

Scilab Textbook Companion for  
Control Systems  
by A Nagoor Kani<sup>1</sup>

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# **Book Description**

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Scilab numbering policy used in this document and the relation to the above book.

**Exa** Example (Solved example)

**Eqn** Equation (Particular equation of the above book)

**AP** Appendix to Example(Scilab Code that is an Appednix to a particular Example of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means a scilab code whose theory is explained in Section 2.3 of the book.

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# Chapter 2

## COMPONENTS OF CONTROL SYSTEM

### Scilab code Exa 2.1 POTENTIOMETER

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 2.1
7 clc;
8 clear;
9 n=300; // number of turns
10 li=0.01//linearity =1%
11 v=30//voltage=30V
12 kp=v/n
13 disp(kp,'Potentiometer constant in (volts/turn)')
14 nmid=n/2
15 vmid=kp*nmid
16 disp(vmid,'Voltage at mid point is;')
17 disp('Range of voltage at mid point with 1%
linearity is 14.7 volts to 15.3 volts')//vmid(+-)
0.3
```

```

18 // assuming potentiometer is perfectly linear so the
    resistance at midpoint setting from reference is
    50 kiloohm
19 // load resistance of 500Kiloohm is connected in
    parallel with potentiometer
20 req=(500*50)/(500+50)
21 v0=(v*req)/(50+req) //using voltage divison rule
22 disp(v0, 'Voltage at midpoint with load resistance
    500 Kiloohm (in volts)')

```

---

### Scilab code Exa 2.2 GEAR TRAIN

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 2.2
7 clc;
8 clear;
9 n1=20 //no of teeth in first gear
10 n2=10 //no of teeth in second gear
11 diratio=n1/n2
12 disp(diratio, 'the ratio of diameters is ')
13 theta1=40 //gear1 is rotated by an angle of 40 degree
14 theta2=(n1/n2)*theta1
15 disp(theta2, 'displacement of gear2 in (degrees)')
16 as1=30 //angular speed of gear1 is 30 rad/sec
17 as2=(n1/n2)*as1
18 disp(as2, 'angular speed of gear2 in (rad/sec)')
19 aa2=4 //angular acceleration of gear 2 is 4 rad/sec^2
20 aa1=(n2/n1)*aa2
21 disp(aa1, 'angular acceleration of gear 1 in (rad/sec
    ^2)')
22 t1=5 //torque on gear1 5N-m

```

```
23 t2=(n2/n1)*t1
24 disp(t2, 'torque on gear2 in (N-m)')
```

---

### Scilab code Exa 2.3 GEAR TRAIN

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 2.3
7 clc;
8 clear;
9 n1=200//no of teeth in gear1
10 n2=50//no of teeth in gear2
11 n3=100//no of teeth in gear3
12 n4=50//no of teeth in gear4
13 n5=40//no of teeth in gear5
14 n6=20//no of teeth in gear6
15 n7=150//no of teeth in gear7
16 //if gear 1 rotates in clockwise then all odd no
     gears rotate in clockwisw and even no gear rotate
     in anticlockwise
17 ad1=2//angular displacement in gear 1 is 2rad
18 ad4=(n1/n4)*ad1
19 disp(ad4, 'angular displacement in gear 4 in rad (
     anticlockwise)')
20 ad7=(n1/n7)*ad1
21 disp(ad7, 'angular displacement in gear 7 in rad (
     clockwise)')
22 av6=20//angular velocity of gear 6 is 20 rad/sec
23 av1=(n6/n1)*av6
24 disp(av1, 'angular velocity of gear 1 in rad/sec; (
     clockwise)')
25 av3=(n6/n3)*av6
```

```
26 disp(av3,'angular velocity of gear 3 in rad/sec; ('  
    clockwise)')  
27 t1=10//torque on gear 1 is 10 N-m  
28 t3=(n3/n1)*t1  
29 disp(t3,'torque in gear 3 in N-m')  
30 t7=(n7/n1)*t1  
31 disp(t7,'torque in gear 7 in N-m')
```

---

# Chapter 3

## TIME RESPONSE ANALYSIS

### Scilab code Exa 3.1 RESPONSE OF THE SYSTEM

```
1 // control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 3.1
7
8 clc;
9 clear;
10 s=%s
11 p=poly([4], 's', 'coeff')
12 q=poly([0 5 1], 's', 'coeff')
13 g=p./q
14 disp(g, 'The given transfer function is')
15 c=g/(1+g)
16 disp(c, 'The closed loop transfer function is')
17 u=c/s
18 disp(u, 'The input is unit step signal')
```

---

This code can be downloaded from the website [www.scilab.in](http://www.scilab.in)

### Scilab code Exa 3.2 RESPONSE OF THE SYSTEM

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 3.2
7
8 clc;
9 clear;
10 s=%s
11 p=poly([100], 's', 'coeff')
12 q=poly([0 2 1], 's', 'coeff')
13 h=poly([1 0.1 0 ], 's', 'coeff')
14 g=p./q
15 disp(g, 'the given transfer function is ')
16 c=g/(1+(g*h))
17 disp(c, 'the closed loop transfer function is ')
18 u=c/s
19 disp(u, 'the input is unit step signal')
```

---

This code can be downloaded from the website [www.scilab.in](http://www.scilab.in)

### Scilab code Exa 3.3 RESPONSE OF THE SYSTEM

```
1 //control systems by Nagoor Kani A
2 //Edition 3
```

```

3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 3.3
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 // the input is unit step signal
12 h=syslin('c', 600/(s^2+70*s+600))//the closed loop
    transfer function
13 disp(h,'the closed loop transfer function')
14 //standard form od second order system is w^2/s^2+2*
    zeta*w*s+w^2
15 //compaing h with the standard form
16 w=sqrt(600)//natural frequency of oscillation
17 disp(w,'natural frequency of oscillation in rad/sec')
18 zeta=70/(2*w)//damping ratio
19 disp(zeta,'damping ratio')

```

---

#### Scilab code Exa 3.4 RESPONSE OF THE SYSTEM

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 3.4
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 // the input is unit step signal
12 h=syslin('c',100/(s^2+10*s+100))//the value of k is

```

