

Scilab Manual for
Digital Signal Processing
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Experiment: 1

Waveform generation using discrete time signals

Scilab code Solution 1.1 Waveform generation using DT signals

```
1 // Expt 1. Waveform generation using discrete time
  signals using Scilab
2 // O.S. Windows 10
3 ////Scilab 6.0.0
4 //Generation of unit step Discrete signal
5 clear;
6 clc;
7 t=0:4;
8 y=ones(1,5);
9 subplot(3,2,1);
10 plot2d3 (t,y);
11 xlabel('n');
12 ylabel('u(n)');
13 title('Unit Step Discrete Signal');
14
15 //Generation of Unit Ramp Discrete signal
16 n1=0:8;
```

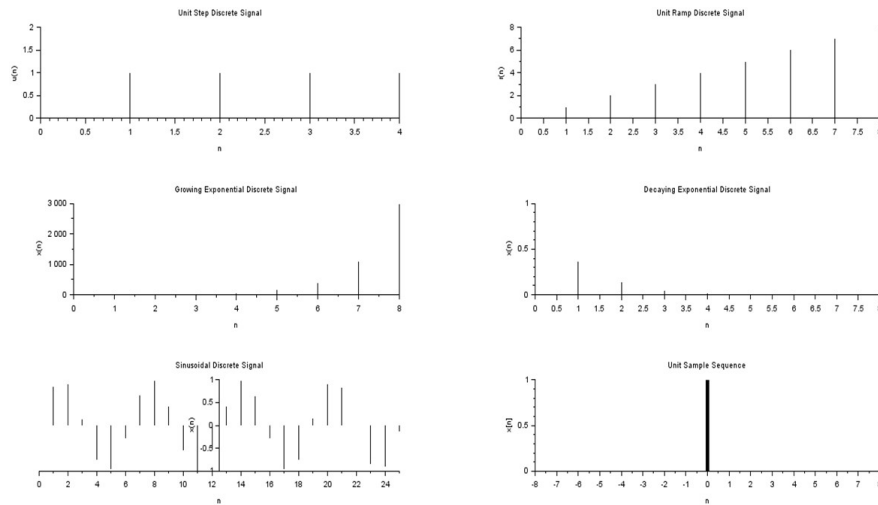


Figure 1.1: Waveform generation using DT signals

```

17 y1=n1;
18 subplot(3,2,2);
19 plot2d3 (n1,y1);
20 xlabel('n');
21 ylabel('r(n)');
22 title('Unit Ramp Discrete Signal');
23
24 //Generation of Growing Exponential Discrete signal
25 n1=0:8;
26 y1=n1;
27 y2=exp(n1);
28 subplot(3,2,3);
29 plot2d3 (n1,y2);
30 xlabel('n');
31 ylabel('x(n)');
32 title('Growing Exponential Discrete Signal');
33
34 //Generation of Decaying Exponential Discrete signal
35 n1=0:8;
36 y1=n1;

```

```

37 y2=exp(-n1);
38 subplot(3,2,4);
39 plot2d3 (n1,y2);
40 xlabel('n');
41 ylabel('x(n)');
42 title('Decaying Exponential Discrete Signal');
43
44 //Generation of sinusoidal discrete signal
45 n1=0:25;
46 y1=n1;
47 y2=sin(n1);
48 subplot(3,2,5);
49 plot2d3 (n1,y2);
50 xlabel('n');
51 ylabel('x(n)');
52 title('Sinusoidal Discrete Signal');
53
54 //Generation of unit impulse sequence
55 l=7;
56 n=-1:l;
57 x=[zeros(1,l),1,zeros(1,l)];
58 b=gca();
59 b.y_location="middle";
60 subplot(3,2,6);
61 plot2d3('gnn',n,x);
62 a= gce ();
63 a. children (1) . thickness =5;
64 xtitle ('Unit Sample Sequence','n','x[n]');

```

Experiment: 2

Z-transform and pole zero plot of a system

Scilab code Solution 2.1 Z transform of DT sequence

```
1 //Expt2: To draw the pole-zero plot
2 //O.S: Windows 10;
3 //Scilab: 6.0.0
4 clear;
5 clc ;
6 //Z- transform of [1 0 3 -1 2]
7 clear;
8 clc ;
9 close ;
10 function [za]=ztransfer(sequence,n)
11 z=poly(0,'z','r')
12 za=sequence*(1/z)^n'
13 endfunction
14 x1=[1 0 3 -1 2];
15 n=0:length(x1)-1;
16 zz=ztransfer(x1,n);
17 //Display the result in command window
18 disp (zz,"Z-transform of sequence is:");
19 // Expected Output:
```

