

# Optimization in Scilab

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# Outline

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- 2 Optimization
- 3 Other Optimization Tools in Scilab
- 4 "Optim" in Scilab

# Today's focus

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- Optimization in Scilab

# Optimization

- Minimize/maximize some (more than one) objective function by varying decision variable
- Subject to constraints on functions of decision variables
- All engineering domains, economics
- Vast area in itself

# Single Objective Optimization Problems

$$\min_x f(x) \quad (1)$$

where  $x$  is  $n$  dimensional,  $f(x)$  is a scalar, with/without

- Bound constraints:  $x_L \leq x \leq x_U$
- Linear/Nonlinear equality constraints:  $g(x) = b$
- Linear/Nonlinear inequality constraints:  $g(x) \leq b$

Components of  $x$  can be real, integer or binary.

Find '**Decision Variables**':  $x$  which minimize '**Obj**':  $f$



# Linear optimization with Linear constraints

- Scilab function: **karmarkar**

## Calling Sequence

**x1=karmarkar(a,b,c,lb)**

- a:matrix (n,p)
  - b:n-vector
  - c:p-vector
  - lb:lower bound
- Also be solved in scilab using linpro function
  - linpro is in Quapro toolbox under Optimization in ATOMS,
  - It can installed by command atomsInstall('Quapro')

# Linear optimization with Linear constraints

Example:-

Maximize

$$3x_1 + x_2 + 3x_3$$

for

$$2x_1 + x_2 + x_3 \leq 2$$

$$x_1 + 2x_2 + 3x_3 \leq 5$$

$$2x_1 + 2x_2 + x_3 \leq 6$$

$$x_1, x_2, x_3 \geq 0$$

# Quadratic with linear constraints

- Scilab function: **qp\_solve**

Calling Sequence

$x1=[x \text{ ,} iact \text{ ,} iter \text{ ,} f]]]=qp\_solve(Q,p1,C1,b,me)$

- Q: real positive definite symmetric matrix (dimension  $n \times n$ ). p- real (column) vector (dimension  $n$ )
- c:p - vector
- lb: lower bound
- me: number of equality constraints
- It can also be solved in scilab using quapro function.
- quapro is in Quapro toolbox under Optimization in ATOMS
- It can be installed by command `atomsInstall(quapro)`

# Quadratic with linear constraints

Example Minimize

$$f(x) = \frac{1}{2}x^T \begin{bmatrix} 2 & 0 \\ 0 & 2 \end{bmatrix} x + \begin{bmatrix} -2 \\ -2 \end{bmatrix}^T x$$

for

$$x_1 + x_2 \geq 2 + \sqrt{2}$$

$$-x_1 + x_2 \geq -2$$

# Other Optimization Tools in Scilab: I

Native (built-in) functions in Scilab:

- **fminsearch**: Computes unconstrained minimum of a given function using the Nelder-Mead algorithm (simplex region search).
  - Native (built-in function) to Scilab:
  - Derivative free, relies on search
  - Basic usage: `[xopt,fopt]=fminsearch(costf,x0)`; `costf` should take `x` as input and return `f` as output
  - Try minimizing  $f(x) = x^2 + 5$  using `fminsearch`
- **neldermead**: Computes minimum of a nonlinear function subject to bounds and nonlinear constraints
  - Option for several types of search algorithms

# Unconstrained Non-linear

- Scilab function: **fminsearch**

Calling Sequence

```
x = fminsearch ( costf , x0 )
```

- `costf`:The cost function. `x0`:The initial guess.
- computes the unconstrained minimum of given function with the Nelder-Mead algorithm.