```

    100
13 k=100
14 zeta=0.5 // given damping ratio
15 disp(k,'the value of k is ')
16 disp(h,'the closed loop transfer function')
17 // standard form od second order system is w^2/s^2+2*
   zeta*w*s+w^2
18 // compaing h with the standard form
19 w=sqrt(k) // natural frequency of oscillation
20 disp(w,'natural frequency of oscillation in rad/sec '
      )
21 mp=exp((-zeta*pi)/sqrt(1-(zeta)^2))*100 // percentage
      peak overshoot
22 disp(mp,'percentage peak overshoot in percentage')
23 tp=%pi/(w*sqrt(1-(zeta)^2))
24 disp(tp,'peak time in seconds')

```

---

### Scilab code Exa 3.6 RESPONSE OF THE SYSTEM

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 3.6
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 // the input is unit step signal
12 h=syslin('c',16/(s^2+4*s+16)) //the value of k is 0.2
13 zeta=0.5 // given damping ratio
14 disp(h,'the closed loop transfer function')
15 // standard form od second order system is w^2/s^2+2*
   zeta*w*s+w^2

```

```

16 //compaing h with the standard form
17 w=4//natural frequency of oscillation
18 disp(w,'natural frequency of oscillation in rad/sec')
19 k=(2*zeta*w-(0.8))/16
20 disp(k,'the value of k is')
21 mp=exp((-zeta*pi)/sqrt(1-(zeta)^2))*100//percentage
   peak overshoot
22 disp(mp,'percentage peak overshoot in percentage')
23 tp=%pi/(w*sqrt(1-(zeta)^2))
24 disp(tp,'peak time in seconds')
25 //constructing a right angle triangle with zeta and
   sqrt(1-zeta^2)
26 theta=atan(0.866/0.5)/(1-zeta^2)/zeta
27 disp(theta,'the value of theta is')
28 tr=(%pi-theta)/(w*sqrt(1-(zeta)^2))
29 disp(tr,'the rise time in seconds')
30 t=1/(zeta*w)//time constant
31 ts1=3*t//settling time for 5% error
32 disp(ts1,'settling time for 5% error in seconds')
33 ts2=4*t//settling time for 2% error
34 disp(ts2,'settling time for 2% error in seconds')

```

---

This code can be downloaded from the website [www.scilab.in](http://www.scilab.in)

### Scilab code Exa 3.7 RESPONSE OF THE SYSTEM

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 3.7
7

```

```

8 clc;
9 clear;
10 s=%s
11 p=poly([1 0.4 0 ],'s','coeff')
12 q=poly([0 0.6 1],'s','coeff')
13 g=p./q
14 disp(g,'the given transfer function is')
15 c=g/(1+g)
16 disp(c,'the closed loop transfer function is')
17 u=c/s
18 disp(u,'the input is unit step signal')
19 //standard form of second order system is w^2/s^2+2*
    zeta*w*s+w^2
20 //comparing h with the standard form
21 w=1//natural frequency of oscillation
22 disp(w,'natural frequency of oscillation in rad/sec',
    )
23 zeta=1/(2*w)
24 disp(zeta,'the damping ratio is')
25 mp=exp((-zeta*pi)/sqrt(1-(zeta)^2))*100 //percentage
    peak overshoot
26 disp(mp,'percentage peak overshoot in percentage')
27 tp=%pi/(w*sqrt(1-(zeta)^2))
28 disp(tp,'peak time in seconds')

```

---

This code can be downloaded from the website [www.scilab.in](http://www.scilab.in)

### Scilab code Exa 3.9 RESPONSE OF THE SYSTEM

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10

```

```

6 // Example 3.9
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 // the input is 12 unit step signal
12 h=syslin('c',10/(s^2+2*s+10))
13 disp(h,'the closed loop transfer function')
14 //standard form od second order system is w^2/s^2+2*
    zeta*w*s+w^2
15 //compaing h with the standard form
16 w=3.162//natural frequency of oscillation
17 disp(w,'natural frequency of oscillation in rad/sec',
      )
18 zeta=2/(2*w)
19 disp(zeta,' damping ratio is ')
20 mp=exp((-zeta*pi)/sqrt(1-(zeta)^2))*100 //percentage
      peak overshoot
21 disp(mp,'percentage peak overshoot in percentage')
22 po=(mp/100)*12//peak over shoot for 12 units
23 disp(po,'peak over shoot for 12 units')
24 tp=%pi/(w*sqrt(1-(zeta)^2))
25 disp(tp,'peak time in seconds')
26 //constructing a right angle triangle with zeta and
    sqrt(1-zeta^2)
27 theta=atan(0.866/0.5)/(1-zeta^2)/zeta
28 disp(theta,'the value of theta is')
29 tr=(%pi- theta)/(w*sqrt(1-(zeta)^2))
30 disp(tr,'the rise time in seconds')
31 t=1/(zeta*w)//time constant
32 ts1=3*t//settling time for 5% error
33 disp(ts1,'settling time for 5% error in seconds')
34 ts2=4*t//settling time for 2% error
35 disp(ts2,'settling time for 2% error in seconds')

```

---

# Chapter 4

## FREQUENCY RESPONSE ANALYSIS

### Scilab code Exa 4.1 BODE PLOT

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 4.1
7 clc;
8 clear;
9 s=poly(0,'s')//defines s as polynomial variable
10 h=syslin('c',(s^2)/((1+0.2*s)*(1+0.02*s)))//the
    given transfer function assigned to variable h .
    Assume the value of K as 1
11 scf(1)
12 bode(h,0.1,100)//frequency range
13 show_margins(h)
14 //calculation of system gain K
15 K=10^(-28/20)//value of K is calculated by equating
    20logK to -28db
16 disp(K,'the value of gain')
```

---

### Scilab code Exa 4.2 BODE PLOT

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 4.2
7 clc;
8 clear;
9 s=poly(0,'s') // defines s as poly nomial variable
10 h=syslin('c',(75*(1+0.2*s))/(s*(s^2+16*s+100))) //the
    given transfer function assigned to variable h
11 scf(1)
12 bode(h,0.1,100) //frequency range
13 show_margins(h)
14 a=g_margin(h)
15 b=p_margin(h)
16 disp(a,b,'the gain margin and phase margin are')
```

---

### Scilab code Exa 4.3 BODE PLOT

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 4.3
7 clc;
8 clear;
9 s=poly(0,'s') // defines s as poly nomial variable
```

```

10 h=syslin('c',(%e*(0.2*s)/(s*(s+2)*(s+8))))//the
    given transfer function assiganned to variable h
    assume K=1
11 scf(1)
12 bode(h,0.1,100)//frequency range
13 show_margins(h)
14 //calculation of K
15 K1=10^(30/20)
16 disp(K1,'when gain margin =2db ')
17 K2=10^(24/20)
18 disp(K2,'the value of K when phase margin is 45')

```

---

#### Scilab code Exa 4.4 BODE PLOT

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 4.4
7 clc;
8 clear;
9 s=poly(0,'s')//defines s as poly nomial variable
10 h=syslin('c',(10)/(s*(1+0.4*s)*(1+0.1*s)))//the
    given transfer function assigned to variable h
11 scf(1)
12 bode(h,0.1,100)//frequency range
13 show_margins(h)