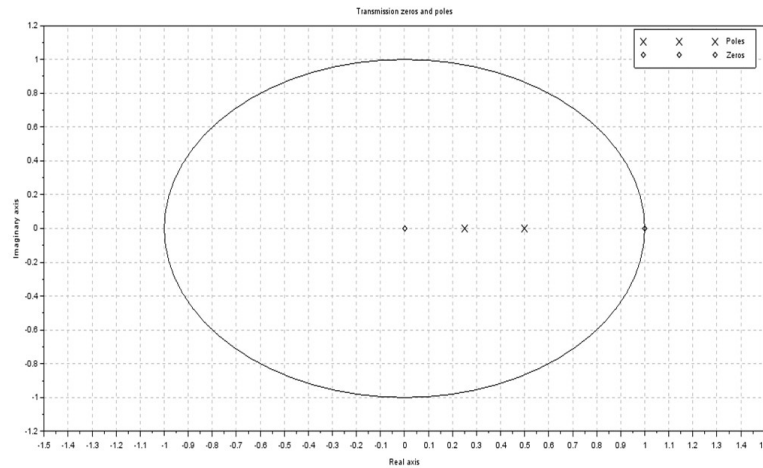


Figure 2.1: Pole Zero Plot of a system

```

20 //Z-transform of sequence is :
21 //      2  4
22 //  2 - z + 3z + z
23 //  -----
24 //      4
25 //      z
26 disp('ROC is the entire plane except z = 0');
27 //ROC is the entire plane except z = 0

```

Scilab code Solution 2.2 Pole Zero Plot of a system

```

1 //Expt2: To draw the pole-zero plot
2 //O.S: Windows 10;
3 //Scilab: 6.0.0
4 clear;
5 clc ;

```

```
6  close ;
7  z=%z
8  H1Z=((z)*(z-1))/((z-0.25)*(z-0.5));
9  xset( 'window' ,1);
10 plzr(H1Z);
```

Experiment: 3

Linear convolution

Scilab code Solution 3.1 Linear Convolution

```
1 //Experiment no 3
2 //Linear Convolution
3 // SciLab version : 6.0.0
4 // O.S. : Windows 10
5 clc;
6 close ;
7 t=0:6;
8 x=[1,2,1,2,1,3,2];
9 subplot(2,2,1);
10 plot2d3 (t,x);
11 xlabel('n');
12 ylabel('x(n)');
13 title('Input sequence x(n)');
14
15 t=0:5;
16 h=[1,-1,2,-2,1,1];
17 subplot(2,2,2);
18 plot2d3 (t,h);
19 xlabel('n');
```

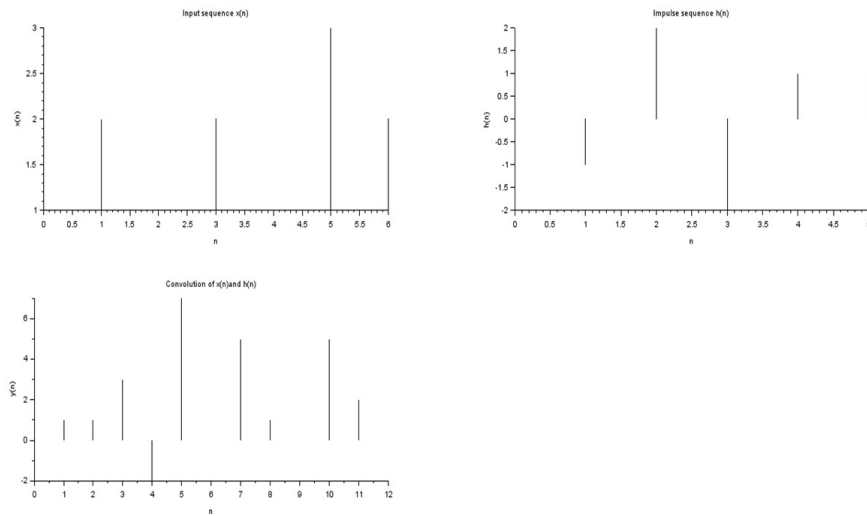


Figure 3.1: Linear Convolution

```

20 ylabel('h(n)');
21 title('Impulse sequence h(n)');
22
23 m = length(x);
24 n = length(h);
25 //Direct Convolution Sum Formula
26 for i = 1:n+m-1
27     conv_sum = 0;
28     for j = 1:i
29         if ((i-j+1) <= n)&(j <= m)
30             conv_sum = conv_sum + x(j)*h(i-j+1);
31         end;
32     y(i) = conv_sum;
33 end;
34 end;
35 disp(y, 'y=');
36 subplot(2,2,3);
37 l=length(y);
38 t=0:(l-1);
39 plot2d3 (t,y);

