)/((10.^(-k2/10))-1))./(2*
      log10(o1/o2));
27 n = round(n);
28 wn= o2./((10.(-k2/10)-1).(1/(2*n)));
29
30 // [h, poles, zeros, gain] = analpf(n, 'butt', [0 0], wn) hb.
      dt = 'c';
  //[fr,hr] = repfreq(hb,fmin,fmax)
31
32
33 h=buttmag(n,wn,1:2*%pi*fs);
34 \text{ mag}=20*\log 10(h)';
35
36
37 //Converting analog to digital filter
38 hz=iir(n, 'lp', 'butt',0.25,[])
39 //g*poly(z, 'z')/poly(p, 'z')
40
41 [hzm,fr]=frmag(hz,256);
42 magz=20*log10(hzm)';
43
44 subplot(2,1,1),plot2d((1:2*%pi*fs)',mag),xtitle('
      Analog IIR filter: lowpass', 'Analog frequency in rads/sec', 'dB',' '); subplot(2,1,2), plot2d(fr,
      magz);xtitle('Digital IIR filter: lowpass 0 < fr</pre>
      < 0.5', 'frequency', 'dB', '');
45
46 //note: Use zoom/axis commands to verify the design.
```



Figure 10.1: Design of digital Butterworth lowpass filter

Scilab code Solution 10.2 Design of Digital Chebyshev lowpass filter

1 //scilab 5.5.2 , OS: Ubuntu 14.04 2 //Program To Design the Digtial Chebyshev IIR Filter 3 ////Design example: 4 //Design a digital IIR low pass filter with following specifications. //a) Pass band cut-off frequency :1000 Hz 5//b) Pass band ripple 6 :-1 dB 7//c) Stop band cut-off frequency :3000 rad 8 //d) Stop band attenuation : -15 dB9 //Sampling frequency: 15000 Hz 10 11 clear all;clc;close; 12 f1=1000; //input ('Enter the pass band edge(Hz)= '); 13 f2=3000; //input ('Enter the stop band edge(Hz)= '); 14 rp=-1;//input('Enter the pass band ripple(dB)= ');

```
15 rs=-15; //input('Enter the stop band attenuation(dB)=
       ');
16 fs=10000; //input('Enter the sampling rate(Hz)=');
17 // Digital filter specifications (rad)
18 w1=2*%pi*f1*1/fs
19 w2=2*%pi*f2*1/fs
20 //Pre warping
21 o1=2*fs*tan(w1/2)
22 \text{ o2=2*fs*tan}(w2/2)
23 or=o2/o1; //Stop-band edge of normalized lowpass
      filter
24 \quad A2 = 10.^{(-rs/10)};
25 A = sqrt(A2);
26 \text{ epsilon2} = (10.^{(-rp/10)-1});
27 epsilon=sqrt(epsilon2)
28 g=((A2-1).^0.5./epsilon)
29
30 \text{ N} = (\operatorname{acosh}(g))/(\operatorname{acosh}(or))
31 N = ceil(N)
32 oc=o1;
33 //[pols,gn] = zpch1(N,epsilon,o1)
34 //Hs = poly(gn, 's', 'coeff ')/real(poly(pols, 's'))
35 h=cheb1mag(N,oc,epsilon,1:2*%pi*fs);
36 mag=20*log10(h)';
37 //plot2d((1:1000)',mag,[2],"011"," ",[ymax,ymin,fmax
      , fmin ])
38 //gain = 20 * \log 10 (abs(h_s)); \% Verify the specification
       [k1,k2] at prewarped frequencies
39 // subplot (211);
40 // plot (omega, gain);
41 //xlabel( frequency in rad/sec);
42 //Converting analog to digital filter
43 fc=w1/(2*%pi);
44 delta1=(1-(1./A2));
45 / / 1 - ripple in passband
46 hz=iir(N, 'lp', 'cheb1', [fc], [delta1 0]);
47 //for cheb1 filters 1-delta(1) < ripple < 1 in passband
48 //g*poly(z, 'z')/poly(p, 'z')
```



Figure 10.2: Design of Digital Chebyshev lowpass filter

Application of IIR filter

Scilab code Solution 11.1 To design a digital IIR Butterworth filter to suppress noise