```

---

#### Scilab code Exa 4.5 BODE PLOT

```

1 //control systems by Nagoor Kani A
2 //Edition 3

```

```

3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 4.5
7 clc;
8 clear;
9 s=poly(0,'s') //defines s as polynomial variable
10 h=syslin('c',(20)/(s*(1+3*s)*(1+4*s))) //the given
    transfer function assigned to variable h
11 scf()
12 bode(h,0.1,100)
13 show_margins(h)
14 //calculation of gain cross over frequency
15 disp('from the plot the value of gain cross over
frequency is :1.1 rad/sec')

```

---

### Scilab code Exa 4.6 BODE PLOT

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 4.6
7 clc;
8 clear;
9 s=poly(0,'s') //defines s as polynomial variable
10 h=syslin('c',(5*(1+2*s))/(1+4*s)*(4+0.25*s)) //the
    given transfer function assigned to variable h
11 scf(1)
12 bode(h,0.1,100) //frequency range
13 show_margins(h)

```

---

# Chapter 5

## CONCEPTS OF STABILITY AND ROOTLOCUS

Scilab code Exa 5.1 ROUTH CRITERION

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.1
7
8 clc;
9 clear;
10 s=poly(0, 's')
11 a=(s^4)+(8*s^3)+(18*s^2)+(16*s)+5
12 b=coeff(a)
13 n=length(b)
14 R=routh_t(a)
15 disp(R, 'the routh array is ; ')
16 disp('since there is no sign change the system is
stable')
17 disp('all the four roots lie left half of the s
plane')
```

---

### Scilab code Exa 5.2 ROUTH CRITERION

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.2
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 a=(s^6)+(2*s^5)+(8*s^4)+(12*s^3)+(20*s^2)+(16*s)+16
12 b=coeff(a)
13 n=length(b)
14 R=routh_t(a)
15 disp(R,'the routh array is ;')
16 ap=s^4+6*s^2+8
17 r=roots(ap)
18 disp(r,'the roots of auxilary polynomial ;')
19 disp('the system is marginally stable ;')
20 disp('four roots lying in imaginary axis ;')
```

---

### Scilab code Exa 5.3 ROUTH CRITERION

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.3
```

```
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 a=(s^5)+(s^4)+(2*s^3)+(2*s^2)+(3*s)+5
12 b=coeff(a)
13 n=length(b)
14 R=routh_t(a)
15 disp(R,'the routh array is;')
16 disp('the system is unstable')
```

---

### Scilab code Exa 5.4 ROUTH CRITERION

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.4
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 a=(9*s^5)-(20*s^4)+(10*s^3)-(s^2)-(9*s)-10
12 b=coeff(a)
13 n=length(b)
14 R=routh_t(a)
15 disp(R,'the routh array is;')
16 disp('there are 3 sign changes in first column of
routh array ')
17 disp('three roots lie on right side of s plane so
the system is unstable')
```

---

### Scilab code Exa 5.5 ROUTH CRITERION

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.5
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 a=(s^7)+(9*s^6)+(24*s^5)+(24*s^4)+(24*s^3)+(24*s^2)
     +(23*s)+15
12 b=coeff(a)
13 n=length(b)
14 R=routh_t(a)
15 disp(R,'the routh array is ;')
16 disp('there is sign change in first column of routh
array so ths system is unstable ;')
17 ae=s^4+s^2+1
18 r=roots(ae)
19 disp(r,'the roots of auxilary equation are ')
20 disp('two roots lie on right half of splane five
roots lie on left half of s plane')
```

---

### Scilab code Exa 5.6 ROUTH CRITERION

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.6
7
```

```

8 clc;
9 clear;
10 s=poly(0, 's')
11 a=(s^7)+(5*s^6)+(9*s^5)+(9*s^4)+(4*s^3)+(20*s^2)
    +(36*s)+36
12 b=coeff(a)
13 n=length(b)
14 R=routh_t(a)
15 disp(R, 'the routh array is ;')
16 //divide characterstic equation by auxilary
    polynomial to get quotient polynomial
17 //routh table for quotient poly nomial
18 a1=(s^3)+(5*s^2)+(9*s)+9 //quotient poly nomial
19 b1=coeff(a1)
20 n1=length(b1)
21 R1=routh_t(a1)
22 disp(R1, 'the routh array for quotient poly nomial is
    ;')
23 ap=s^4+4 //auxillary polynomial
24 r=roots(ap)
25 disp(r, 'the roots are ')
26 disp('the system is unstable')
27 disp('two roots on right half of s plane and five
    roots lie in left half of s plane')

```

---

### Scilab code Exa 5.7 ROUTH CRITERION

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.7
7
8 clc;

```

```

9 clear;
10 s=poly(0, 's')
11 a=(s^5)+(4*s^4)+(8*s^3)+(8*s^2)+(7*s)+4
12 b=coeff(a)
13 n=length(b)
14 R=routh_t(a)
15 disp(R, 'the routh array is ; ')
16 ap=s^2+1
17 r=roots(ap)
18 disp(r, 'the roots are ')
19 disp ('the roots of auxillary equation are in
        imagianry axis so the system is marginally stable
        ')
20 disp('three roots lie in left half of s plane')

```

---

### Scilab code Exa 5.8 ROUTH CRITERION

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.8
7
8 clc;
9 clear;
10 s=poly(0, 's')
11 a=(s^6)+(s^5)+(3*s^4)+(3*s^3)+(3*s^2)+(2*s)+1
12 b=coeff(a)
13 n=length(b)
14 R=routh_t(a)
15 disp(R, 'the routh array is ; ')
16 //characterstic polynomial can be expressed as
        product of auxillary polynomial and quotient
        polynomial

```

```

17 // divide characterstic equation by auxilary
    polynomial to get quotient polynomial
18 //routh table for quotient poly nomial
19 a1=(s^4)+(s^3)+(2*s^2)+(2*s)+1 //quotient poly
    nomial
20 b1=coeff(a1)
21 n1=length(b1)
22 R1=routh_t(a1)
23 disp(R1,'the routh array for quotient poly nomial is
    ;')
24 ap=s^2+1
25 r=roots(ap)
26 disp(r,'the roots are')
27 disp('the system is unstable')
28 disp('two roota on imaginary axis ,two roots on
    right half of s plane and two roots lie in left
    half of s plane')

```

---

### Scilab code Exa 5.9 ROUTH CRITERION

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.9
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 //the close loop tranfer function is K/s*(s+1)*(s+2)
    +K
12 a=(s^3)+(3*s^2)+(2*s)+1//the characterstic equation
    assuming K=1
13 b=coeff(a)