```

```
40 xlabel('n');  
41 ylabel('y(n)');  
42 title('Convolution of x(n) and h(n)');
```

Experiment: 4

Auto co-relation and cross co-relation

Scilab code Solution 4.1 Auto correlation

```
1 //Experiment no 4
2 //Auto Correlation
3 // SciLab version : 6.0.0
4 // O.S. : Windows 10
5 clear;
6 clc;
7 close;
8 x = input('Enter the given discrete time sequence');
   // Enter a sequence x(n)={1,2,3,4}
9 l = length(x);
10 t=0:l-1;
11 subplot(1,2,1);
12 plot2d3 (t,x);
13 xlabel('n');
14 ylabel('x(n)');
15 title('Input sequence x(n)');
16 h = zeros(1,l);
```

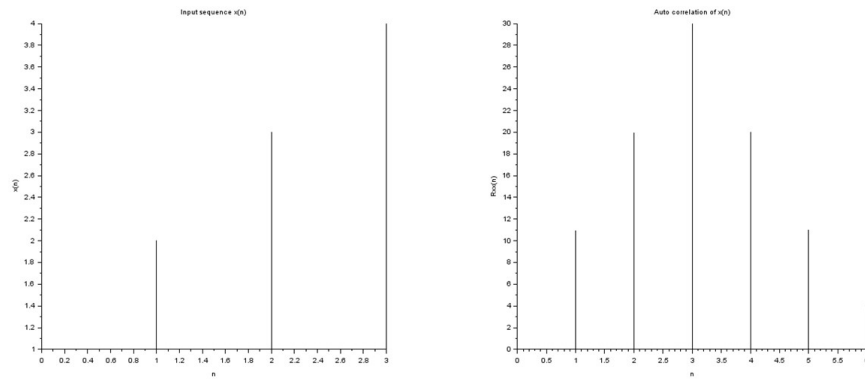


Figure 4.1: Auto correlation

```

17 for i = 1:l
18     h(l-i+1) = x(i);
19 end
20 N = 2*l-1;
21 Rxx = zeros(1,N);
22 for i = l+1:N
23     h(i) = 0;
24 end
25 for i = l+1:N
26     x(i) = 0;
27 end
28 for n = 1:N
29     for k = 1:N
30         if(n >= k)
31             Rxx(n) = Rxx(n)+x(n-k+1)*h(k);
32         end
33     end
34 end
35 disp(Rxx,'Auto Correlation Result is ');//Expected
      output Rxx(n) = {11,20,30,20,11}

```

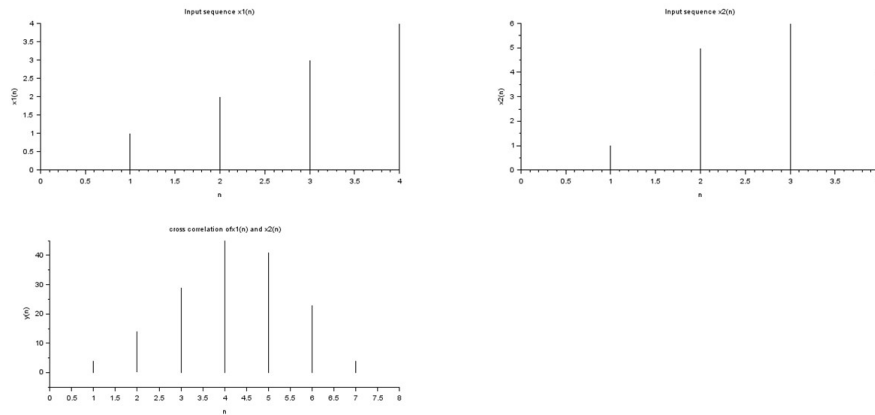


Figure 4.2: Cross correlation

```

36 L=length(Rxx);
37 t=0:L-1;
38 subplot(1,2,2);
39 plot2d3 (t,Rxx);
40 xlabel('n');
41 ylabel('Rxx(n)');
42 title('Auto correlation of x(n)');

```

Scilab code Solution 4.2 Cross correlation

```

1 //Experiment no 4b
2 //cross correlation
3 // SciLab version : 6.0.0
4 // O.S. : Windows 10
5 clc;
6 close ;