```
1 //scilab 5.5.2 , OS: Ubuntu 14.04
2 // This program will suppress noise at f=4000 Hz
      using Butterworth prototype
3 // pass band edge=f1=1500Hz
4 //stop band edge=f2=2000 Hz
5 //sampling rate =Fs=10000 Hz = 1/Ts
6 //passband attenuation = -1db
7 //stop attenuation = -3 db
8
9 clear all;clc;close;
10 fl=input ('Enter the pass band edge(Hz) = ');
11 f2=input ('Enter the stop band edge(Hz)=');
12 k1=input('Enter the pass band attenuation(dB)= ');
13 k2=input('Enter the stop band attenuation(dB)= ');
14 fs=input ('Enter the sampling rate (Hz)= ');
15
16 signal_fo=1000;
17 noise_fo=4000;
18
19 // Digital filter specifications (rad)
```

```
20 w1=2*%pi*f1*1/fs;
21 w2=2*%pi*f2*1/fs;
22
23 //Pre warping
24 \text{ ol}=2*fs*tan(w1/2)
25 \text{ o2=2*fs*tan}(w2/2)
26
27 //Design of analog filter
28 n=log10((((10.^(-k1/10))-1)/((10.^(-k2/10))-1))./(2*
      log10(o1/o2));
29 n = round(n);
30 wn= o2./((10.(-k2/10)-1).(1/(2*n)));
31
32 / [h, poles, zeros, gain] = analpf(n, 'butt', [0 0], wn)hb.
      dt = 'c';
33 //[fr,hr] = repfreq(hb,fmin,fmax)
34
35 h=buttmag(n,wn,1:2*%pi*fs);
36 mag=20*log10(h)';
37 // plot 2d ((1:2*\% pi*fs)', mag)
38 //xtitle('Analog IIR filter: lowpass', 'Analog
      frequency in rads/sec', 'dB', '');
39
40 //Converting analog to digital filter
41 hz=iir(n, 'lp', 'butt',0.25,[])
42 //g*poly(z, 'z')/poly(p, 'z')
43
44 [hzm, fr] = frmag(hz, 256);
45 magz=20*log10(hzm)';
46 fr1=fr*fs;
47 // figure; plot2d (fr1 ', magz'); xtitle ('Digital IIR
      filter: lowpass 0 < \text{fr} < 0.5', 'frequency', 'dB', '
       ');
48
49
  /////note: Use zoom/axis commands to verify the
      design.
50 //These coefficients are to be read from variable hz
       (line 41, output of iir function)
```

```
51 num=[0.2928 0.5858 0.2928];
52 den=[1 0 0.1716]; // In negative powers of z
53
54 //Signal generation (sine wave of frequency 1000 Hz)
       of length 1 second
55 t=0:1/fs:10/signal_fo;//10 cycles of input
56 original_signal=sin(2*%pi*signal_fo*t);
57
58 //Noise generation (sine wave of frequency 4000 Hz)
      of length 1 second
59 t=0:1/fs:10/signal_fo;
60 noise=sin(2*%pi*noise_fo*t);
61
62 noisy_signal=original_signal+noise;
63
64 filter_output=filter(num,den,noisy_signal);
65
66 //Plot original, noisy and filtered outputs
67
68 figure;subplot(3,1,1), plot2d(t,original_signal),
     xtitle('Original_signal', 't', 'x(t)'),
69 subplot(3,1,2), plot2d(t,noisy_signal),xtitle('
      Noisy_signal', 't', 'n(t)'),
70 subplot(3,1,3), plot2d(t,filter_output),xtitle('
      Filtered_signal', 't', 'y(t)');
71 l1=length(original_signal);
72 l2=length(noisy_signal);
73 N=512;
74 x=[original_signal zeros(1,N-l1)];//To make it of
      length 512
75 n=[noisy_signal zeros(1,N-l1)];
76 y=[filter_output zeros(1,N-l1)];
77 X = fft(x);
78 N=fft(n);
79 Y = fft(y);
80 f = (0:511) * fs;
81 figure;
82 subplot(3,1,1), plot2d(f,abs(X)),xtitle('
```



Figure 11.1: To design a digital IIR Butterworth filter to suppress noise