```

```
14 n=length(b)
15 R=routh_t(a)
16 disp(R,'the routh array is ;')
17 disp('the value of K lies between 0 to6 for the
      system to be stable')
```

---

### Scilab code Exa 5.12 ROUTH CRITERION

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.12
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 //the close loop tranfer function is K(1-s)/s*(s^2+5
    s+9)+K(1-s)
12 a=(s^3)+(5*s^2)+(8*s)+1 //the charater stic equation
    is assuming K=1
13 b=coeff(a)
14 n=length(b)
15 R=routh_t(a)
16 disp(R,'the routh array is ;')
17 disp('the value of K lies between 0 to7.5 for the
      system to be stable')
```

---

### Scilab code Exa 5.13 NYQUIST PLOT

```
1 //control systems by Nagoor Kani A
2 //Edition 3
```

```

3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.13
7
8 clc;
9 clear;
10 s=poly(0,'s')//defines s as poly nomial variable
11 h=syslin('c',(230/(s*(s+2)*(s+10))))//the value of K
    lies between 0 to 240 .the given transfer
    function assigned to variable h
12 nyquist(h)
13 show_margins(h,'nyquist')
14 //calculation of K
15 //when -0.00417K=-1the contour passes through -1+j0
    and the corospondig value of K is the limiting
    value of k for stablty
16 K=1/0.00417
17 disp(K,'the value of K is')

```

---

### Scilab code Exa 5.14 NYQUIST PLOT

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.14
7
8 clc;
9 clear;
10 s=poly(0,'s')//defines s as poly nomial variable
11 h=syslin('c',(0.6*(1+s)^2/(s^3)))//the system is
    stable for K vlaue greater than 0.5. the given
    transfer function assigned to variable h

```

```

12 scf()
13 nyquist(h)
14 show_margins(h, 'nyquist')
15 //when K>0.5 -1+j0 is encircled in both clockwise
    and anticlockwise direction one time. so the
    system is stable
16 disp('the system is stable for K value greater than
    0.5.')

```

---

### Scilab code Exa 5.15 NYQUIST PLOT

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.15
7
8 clc;
9 clear;
10 s=poly(0,'s')//defines s as polynomial variable
11 h=syslin('c',(1+4*s)/(s*(1+s)*(1+2*s)))//the given
    transfer function assigned to variable h
12 scf()
13 nyquist(h)
14 show_margins(h, 'nyquist')
15 disp('the closed loop system is unstable ')
16 disp('two poles of closed loop system are lying on
    right half of s plane')

```

---

### Scilab code Exa 5.16 NYQUIST PLOT

```

1 // control systems by Nagoor Kani A

```

```

2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.16
7
8 clc;
9 clear;
10 s=poly(0,'s') //defines s as polynomial variable
11 h=syslin('c',(7*(1+0.5*s)*(1+s)/(1+10*s)*(s-1)))//  

    system is stable for K>6.....the given transfer  

    function assigned to variable h
12 scf()
13 nyquist(h)
14 show_margins(h,'nyquist')
15 //calculation of K
16 //when -0.01667K=-1 the contour passes through -1=   

    j0 and the corresponding value of K is the limiting  

    value of k for stability
17 K=1/0.1667
18 disp(K,'the value of K is ')
19 disp('the open loop system is unstable')
20 disp('for stability of closed loop system K>6')

```

---

### Scilab code Exa 5.17 NYQUIST PLOT

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.17
7
8 clc;
9 clear;

```

```
10 s=poly(0,'s')//defines s as polynomial variable
11 h=syslin('c',(5/(s*(1-s))))//the given transfer
   function assigned to variable h
12 scf()
13 nyquist(h)
14 disp('Both open loop and closed loop functions are
unstable')
```

---

### Scilab code Exa 5.18 NYQUIST PLOT

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.28
7
8 clc;
9 clear;
10 s=poly(0,'s')//defines s as poly nomial variable
11 h=syslin('c',(s+2)/(s+1)*(s-1))//the given transfer
   function assigned to variable h
12 scf()
13 nyquist(h)
14 show_margins(h,'nyquist')
15 disp('open loop system is unstable')
16 disp('closed loop system is stable;')
```

---

### Scilab code Exa 5.22 ROOT LOCUS

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
```

```

4 // Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.22
7
8 clc;
9 clear;
10 s=poly(0,'s')//defines s as poly nomial variable
11 G=syslin('c',(1/(s*(s^2+4*s+13))))//the given
    transfer function assigned to variable G assume K
    =1
12 scf()
13 evans(G)
14 //calculation of K
15 disp('the characterstic equation is given by : s
    ^2+4*s^2+13*s+K')
16 //put s=jw and equate real and imaginary parts
17 //K=4*w^2
18 K=4*13
19 disp(K,'the value of K is ')

```

---

### Scilab code Exa 5.23 ROOT LOCUS

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.23
7
8 clc;
9 clear;
10 s=poly(0,'s')//defines s as poly nomial variable
11 h=syslin('c',(48/(s*(s+2)*(s+4))))//the given
    transfer function assigned to variable h assume K
    =1

```

```

12 scf()
13 evans(h)
14 //calculation of K
15 disp('the characteristic equation is given by : s
      ^3+6*s^2+8*s+K')
16 //put s=jw and equate real and imaginary parts
17 //K=4*w^2
18 K=6*8
19 disp(K, 'the value of K is ')

```

---

### Scilab code Exa 5.24 ROOT LOCUS

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.24
7
8 clc;
9 clear;
10 s=poly(0,'s')//defines s as poly nomial variable
11 h=syslin('c',(s+9)/(s*(s^2+4*s+11)))//the given
     transfer function assigned to variable h assume K
     =1
12 scf()
13 evans(h)
14 //the characteristic equation is (s^3+4s^2+11s)+Ks+9K
15 //put s=jw and equating real and imaginary parts to
     calculate K
16 K=(4*(4.4)^2)/9//the value of w is 4.4
17 disp(K, 'the value of K is ;')