```

```

7  t1=0:4;
8  x1=[0,1,2,3,4];
9  subplot(2,2,1);
10 plot2d3 (t1,x1);
11 xlabel('n');
12 ylabel('x1(n)');
13 title('Input sequence x1(n)');
14
15 t2=0:4;
16 x2=[0,1,5,6,4];
17 subplot(2,2,2);
18 plot2d3 (t2,x2);
19 xlabel('n');
20 ylabel('x2(n)');
21 title('Input sequence x2(n)');
22
23 y=xcorr(x1,x2);
24 l=length(y);
25 t3=0:l-1;
26 subplot(2,2,3);
27 plot2d3 (t3,y);
28 xlabel('n');
29 ylabel('y(n)');
30 title('cross correlation of x1(n) and x2(n)');

```

Experiment: 5

Implementation of DFT and IDFT

Scilab code Solution 5.1 Implementation of DFT

```
1 // Expt 5. Implementation of 8 point DFT
2 // O.S. Windows 10
3 //// Scilab 6.0.0
4
5 clear;
6 clc;
7 x1=input('Enter a sequence ');// input a sequence x1
   = {1,1,1,1,0,0,0,0}
8 //DFT Computation
9 X1 = fft (x1 , -1);
10
11 disp(X1,"X1[k]="); //Expected outpput sequences X1[k]
   in command window {4,1-2.4142136i,0,1-0.4142136i
   ,0,1+0.4142136i,0,1+2.4142136i}
12 mag = abs (X1);
13 subplot(1,2,1);
14 plot2d3 (mag);
```

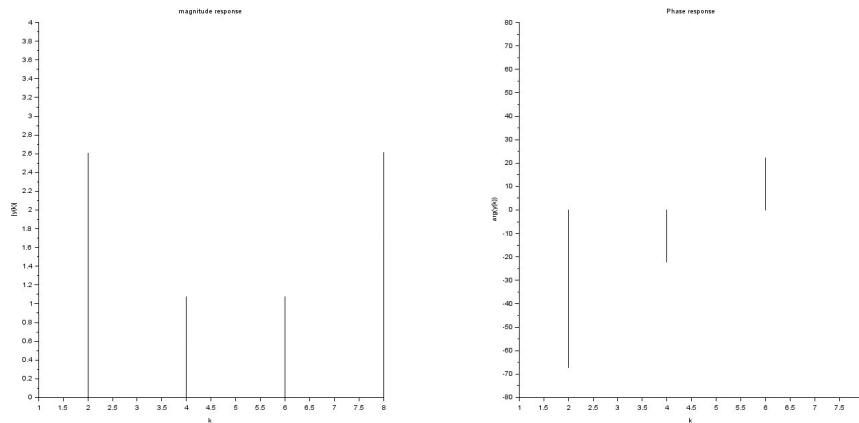


Figure 5.1: Implementation of DFT

```

15 xlabel('k');
16 ylabel('|y(k)|');
17 title('magnitude response');
18
19 x1= atan ( imag (X1),real (X1));
20 phase =x1 *(180/ %pi );
21 subplot(1,2,2);
22 plot2d3 (phase);
23 xlabel('k');
24 ylabel('arg(y(k))');
25 title('Phase response');

```

Scilab code Solution 5.2 Implementation of IDFT

```

1 // Expt 5. IDFT of sequence X[k]=[5,0,1-j,0,1,0,1+j
  ,0]
2 // O.S. Windows 10
3 ////Scilab 6.0.0
4 clear;

```

```

5  clc ;
6  clear;
7  clc ;
8  j=sqrt(-1);
9  X = [5,0,1-j,0,1,0,1+j,0];
10 //IDFT Computation
11 x = fft (X , 1);
12 //Display sequences x[n] in command window
13 disp(x,"x[n]=");
14 // outputx[n]=[1,0.75,0.5,0.25,1,0.75,0.5,0.25]

```

Experiment: 6

circular convolution using FFT

Scilab code Solution 6.1 Circular Convolution using FFT

```
1 // Expt 6. Circular Convolution using FFT
2 // O.S. Windows 10
3 //// Scilab 6.0.0
4 //x1[n]=[1,-1,-2,3,-1]
5 //x2[n]=[1,2,3]
6 clear;
7 clc ;
8 close ;
9 x1=[1,-1,-2,3,-1];
10 x2=[1,2,3];
11 //Loop for zero padding the smaller sequence out of
    the two
12 n1=length(x1);
13 n2=length(x2);
14 n3=n2-n1;
15 if (n3>=0) then
16   x1=[x1,zeros(1,n3)];
17 else
18   x2=[x2,zeros(1,-n3)];
```