```
Original_signal', 'F', 'X(f)'),
83 subplot(3,1,2), plot2d(f,abs(N)),xtitle('
            Noisy_signal', 'F', 'N(f)'),
84 subplot(3,1,3), plot2d(f,abs(Y)),xtitle('
            Filtered_signal', 'F', 'Y(f)');
```



Figure 11.2: To design a digital IIR Butterworth filter to suppress noise

Design of Notch filter

Scilab code Solution 12.1 Suppression of noise at a given frequency using Notch filter

1

```
2 //scilab 5.5.2 , OS: Ubuntu 14.04
3 //Program To Design a simple notch filter and verify
4 // Design a simple notch filter to stop a
      disturbance with frequency F_0=3.5 kHz and a
      sampling frequency F_s=8 \text{ kHz}.
5 //Also, verify the notch filter operation by adding
     a sinewave of F<sub>0</sub> Hz to a speech signal, filter
     and verify.
6
7 //Scilab Program:
8 clc;clear;close;
9 f=3500; //input("Enter the frequency in Hz");
                  //3500
10 fs=8000; //input("Enter the sampling rate");
                    //8000
11 r=0.98; //input ("Enter the radius of the pole in the
     z-plane"); //0.98
12 w=2*%pi*f/fs;
13 z1 = exp(\%i * w);
```

```
14 z2 = exp(-\%i*w);
15 p1=r*exp(\%i*w);
16 p2=r*exp(-\%i*w);
17 z = \% z;
18 num1 = (real((z-z1)*(z-z2)))
19 den1=(real(((z-p1)*(z-p2))))
20 Hz=num1./den1
21 // figure (1); plzr (Hz); zgrid ()
22 [h1 fr]=frmag(Hz,512)
23 figure(1); plot2d(fr*fs,h1); xtitle('Magnitude
      response', 'frequency in Hz', 'Mag');
24
25 //Noise generation
26
27 original_signal=wavread('home/hyrkswamy/kswamy/
      Coursework/SAP/wav/mask.wav');
28 t=0:1/fs:(length(original_signal)-1)/fs;
29 noise=sin(2*%pi*f*t);
30 noisy_signal=original_signal+noise;
31
32 filter_output=filter(num1,den1,noisy_signal);
33
34 //Play back the original, noisy and filtered outputs
35 playsnd(original_signal,fs);
36 pause;
37 playsnd(noisy_signal,fs);
38 pause;
39 playsnd(filter_output,fs);
```



Figure 12.1: Suppression of noise at a given frequency using Notch filter

Design of Resonator

Scilab code Solution 13.1 Design of a Notch filter to filter noise at a given frequency

```
1
2 //scilab 5.5.2 , OS: Ubuntu 14.04
3 //Design a digital resonator that resonates at 1000
     Hz. Assume Fs = 8000 Hz.
4 // Calculate the pole location
5 / w = 2 * pi * f / fs;
6 //Complex conjugate pair of poles at w=pi/4 and -pi
      /4
7 //Assume radius=0.98 (near to unit circle but inside
       the unit circle)
8
9 //Scilab Program:
10 clc;
11 clear;
12 close;
13 f=1000; //input("Enter the frequency in Hz");
      //1000
14 fs=8000;//input("Enter the sampling rate");
      //8000
15 r=0.98;//input("Enter the radius of the pole in the
```



Figure 13.1: Design of a Notch filter to filter noise at a given frequency

```
z-plane");
                    //0.98
16 w=2*%pi*f/fs;
17 pole1=r*exp(\%i*w);
18 pole2=r*exp(-%i*w);
19
20 \ z = \% z;
21
22 num1=real(z^{(2)});
23 den1=real(z^{(2)} - 1.3859293*z+0.9604);
24 Hz=num1./den1;
25 // figure;
26 //plzr(Hz);
27 [h1 fr]=frmag(Hz,1024);
28 figure;
29 plot2d(fr*fs,h1);
30 xtitle('Magnitude response', 'frequency in Hz', 'Mag')
      ;
```