```

---

### Scilab code Exa 5.25 ROOT LOCUS

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.25
7
8 clc;
9 clear;
10 s=poly(0,'s') //defines s as polynomial variable
11 h=syslin('c',(1/(s*(s+4)*(s^2+4*s+20)))) // the given
    transfer function assigned to variable h assume
    K=1
12 scf()
13 evans(h)
14 //the characteristic equation is (s^4+8s^3+36s^2+80s)
    +K
15 //put s=jw and equating real and imaginary parts to
    calculate K
16 K=-(3.2)^4+36*(3.2)^2 //the value of w is 3.2
17 disp(K, 'the value of K is ;')
```

---

### Scilab code Exa 5.26 ROOT LOCUS

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.26
7
8 clc;
9 clear;
```

```

10 s=poly(0,'s')// defines s as polynomial variable
11 h=syslin('c',(s+15)/(s*(s+1)*(s+5)))//the given
    transfer function assigned to variable h assume K
    =1
12 scf()
13 evans(h)
14 //the characteristic equation is (s^3+6s^2+5s)+Ks+15K
15 //put s=jw and equating real and imaginary parts to
    calculate K
16 K=30/(-4.5)
17 disp(K,'the value of K is;')

```

---

### Scilab code Exa 5.27 ROOT LOCUS

```

1 // control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.27
7
8 clc;
9 clear;
10 s=poly(0,'s')// defines s as polynomial variable
11 K=poly(0,'K')
12 h=syslin('c',(s^2+6*s+25)/(s*(s+1)*(s+2)))//the
    given transfer function assigned to variable h
    assume K=1
13 scf()
14 evans(h)
15 //the characteristic equation is (s^3+(3+K)s^2+(2+6K)
    s)25K
16 //put s=jw and equating real and imaginary parts to
    calculate K
17 a=roots((-6*K^2)+5*K-6)

```

```
18 disp(a,'the value of K is')
```

---

### Scilab code Exa 5.28 ROOT LOCUS

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 5.28
7
8 clc;
9 clear;
10 s=poly(0,'s')//defines s as polynomial variable
11 h=syslin('c',(1/(s*(s^2+6*s+10))))//the given
    transfer function assigned to variable h assume K
    =1
12 scf()
13 evans(h)
14 //the characteristic equation is (s^3+6s^2+10s)+K
15 //put s=jw and equating real and imaginary parts to
    calculate K
16 K=6*(3.2)^2//the value of w is 3.2
17 disp(K,'the value of K is ')
```

---

# Chapter 6

## LINEAR SYSTEM DESIGN

### Scilab code Exa 6.1 LAG COMPENSATOR

```
1 // control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 6.1
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 //calculation of gain K
12 //for ramp input ess(steady state error ) is 0.2
13 ess=0.2
14 kv=1/ess
15 // open loop transfer function G(s)=K/s*(1+2*s)
16 //by definition of velocity error constant applying
    limit s=0 in G(s)
17 disp('the value of K is 5; ')
18 h=syslin('c',5/(s*(1+2*s)))
19 bode(h)
20 show_margins(h)
```

```

21 xtitle("uncompensated system")
22 //from the plot the phase margin of uncompensated
   system is 18
23 //but the system requires phase margin of 40 so lag
   compensation required
24 pm=45//choose PM of compensated system is 45 degree
25 phigcn=45-180// phase of G(s) at new gain cross over
   frequency
26 wgcn=0.5//the frequency corresponding to phase of
   -135 is 0.5 rad/sec
27 agcn=20//db magnitude at wgcn
28 //20log betaa=20
29 betaa=10^(agcn/20)
30 disp(betaa,'the value for betaa is ')
31 zc=wgcn/10//zero of lag compensator
32 t=10/wgcn
33 disp(t,'the value for t is ')
34 pc=1/(betaa*t)
35 disp(pc,'pole of lag compensator is ')
36 //transfer function of lag compensation is (s+1/t)/(
   s+1/betaa*t))
37 hc=syslin('c', (10*(1+20*s))/(1+200*s))
38 disp(hc,'the transfer function of lag compensator is
   ;')
39 //open loop transfer function of compensated system
   is h*hc
40 hcmp=syslin('c',h*hc)
41 disp(hcmp,'open loop transfer function of
   compensated system is ')
42 figure()
43 bode(hcmp)
44 show_margins(hcmp)
45 xtitle("compensated system")

```

---

### Scilab code Exa 6.2 LAG COMPENSATOR

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 6.2
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 //calculation of gain K
12 kv=30//velocity error constant is 30sec^-1
13 // open loop transfer function G(s)=K/s*(s+4)*(s+80)
14 //by definition of velocity error constant applying
    limit s=0 in G(s)
15 disp('the value of K is 9600; ')
16 h=syslin('c',9600/(s*(s+4)*(s+80)))
17 bode(h)
18 show_margins(h)
19 xtitle("uncompensated system")
20 //from the plot the phase margin of uncompensated
    system is 12
21 //but the system requires phase margin of 33 so lag
    compensation required
22 pm=38//choose PM of compensated system is 38 degree
23 phigcn=38-180// phase of G(s) at new gain cross over
    frequency
24 wgcn=4.7//the frequency corresponding to phase of
    -142 is 4.7 rad/sec
25 agcn=16//db magnitude at wgcn
26 //20log betaa=16
27 betaa=10^(agcn/20)
28 disp(betaa,'the value for betaa is ')
29 zc=wgcn/10//zero of lag compensator
30 t=10/wgcn
31 disp(t,'the value for t is ')
32 pc=1/(betaa*t)
33 disp(pc,'pole of lag compensator is ')

```

```

34 // transfer function of lag compensation is (s+1/t)/(
35   s+1/betaa*t))
36 hc=syslin('c', (6.3*(1+2.13*s))/(1+13.419*s))
37 disp(hc,'the transfer function of lag compensator is
38   ;')
39 //open loop transfer function of compensated system
40   is h*hc
41 hcmp=syslin('c',h*hc)
42 disp(hcmp,'open loop transfer function of
43   compensated system is ')
44 figure()
45 bode(hcmp)
46 show_margins(hcmp)
47 xtitle("compensated system")

```

---

### Scilab code Exa 6.3 LAG COMPENSATOR

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 6.3
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 K=20//the value of K
12 h=syslin('c',20/(s*(s+2)*(s+8)))
13 evans(h)
14 xtitle("uncompensated system")
15 //given ramp input ess(steady state error ) is0.125
16 ess=0.125
17 kvd=1/ess//desired velocity error constant
18 // transfer function of un compensated system G(s)

```