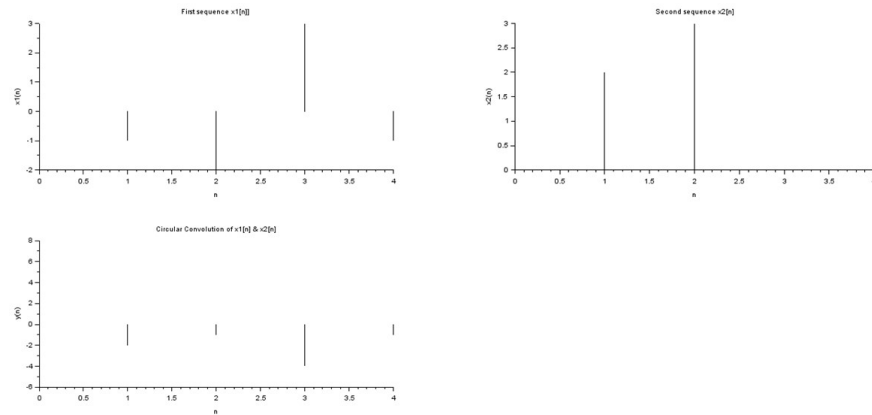


Figure 6.1: Circular Convolution using FFT

```

19 end
20 //DFT Computation
21 X1=fft(x1,-1);
22 X2=fft(x2,-1);
23 Y=X1.*X2;
24 //IDFT Computation
25 y=fft(Y,1);
26 n4=length(y);
27 //Display sequence y[n] in command window
28 disp(y,"y[n]=");
29 // Plotting of sequences
30 t=0:n1-1;
31 subplot(2,2,1);
32 plot2d3(t,x1);
33 xlabel('n');
34 ylabel('x1(n)');
35 title('First sequence x1[n]');
36
37 t1=0:n1-1;
38 subplot(2,2,2);

```

```
39 plot2d3 (t1,x2);
40 xlabel('n');
41 ylabel('x2(n)');
42 title('Second sequence x2[n]');
43
44 t2=0:n1-1;
45 subplot(2,2,3);
46 plot2d3 (t1,y);
47 xlabel('n');
48 ylabel('y(n)');
49 title('Circular Convolution of x1[n] & x2[n]');
```

Experiment: 7

Fast convolution using Overlap add/Overlap save method

Scilab code Solution 7.1 Fast convolution using overlap save method

```
1 // Expt 7 Fast convolution using overlap Save method
2 //O.S. Windows 10
3 //Scilab 6.0.0
4 clc;
5 clear all;
6 x =[1,2,-1,2,3,-2,-3,-1,1,1,2,-1];
7 h =[1,2,3,-1];
8 n1 = length(x);
9 n2 = length(h);
10 N = n1+n2-1;
11 h1 = [h zeros(1,N-n1)];
12 n3 = length(h1);
13 y = zeros(1,N);
14 x1 = [zeros(1,n3-n2) x zeros(1,n3)];
15 H = fft(h1,-1);
16 for i = 1:n2:N
17 y1 = x1(i:i+(2*(n3-n2)));
```

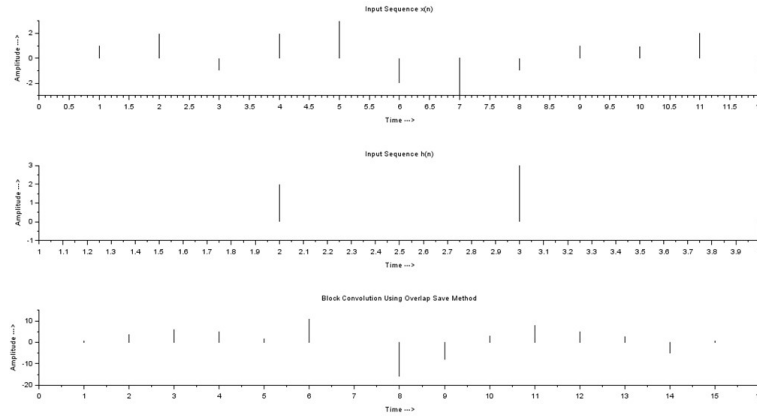


Figure 7.1: Fast convolution using overlap save method

```

18 y2 = fft(y1);
19 y3 = y2.*H;
20 y4 = round(fft(y3,1));
21 y(i:(i+n3-n2)) = y4(n2:n3);
22 end
23 subplot(3,1,1);
24 plot2d3(x(1:n1));
25 title('Input Sequence x(n)');
26 xlabel('Time —>');
27 ylabel('Amplitude —>');
28 subplot(3,1,2);
29 plot2d3(h(1:n2));
30 title('Input Sequence h(n)');
31 xlabel('Time —>');
32 ylabel('Amplitude —>');
33 subplot(3,1,3);
34 disp('Fast Convolution Using Overlap Save Method = ');
35 disp(y(1:N));
36 plot2d3(y(1:N));