# Unconstrained Non-linear

Example:  $f(x) = x_1^2 + x_2^2 + x_1x_2$

# Optim command in Scilab

Simplified Call:

$[f_{opt}, x_{opt}] = \text{optim}(\text{costf}, x_0)$

where

- $x_0$ : initial guess where minimum of  $f$  occurs,
- $f_{opt}$ : the optimum (minimum) value,
- $x_{opt}$ : where the optimum occurs,
- $\text{costf}$ : user specified (scilab) function to compute objective function ( $f$ ) and/or its gradient ( $g$ ) depending on the input integer flag "ind" as:  
 $[f, g, \text{ind}] = \text{costf}(x, \text{ind})$



# Simple example

$$f(x) = x^2 + 10$$

$$g(x) = 2x$$

- Minimize  $f(x)$  starting from  $x_0 = 10$ .
- Write a function (example "myfunction1.sci") which takes  $x, ind$  as input and returns  $f, g, ind$  as output.
- Use "optim" function to minimize.
- Answer:  $f_{opt} = 10, x_{opt} = 0$ .

## Another example (Campbell et al., 2010)

$$f(x_1, x_2, x_3) = (x_1 - x_3)^2 + 3(x_1 + x_2 + x_3 - 1)^2 + (x_1 - x_3 + 1)^2$$

with gradient

$$\begin{aligned} g &= \left[ \frac{\partial f}{\partial x_1}, \frac{\partial f}{\partial x_2}, \frac{\partial f}{\partial x_3} \right] \\ &= [2(x_1 - x_3) + 6(x_1 + x_2 + x_3 - 1) + 2(x_1 - x_3 + 1), \\ &\quad 6(x_1 + x_2 + x_3 - 1), -2(x_1 - x_3) - 2(x_1 - x_3 + 1) + 6(x_1 + x_2 + x_3 - 1)] \end{aligned}$$

# Exercise plan

- Minimize the function starting with guess values  $x_0 = [1, 1, 1]$ .
- Write a function (example "myfunction2.sci") which takes  $x, ind$  as input and returns  $f, g, ind$  as output.
- Use "optim" function to minimize.
- Answer:  $x_{opt} = [0.14, 0.27, 0.64], f_{opt} = 0.51$ .

# Other options with optim

Several other options/features with optim

- Several optimization algorithms: quasi-newton, conjugate gradient, etc.
- Gradient computation using finite differences: "NDcost" used with optim.
- Various stopping/diagnostic criteria: Maximum number of iterations, calls to costf, thresholds, etc.
- Use of ind to compute gradient only when required (save computational effort).
- help optim: to know more

# Other Optimization Tools in Scilab: II

Native (built-in) functions in Scilab:

AI based algorithms

- Genetic algorithms: single objective optimization, multiobjective optimization, various implementations
- Simulated annealing

# Optimization Toolboxes in Scilab

Can be installed easily (atoms or otherwise) or interfaces to them

- quapro: linear, quadratic programming ( $Q$  not necessarily positive definite)
- IPOpt, fsqp, lp\_solve, etc.

Check "<http://atoms.scilab.org/categories/optimization>"

# Optimization Features available in Scilab

- Nonlinear optimization with the **optim** function
- Quadratic optimization with the **qpsolve** function
- Nonlinear least-square optimization with the **lsqrsolve** function
- Semidefinite programming with the **semidef** function
- Genetic algorithms with the **optim\_ga** function
- Simulated annealing with the **optim\_sa** function
- Linear matrix inequalities with the **lmisolver** function

# Missing optimization features in Scilab

A list of features which are not available in Scilab, but are available in toolboxes.

- Integer parameter with linear objective solver and sparse matrices : currently available in **LPSOLVE** toolbox, based on the simplex method,
- Linear objective with sparse matrices : currently available in **LIPSOL**, based on interior points method,
- Nonlinear objective and non linear constraints : currently available in interface to **IPOPT** toolbox, based on interior point methods,
- Nonlinear objective and non linear constraints : currently available in interface to **CONMIN** toolbox, based on method of feasible directions,



## References

- S. L. Campbell, J.P. Chancelier and R. Nikoukhah, "Modeling and Simulation in Scilab/Scicos", Springer, 2006.

**Thank You**