```

=20/s*(s+2)*(s+8)
19 //by definition of velocity error constant applying
    limit s=0 in G(s)
20 kvu=1.25
21 disp(kvu,'The velocity error constant of un
    compensated system is')
22 disp(kvd,'desired velocity error constant')
23 A=kvd/kvu//A is the factor by which velocity error
    constant increases
24 betaa=A*1.2
25 disp(betaa,'the value of betaa is')
26 zc=0.1*(-2)//zero of lag compensator=0.1* second
    pole
27 t=(-1/zc)
28 disp(t,'the value for t is')
29 pc=(-1)/(betaa*t)//pole of lag compensator
30 //transfer function of lag compensation is (s+1/t)/(
    s+1/betaa*t))
31 hc=syslin('c',(s+0.2*s)/(s+0.026*s))
32 disp(hc,'transfer function of lag compensation is')
33 //open loop transfer function of compensated system
    is h*hc
34 hcmp=syslin('c', h*hc)
35 disp(hcmp,'open loop transfer function of
    compensated system is')
36 figure()
37 evans(hcmp)
38 xtitle("compensated system")
39 //by definition of velocity error constant applying
    limit s=0 in hcmp
40 kvc=9.165//velocity error constant of compensated
    system
41 essc=1/kvc//steady state error for compensated
    system
42 disp(essc,'steady state error for compensated system
    ')
43 disp('since the steady state error of compensated
    system is less than 0.125 the design is')

```

acceptable ')

---

### Scilab code Exa 6.4 LAG COMPENSATOR

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 6.4
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 K=240//the value of K
12 h=syslin('c',240/(s*(s+10)^2))
13 evans(h)
14 xtitle("uncompensated system")
15 kvd=20//given desired velocity error constant
16 // transfer function of un compensated system G(s)
17 // =20/s*(s+2)*(s+8)
18 //by definition of velocity error constant applying
19 // limit s=0 in G(s)
20 kvu=2.4
21 disp(kvu,'The velocity error constant of un
22 compensated system is')
23 disp(kvd,'desired velocity error constant')
24 A=kvd/kvu//A is the factor by which velocity error
25 constant increases
26 betaa=A*1.2
27 disp(betaa,'the value of betaa is')
28 zc=0.1*(-10)//zero of lag compensator=0.1* second
29 pole
30 t=(-1/zc)
31 disp(t,'the value for t is')
```

```

27 pc=(-1)/(betaa*t)//pole of lag compensator
28 //transfer function of lag compensation is (s+1/t)/(
29 s+1/betaa*t))
30 hc=syslin('c',(s+1)/(s+0.1))
31 disp(hc,'transfer function of lag compensation is ')
32 //open loop transfer function of compensated system
33 is h*hc
34 hcmp=syslin('c', h*hc)
35 disp(hcmp,'open loop transfer function of
36 compensated system is ')
37 figure()
38 evans(hcmp)
39 xtitle("compensated system")
40 //by definition of velocity error constant applying
41 limit s=0 in hcmp
42 kvc=24//velocity error constant of compensated
43 system
44 disp('since the velocity error constant of
45 compensated system is greater than specified
46 value the design is acceptable')

```

---

### Scilab code Exa 6.5 LEAD COMPENSATOR

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 6.5
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 //calculation of gain K
12 //given for ramp input ess(steady state error) is

```

```

1/15
13 ess=1/15
14 kv=1/ess
15 // open loop transfer function G(s)=K/s*(s+1)
16 //by definition of velocity error constant applying
    limit s=0 in G(s)
17 disp('the value of K is 15; ')
18 h=syslin('c',15/(s*(s+1)))
19 bode(h)
20 show_margins(h)
21 xtitle("uncompensated system")
22 //from the plot the phase margin of uncompensated
    system is 13
23 //but the system requires phase margin of 45 so lead
    compensation required
24 pm=45//choose PM of compensated system is 45 degree
25 phim=37//maximum lead angle
26 alpha=(1-(sind(phim)))/(1+(sind(phim)))
27 disp(alpha,'the vale of alpha is ')
28 wmdb=-20*log(1/sqrt(alpha))///db magnitude
29 wm=5.6//from the bode plot of uncompensated system
    the frequency wm corosponding to db gain of -6db
    is 5.6 rad/sec
30 t=1/(wm*sqrt(alpha))
31 disp(t,'the value of t is ')
32 //transfer function of lead compensator is (s+1/t)/(
    s+1/alpha*t)
33 hc=syslin('c',(0.25*(1+0.36*s))/(1+0.09*s))
34 disp(hc,' transfer function of lead compensator is ')
35 //open loop transfer function of compensated system
    is h*hc
36 hcmp=syslin('c',h*hc)
37 disp(hcmp,'open loop transfer function of
    compensated system is ')
38 figure()
39 bode(hcmp)
40 show_margins(hcmp)
41 xtitle("compensated system")

```

---

### Scilab code Exa 6.6 LEAD COMPENSATOR

```
1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 6.6
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 //calculation of gain K
12 kv=50//given velocity error constant
13 // open loop transfer function G(s)=K/s*(s+1)(s+5)
14 //by definition of velocity error constant applying
    limit s=0 in G(s)
15 disp('the value of K is 250; ')
16 h=syslin('c',250/(s*(s+1)*(s+5)))
17 bode(h)
18 show_margins(h)
19 xtitle(" uncompensated system")
20 //from the plot the phase margin of uncompensated
    system is -44
21 //but the system requires phase margin of 20 so lead
    compensation required
22 pm=20//choose PM of compensated system is 20 degree
23 //since the lead angle required is greater than 60
    we have to realise lead compensator as cascade of
    two compensators with each compensator providing
    half of required phase
24 phim=69/2//maximum lead angle
25 alpha=(1-sind(phim))/(1+sind(phim))
26 disp(alpha,'the vale of alpha is ')
```

```

27 wmdb=-20*log(1/sqrt(alpha))///db magnitude
28 wm=7.8//from the bode plot of uncompensated system
    the frequency wm corresponding to db gain of -6db
    is 5.6 rad/sec
29 t=1/(wm*sqrt(alpha))
30 disp(t,'the value of t is')
31 //transfer function of lead compensator is (s+1/t)/(
    s+1/alpha*t)
32 hc=syslin('c',(0.0784*(1+0.024*s)^2)/(1+0.067*s)^2)
33 disp(hc,' transfer function of lead compensator is')
34 //open loop transfer function of compensated system
    is h*hc
35 hcmp=syslin('c',h*hc)
36 disp(hcmp,'open loop transfer function of
    compensated system is ')
37 figure()
38 bode(hcmp)
39 show_margins(hcmp)
40 xtitle("compensated system")

```

---

### Scilab code Exa 6.9 LAG LEAD COMPENSATOR

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 6.9
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 //calculation of gain K
12 kv=80//given velocity error constant
13 // open loop transfer function G(s)=K/s*(s+3)(s+6)