```

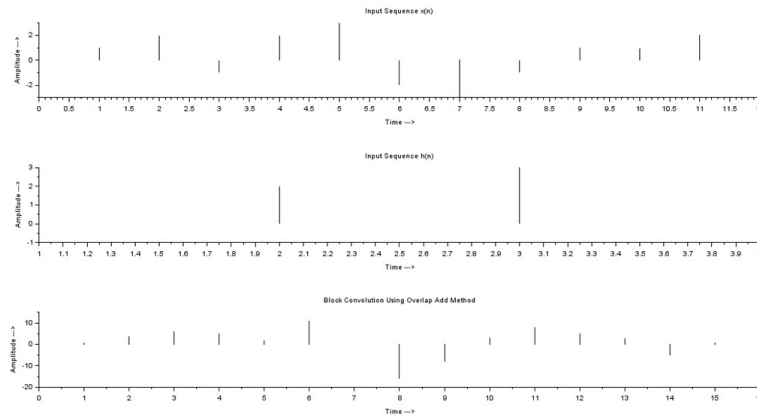


Figure 7.2: Fast convolution using overlap add method

```

37 title('Block Convolution Using Overlap Save Method')
38 ;
39 xlabel('Time ——>');
40 ylabel('Amplitude ——>');
41 // result:Fast Convolution Using Overlap Save Method
42 //      =
      1      4      6      5      2      11      0      -16
     -8      3      8      5      3      -5      1

```

Scilab code Solution 7.2 Fast convolution using overlap add method

```

1 // Expt 7 Fast convolution using overlap add method
2 //O.S. Windows 10
3 //Scilab 6.0.0
4

```

```

5  clc;
6  clear;
7  x = [1,2,-1,2,3,-2,-3,-1,1,1,2,-1];
8  h = [1,2,3,-1];
9  n1 = length(x);
10 n2 = length(h);
11 N = n1+n2-1;
12 y = zeros(1,N);
13 h1 = [h zeros(1,n2-1)];
14 n3 = length(h1);
15 y = zeros(1,N+n3-n2);
16 H = fft(h1,-1);
17 for i = 1:n2:n1
18 if i<=(n1+n2-1)
19 x1 = [x(i:i+n3-n2) zeros(1,n3-n2)];
20 else
21 x1 = [x(i:n1) zeros(1,n3-n2)];
22 end
23 x2 = fft(x1,-1);
24 x3 = x2.*H;
25 x4 = round(fft(x3,1));
26 if (i==1)
27     y(1:n3) = x4(1:n3);
28 else
29 y(i:i+n3-1) = y(i:i+n3-1)+x4(1:n3);
30 end
31 end
32 subplot(3,1,1);
33 plot2d3(x(1:n1));
34 title('Input Sequence x(n)');
35 xlabel('Time —>');
36 ylabel('Amplitude —>');
37 subplot(3,1,2);
38 plot2d3(h(1:n2));
39 title('Input Sequence h(n)');
40 xlabel('Time —>');
41 ylabel('Amplitude —>');
42 subplot(3,1,3);

```

```

43 disp('Fast Convolution Using Overlap Add Method = ')
    ;
44 disp(y(1:N));
45 plot2d3(y(1:N));
46 title('Fast Convolution Using Overlap Add Method');
47 xlabel('Time ——>');
48 ylabel('Amplitude ——>');
49 // Result:Fast Convolution Using Overlap Add Method
    =
50 //      1      4      6      5      2      11      0      -16
        -8      3      8      5      3      -5      1

```

Experiment: 8

Realization of FIR system

Scilab code Solution 8.1 Program to determine filter coefficients obtained by sampling

```
1 // Expt 8. Program to determine filter coefficients
   obtained by sampling:
2 // O.S. Windows 10
3 // Scilab 6.0.1
4 clear;
5 clc ;
6 close ;
7 N=7;
8 U=1;          //Zero Adjust
9 for n=0+U:1:N-1+U
10 h(n)=(1+2*cos(2*%pi*(n-U-3)/7))/N
11 end
12 disp(h," Filter Coefficients ,h(n)=")
13 // Filter Coefficients ,h(n)=
14
15 // -0.1145625
16 // 0.0792797
17 // 0.3209971
18 // 0.4285714
19 // 0.3209971
```

20 // 0.0792797
21 // -0.1145625

Experiment: 9

Design of FIR filter using frequency sampling method.