```

```

14 //by definition of velocity error constant applying
    limit s=0 in G(s)
15 disp('the value of K is 1440; ')
16 h=syslin('c',1440/(s*(s+3)*(s+6)))
17 bode(h)
18 show_margins(h)
19 xtitle("uncompensated system")
20 //from the plot the phase margin of uncompensated
    system is -46
21 pm=40//choose PM of compensated system is 40 degree
22 phigcn=40-180// phase of G(s) at new gain cross over
    frequency
23 wgcn=1.8//the frequency corresponding to phase of
    -140 is 1.8 rad/sec
24 wgcl=4//choose gain cross over frequency of lag
    compensator as 4rad/sec
25 agcl=23//db magnitude at egcl is 23db
26 //agcl=20log*betaa
27 betaaa=10^(agcl/20)
28 disp(betaaa,'the value of betaaa is ')
29 zc1=wgcl/10//zero of lag compensator
30 t1=10/wgcl
31 disp(t1,'the value of t1 is ')
32 pc1=1/(betaaa*t1)
33 disp(pc1,'pole of lag compensator is ')
34 //transfer function of lag section is (betaaa*1+st1)
    /(1+s*betaaa*t1)
35 hc1=syslin('c',(14*(1+2.5*s))/(1+35*s))
36 disp(hc1,'transfer function of lag section ')
37 alpha=1/betaaa
38 disp(alpha,'the value of alpha is ')
39 wmdb=-20*log(1/sqrt(alpha))///db magnitude
40 wm=17//from the bode plot of uncompensated system
    the frequency wm corresponding to db gain of -12
    db is 17rad/sec
41 t2=1/(wm*sqrt(alpha))
42 //transfer function of lead section is (alpha*1+st2)
    /(1+s*alpha*t2)

```

```

43 hc2=syslin('c',(0.07*(1+0.22*s))/(1+0.0154*s))
44 disp(hc2,'transfer function of lead section')
45 hc3=syslin('c',hc1*hc2)
46 disp(hc3,'the transfer function of lag lead
compensation system is')
47 //open loop transfer function of compensated system
is h*hc3
48 hcmp=syslin('c',h*hc3)
49 disp(hcmp,'the overall transfer function of
compensated system')
50 figure()
51 bode(hcmp)
52 show_margins(hcmp)
53 xtitle("compensated system")

```

---

### Scilab code Exa 6.11 PD CONTROLLER

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 6.11
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 //given tranfer function g(s)=10/(s*(1+2*s)*(1+s))
12 h=syslin('c',10/(s*(1+2*s)*(1+s)))
13 pm=30//given phase margin
14 w=6.2//given gain cross over frequency in rad/sec
15 //put s=jw in G(s) magnitude of G(jw) gives A1 and
angle of G(jw) gives phi1 at w
16 A1=2.052
17 phi=-207.5//in degrees

```

```

18 theta=30-(-27.5) // desired pm -pm of uncompensated
    system
19 kd=sind(theta)/w*A1//derivative constant
20 kp=cosd(theta)/A1//proportional constant
21 disp(kd,kp,'the values of derivative constant and
    proportional constant are')
22 //transfer function of PD controller is (kp+kd*s)
23 hc=syslin('c', s*((0.343/s)+0.262))
24 disp(hc,'the transfer function of PD controller is')
25 hcmp=syslin('c', h*hc)
26 disp(hcmp,'the transfer function of compensated
    system is')

```

---

### Scilab code Exa 6.12 PI CONTROLLER

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 6.12
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 //given tranfer function g(s)=100/(s+1)*(s+2)*(s+5)
12 h=syslin('c',100/(s+1)*(s+2)*(s+5))
13 pm=60//given phase margin
14 w=0.5//given gain cross over frequency in rad/sec
15 //put s=jw in G(s) magnitude of G(jw) gives A1 and
    angle of G(jw) gives phi1 at w
16 A1=8.63
17 phi=-46//in degrees
18 theta=pm-134//desired pm -pm of uncompensated system
19 ki=(-w)*sind(theta)/A1//integral constant

```

```

20 kp=cosd(theta)/A1//proportional constant
21 disp(ki,kp,'the values of integral constant and
   proportional constant are')
22 //transfer function of PI controller is (kp+ki/s)
23 hc=syslin('c', 0.056*(1+0.57*s)/s)
24 disp(hc,'the transfer function of PD controller is')
25 hcmp=syslin('c', h*hc)
26 disp(hcmp,'the transfer function of compensated
   system is')

```

---

### Scilab code Exa 6.13 PID CONTROLLER

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 6.13
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 //given tranfer function g(s)=100/(s+1)*(s+2)*(s+10)
12 h=syslin('c',100/(s+1)*(s+2)*(s+10))
13 pm=45//given phase margin
14 w=4//given gain cross over frequency in rad/sec
15 //put s=jw in G(s) magnitude of G(jw) gives A1 and
   angle of G(jw) gives phi1 at w
16 A1=0.5
17 phi=-161//in degrees
18 theta=pm-19//desired pm -pm of uncompensated system
19 ess=0.1//steady state error for ramp input
20 kv=1/ess//velocity errpr constant
21 //the transfer function of PID controller is Gc(s)=
   kp+kd*s+ki/s

```

```

22 //by definition of velocity error constant applying
    s=0 in S*Gc(s)*G(s)
23 ki=2//integeral constant
24 disp(ki,'the value of integral constant')
25 kd=((sind(theta)/(w*A1))+(ki/w^2))//derivative
    constant
26 kp=cosd(theta)/A1//proportional constant
27 disp(kd,kp,'the values of proportional constant
    and derivative constant are')
28 hc=syslin('c',0.344*(s^2+5.23*s+5.81)/s)
29 disp(hc,'the transfer function of PID controller is',
    )
30 hcmp=syslin('c',h*hc)
31 disp(hcmp,'the transfer function of compensated
    system is')

```

---

### Scilab code Exa 6.14 PD CONTROLLER

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 6.14
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 //dominent pole sd=-zeta*w=%i*w*sqrt(1-zeta^2)
12 zeta=0.8//damping ratio
13 w=2//natural frequency of osciilation in rad/sec
14 sd=(-zeta*w)+(%i*w)*sqrt(1-zeta^2))
15 disp(sd,'the dominennt pole is')
16 d=abs(sd)
17 disp(d,'the value of d is ')

```

```

18 betaa=phasemag(sd)
19 disp(betaa,'the value of betaa is ;')
20 h=syslin('c',20/s*(s+2)*(s+4))//given tranfer
   function G(s)
21 //find magnitude and phase of G(s) at s=sd
22 a=20/(sd*(2+sd)*(4+sd))
23 ad=abs(a)
24 disp(ad,'the value of ad is ')
25 phid=phasemag(a)
26 disp(phid,'the value of phid is ')
27 kd=sind(phid)/(d*ad*sind(betaa))//derivative
   constant
28 disp(kd,'the derivative constant is ')
29 kp=(-sind(betaa+phid))/(ad*sind(betaa))//
   proportional constant
30 disp(kp,'the integral constant is ')
31 hc=syslin('c', s*((0.243/s)+0.557))//transfer
   function of PD controller is kpo +kd*s
32 disp(hc,'transfer function of PD controller is ')
33 hcmp=syslin('c',h*hc)//transfer function
   compensated system
34 disp(hcmp,'transfer function compensated system ')

```

---

### Scilab code Exa 6.15 PI CONTROLLER

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 6.15
7
8 clc;
9 clear;
10 s=poly(0,'s')

```

```

11 //dominent pole sd=zeta*w=%i*w*sqrt(1-zeta^2)
12 zeta=0.9//damping ratio
13 w=2.5//natural frequency of osciilation in rad/sec
14 sd=(-zeta*w)+(%i*w)*sqrt(1-zeta^2))
15 disp(sd,'the dominennt pole is ')
16 d=abs(sd)
17 disp(d,'the value of d is ')
18 betaa=phasemag(sd)
19 disp(betaa,'the value of betaa is ;')
20 h=syslin('c',4/(s+1)*(s+5))//given tranfer function
   G(s)
21 //find magnitude and phase of G(s) at s=sd
22 a=4/((1+sd)*(5+sd))
23 ad=abs(a)
24 disp(ad,'the value of ad is ')
25 phid=phasemag(a)
26 disp(phid,'the value of phid is ')
27 ki=-(d*sind(phid))/(ad*sind(betaa))//integral
   constant
28 disp(ki,'the integral constant is ')
29 kp=(-sind(betaa+phid))/(ad*sind(betaa))-(2*ki*cosd(
   betaaa))/d //proportional constant
30 disp(kp,'the proportional constant is ')
31 hc=syslin('c', 2.02*(s+1.19)/s)//transfer function
   of PD controller is kpo +kd*s
32 disp(hc,'transfer function of PI controller is ')
33 hcmp=syslin('c',h*hc)//transfer function
   compensated system
34 disp(hcmp,'transfer function compensated system ')

```

---

### Scilab code Exa 6.16 PID CONTROLLER

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015

```

```

4 // Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 6.15
7
8 clc;
9 clear;
10 s=poly(0,'s')
11 //dominent pole sd=-zeta*w=%i*w*sqrt(1-zeta^2)
12 zeta=0.8//damping ratio
13 w=2.5//natural frequency of osciilation in rad/sec
14 sd=(-zeta*w)+(%i*w)*sqrt(1-zeta^2))
15 disp(sd,'the dominennt pole is ')
16 d=abs(sd)
17 disp(d,'the value of d is ')
18 betaa=phasemag(sd)
19 disp(betaa,'the value of betaa is ;')
20 h=syslin('c',75/(s+1)*(s+3)*(s+8))//given tranfer
    function G(s)
21 //find magnitude and phase of G(s) at s=sd
22 a=75/((1+sd)*(3+sd)*(8+sd))
23 ad=abs(a)
24 disp(ad,'the value of ad is ')
25 phid=phasemag(a)
26 disp(phid,'the value of phid is ')
27 ess=0.08//steady state error
28 kv=1/ess//velocity error constant
29 //the transfer function of PID controller is Gc(s)=
    kp+kd*s+ki/s
30 //by definition of velocity error constant applying
    s=0 in S*Gc(s)*G(s)
31 ki=12.5/3.125//integeral constant
32 kd=sind(phid)/(d*ad*sind(betaa))+(ki/(d^2)) //
    derivative constant
33 disp(kd,'the derivative constant is ')
34 kp=(-sind(betaa+phid))/(ad*sind(betaa))-(2*ki*cosd(
    betaaa))/d //proportional constant
35 disp(kp,'the proportional constant is ')
36 hc=syslin('c', 0.68*(s^2+4.26*s+5.88)/s)//transfer

```

```
    function of PID controller is kpo*f +kd*s
37 disp(hc,'transfer function of PI controller is ')
38 hcmp=syslin('c',h*hc)//transfer function
    compensated system
39 disp(hcmp,'transfer function compensated system ')
```

---

# Chapter 7

## STATE SPACE ANALYSIS

### Scilab code Exa 7.10 STATE MODEL

```
1 // control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 7.10
7
8 clc;
9 clear;
10 s=%s
11 p=poly([10], 's', 'coeff')
12 q=poly([1 2 4 1], 's', 'coeff')
13 sm=cont_frm(p,q)
14 disp(sm, 'the state model in matrix form is')
```

---

This code can be downloaded from the website [www.scilab.in](http://www.scilab.in)

### Scilab code Exa 7.11 STATE MODEL

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 7.11
7
8 clc;
9 clear;
10 s=%s
11 p=poly([40 10], 's', 'coeff')
12 q=poly([0 3 4 1], 's', 'coeff')
13 sm=cont_frm(p,q)
14 disp(sm, 'the state model in matrix form is ')

```

---

This code can be downloaded from the website [www.scilab.in](http://www.scilab.in)

### Scilab code Exa 7.12 STATE MODEL

```

1 //control systems by Nagoor Kani A
2 //Edition 3
3 //Year of publication 2015
4 //Scilab version 6.0.0
5 //operating systems windows 10
6 // Example 7.12
7
8 clc;
9 clear;
10 s=%s
11 h=syslin('c',(2*(s+5))/((s+2)*(s+3)*(s+4)))
12 disp(h, 'thr transfer function is ')
13 ss=tf2ss(h)
14 disp(ss, 'the state space model is ')
15 [Ac,Bc,U,ind]=canon(ss(2),ss(3))

```

16 **disp**(Ac ,Bc ,U ,ind)

---

This code can be downloaded from the website [www.scilab.in](http://www.scilab.in)