Scilab code Solution 9.1 Design of FIR LPF using frequency sampling method

```
1 //Exp 9. FIR LPF using frequency Sampling Method
2 //O.S. Windows 10;
3 // Scilab 6.0.0.
4 clc ;
5 clear ;
6 N =15;
7 U=1;
8 for n=0+U:1:N-1+U
9 h(n)=(1+cos(2*%pi*(7-n)/N))/N;
10 end
11 [hz,f]=frmag(h,256);
12 hz_dB=20*log10(hz)./max(hz);
13 figure;
14 plot(2*f,hz_dB);
15 a=gca();
16 xlabel('Frequency wpi');
```

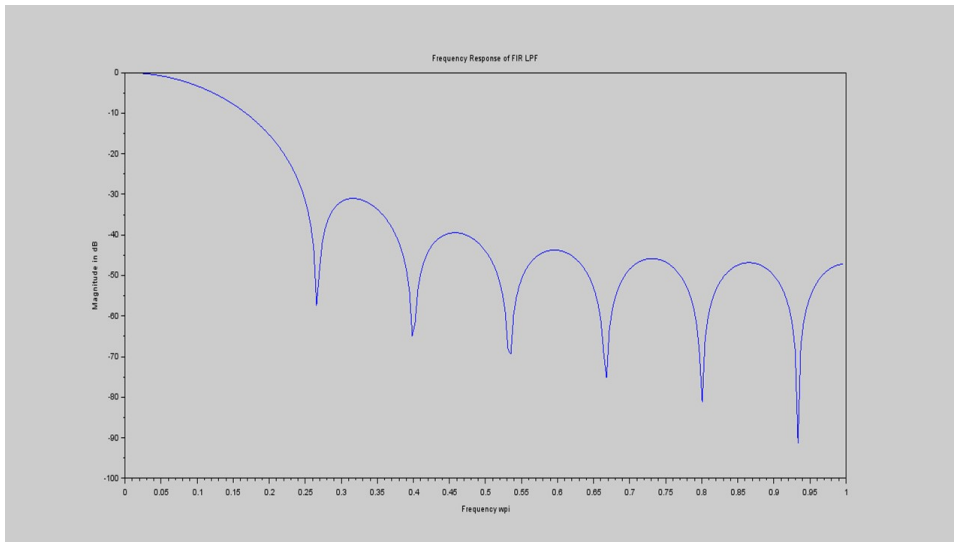


Figure 9.1: Design of FIR LPF using frequency sampling method

```

17 ylabel('Magnitude in dB') ;
18 title ('Frequency Response of FIR LPF');

```

Experiment: 10

Design of FIR filter using windowing technique.

Scilab code Solution 10.1 FIR Filter using rectangular window

```
1 //Expt. 10 Design of FIR filter (Band Pass) using
   windowing technique (Kaiser Window)
2 // O.S. Windows 10
3 // Scilab 6.0.0.
4 clear;
5 clc ;
6 close ;
7 wsf=200*%pi; //rad/sec
8 ws1=20*%pi; //rad/sec
9 ws2=80*%pi; //rad/sec
10 wp1=40*%pi; //rad/sec
11 wp2=60*%pi; //rad/sec
12 as=30 //dB
13 ap=0.5 //dB
14 B=min(wp1-ws1, ws2-wp2);
15 wc1=wp1-B/2;
16 wc2=wp2+B/2;
```

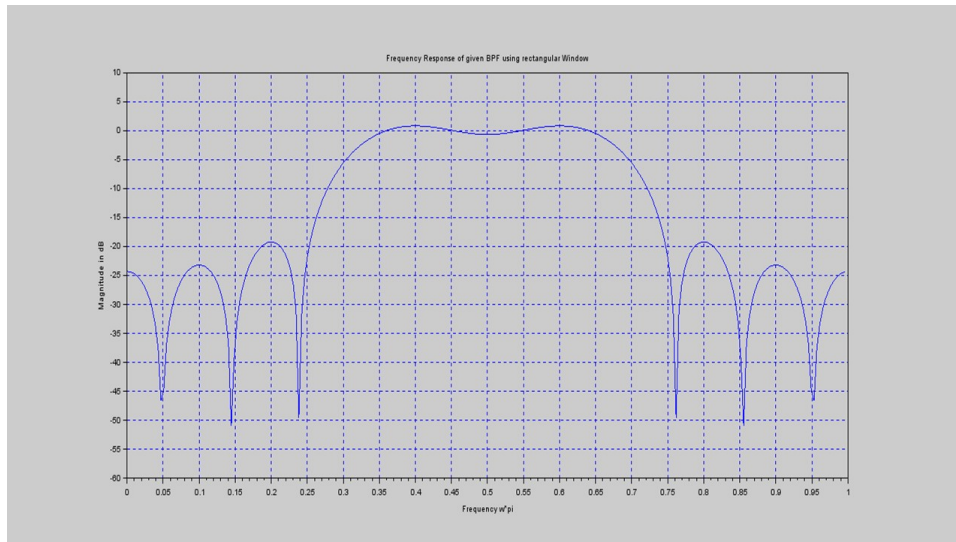


Figure 10.1: FIR Filter using rectangular window

```

17 wc1=wc1*2*%pi/wsf;
18 wc2=wc2*2*%pi/wsf;
19 delta1=10^(-0.05*as);
20 delta2=(10^(0.05*as)-1)/(10^(0.05*as)+1);
21 delta=min(delta1,delta2);
22 alphas=-20*log10(delta);
23 alpha=0.5842*(alphas-21)^0.4+0.07886*(alphas-21)
24 D=(alphas-7.95)/14.36;
25 N1=wsf*D/B+1;
26 N=ceil(N1);
27 U=ceil(N/2);
28 win_l=window('re',N,alpha);
29 for n=-floor(N/2)+U:1:floor(N/2)+U
30 if n==ceil(N/2);
31 hd(n)=0.4;
32 else
33 hd(n)=(sin(0.7*%pi*(n-U))-sin(0.3*%pi*(n-U)))/(%pi*(
    n-U));
34 end
35 h(n)=hd(n)*win_l(n);

```

```

36 end
37 [hzm ,fr ]= frmag (h ,256) ;
38 hzm_dB = 20* log10 (hzm)./ max ( hzm );
39 figure
40 plot (2*fr , hzm_dB )
41 a= gca ();
42 xlabel ('Frequency w*pi ');
43 ylabel ('Magnitude in dB');
44 title ('Frequency Response of given BPF using
         rectangular Window');
45 xgrid (2);
46 disp(h," Filter Coefficients ,h(n)=");

```

Experiment: 11

Design of IIR filter using impulse invariant technique.

Scilab code Solution 11.1 Design of IIR Filter using Impulse Invariant technique

```
1 //Expt.11:To Design the Filter using Impulse
  Invariant Method
2 // O.S. Windows 10
3 //Scilab: 6.0.0
4 clear;
5 clc ;
6 close ;
7 s=%s;
8 T=0.2;
9 HS=10/(s^2+7*s+10);
10 elts=pfss(HS);
11 disp(elts,'Factorized HS = ');
12 //Outputs:
13 //Factorized HS =
14 // (1)
15 // 3.3333333
16 // -----
17 // 2 + s
```

```

18 // (2)
19 // -3.3333333
20 // -----
21 // 5 + s
22
23 //The poles comes out to be at -5 and -2
24 p1=-5;
25 p2=-2;
26 z=%z;
27 HZ=T*((-3.33/(1-%e^(p1*T)*z^(-1)))+(3.33/(1-%e^(p2*T
    )*z^(-1))))
28 disp(HZ,'HZ = ');
29 //Result:
30 //HZ =
31 //      0.2014254z
32 // -----
33 //                                     2
34 // 0.2465970 - 1.0381995z + z

```

Experiment: 12

Design of IIR filters using Bilinear transformation/Butterworth Technique.

Scilab code Solution 12.1 IIR filter design using Bilinear Transformation Technique

```
1 //Expt 12 Design of IIR filters using Bilinear
   transformation/Butterworth Technique.
2 //To Find out Bilinear Transformation of  $HS=2/((s+1)
   *(s+2)*(s+3))$ 
3 // O.S. Windows 10;
4 //Scilab 6.0.0
5 clear;
6 clc ;
7 close ;
8 s=%s;
9 z=%z;
10 HS=2/((s+1)*(s+2)*(s+3));
11 T=1;
12 HZ=horner(HS,(2/T)*(z-1)/(z+1));
```

```

13 disp(HZ,'H(z) =');
14
15 //H(z) =
16
17 // .. .      2      3
18 //      2 + 6z + 6z + 2z
19 //      -----
20 //              2      3
21 //      -4z - 8z + 60z

```

Experiment: 13

Design of IIR Filters Chebyshev

Scilab code Solution 13.1 To Design an analog Chebyshev Filter with Given Specifications

```
1 //Expt 13 To Design an analog Chebyshev Filter with
  Given Specifications
2 // O.S. Windows 10;
3 // Scilab 6.0.0
4 clear;
5 clc ;
6 //
7 os=2;
8 op=1;
9 ap=3; //db
10 as=16; //db
11 e1=1/sqrt(2);
12 l1=0.1;
13 epsilon=sqrt(1/(e1^2)-1);
14 lambda=sqrt(1/(l1^2)-1);
15 N=acosh(lambda/epsilon)/acosh(os/op);
16 disp(ceil(N), 'Order of the filter , N =');
17
```

```
18 // Result:
19 //Order of the filter , N =
20
21 // 3.
```
